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NONCONTACT NONDESTRUCTIVE DETERMINATION OF PAVEMENT  
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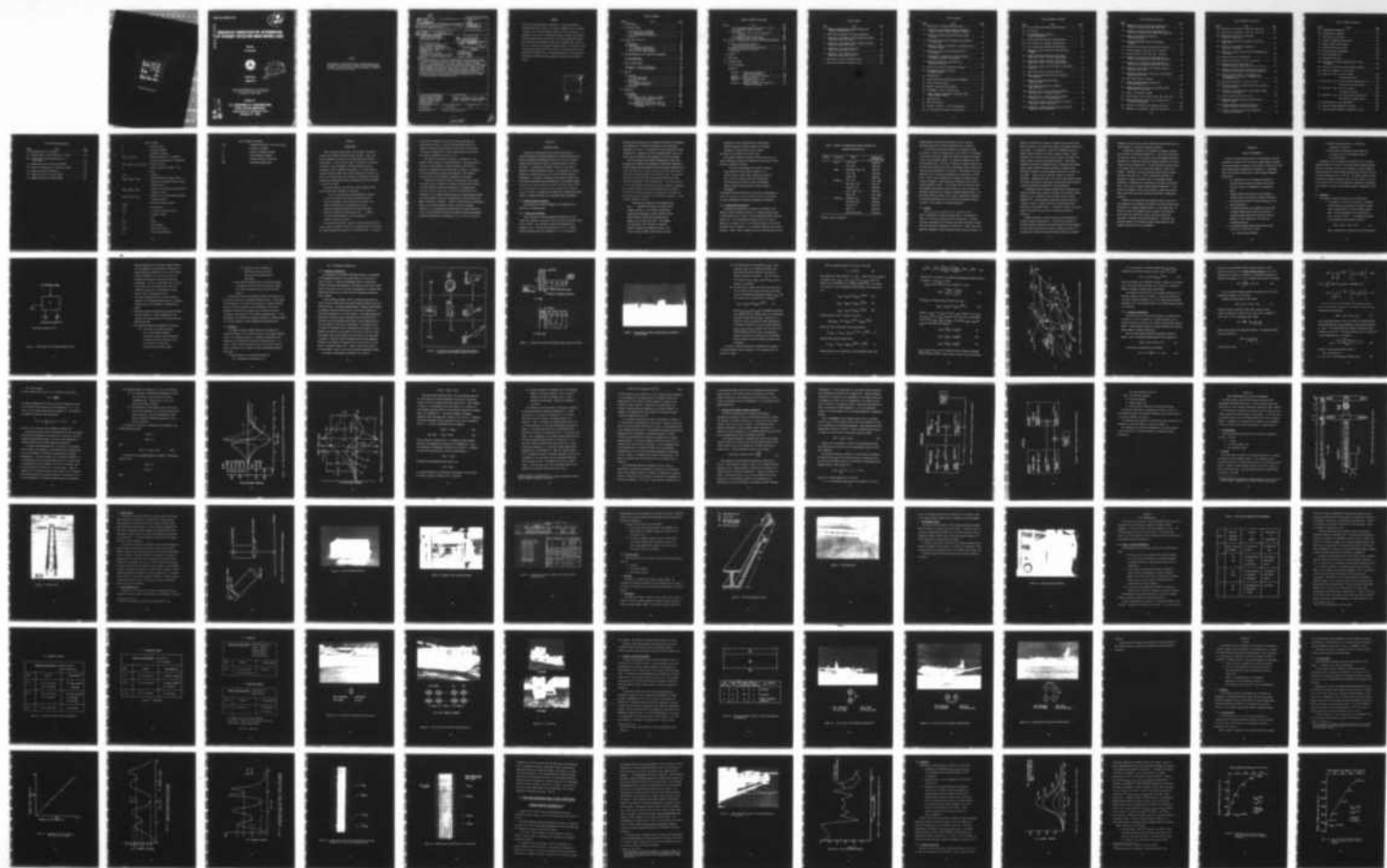
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# NONCONTACT NONDESTRUCTIVE DETERMINATION OF PAVEMENT DEFLECTION UNDER MOVING LOADS

M.E. Harr  
N.T. Ng-A-Qui



Final Report  
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16. Abstract This report presents a procedure for nondestructively evaluating and predicting the deflection response of various flexible pavements to loads imposed by different aircraft. Transfer function theory is used to form the basis of a pavement evaluation and response scheme. Two mobile systems were developed for the measurement of pavement deflections; the Light Emitting Diode (LED) system and the Linear Variable Differential Transformer (LVDT) system. The report concludes that the rapid nondestructive measurement of pavement deflections due to moving prototype loads is feasible and that a total nondestructive evaluation scheme based entirely on the use of prototype loads and measured deflections can be fabricated to evaluate and predict instantaneous response and cumulative effects of loads of various magnitudes and configurations. ←			
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## PREFACE

This work was conducted under sponsorship of the Federal Aviation Administration (FAA) as part of the runway roughness study to determine the effect of the loaded pavement profile on aircraft operations. An outgrowth of this study is a noncontact system to measure the pavement deflection basin under a moving load. This report describes the hardware developed and associated transfer function theory which forms the basis for a pavement evaluation and response scheme. (The effect of the loaded pavement profile will be the subject of a separate report to be published in September 1977.) Continued development of the noncontact system reported herein is being sponsored by the FAA under separate contract.

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# TABLE OF CONTENTS

Section	Title	Page
I.	INTRODUCTION . . . . .	1
II.	LITERATURE REVIEW . . . . .	3
2.1	Airfield Pavement Evaluation . . . . .	3
2.1.1	Destructive Evaluation . . . . .	3
2.1.2	Nondestructive Evaluation . . . . .	5
2.2	Analysis . . . . .	7
III.	THEORY AND METHODOLOGY . . . . .	10
3.1	Hypotheses . . . . .	11
3.2	Evaluation . . . . .	14
3.2.1	Signature Determination . . . . .	15
3.2.2	Parameter Determination . . . . .	23
3.3	Prediction of Pavement Response . . . . .	33
IV.	NEW INSTRUMENTATION FOR DEFLECTION MEASUREMENT . . . . .	38
4.1	The LED System . . . . .	38
4.2	The LVDT System . . . . .	46
V.	FIELD INVESTIGATIONS . . . . .	51
5.1	Series A - Field Investigation . . . . .	51
5.2	Series B - Field Investigation . . . . .	60
VI.	RESULTS . . . . .	66
6.1	Equipment . . . . .	66
6.1.1	The LVDT System . . . . .	66
6.1.2	The LED System . . . . .	67
6.2	Evaluation . . . . .	77
6.2.1	Pavement Deflections . . . . .	77
6.2.2	Transfer Functions . . . . .	89
6.3	Prediction . . . . .	102
VII.	DISCUSSION . . . . .	105
7.1	Equipment . . . . .	105
7.2	Evaluation . . . . .	111
7.2.1	Concepts Used in Computer Programs . . . . .	112
7.2.2	Parameter of the Maximum Lateral Deflection Profile . . . . .	116
7.2.3	Parameters of the Transfer Function . . . . .	118
7.2.4	Relationship Between the k and A <sub>peak</sub> Parameters . . . . .	128

# TABLE OF CONTENTS (Continued)

Section	Title	Page
	7.2.5 Approximate Method to Estimate k, c and m . . . .	131
	7.2.6 Estimating Design Parameters . . . . .	136
7.3	Prediction . . . . .	139
	7.3.1 Validity of the Concept of Equivalency Function . . . . .	140
	7.3.2 Effects of Gear Configurations . . . . .	142
	7.3.3 Relative Effects of k, c and m . . . . .	143
VIII.	EFFECTS OF DISTRIBUTION OF PASSES ON PAVEMENT PERFORMANCE .	144
	8.1 Pass to Coverage Ratio Based on Tire-Contact Area Width . . . . .	144
	8.2 Deflection Based Pass to Coverage Ratio . . . . .	148
	8.3 Effect of Lateral Distribution . . . . .	151
	8.4 Discussion . . . . .	152
IX.	SUMMARY . . . . .	160
X.	CONCLUSIONS . . . . .	162
XI.	RECOMMENDATIONS . . . . .	164
	LIST OF REFERENCES . . . . .	166
	APPENDICES . . . . .	173
	Appendix A: Research and Development of Measurement Systems . . . . .	173
	Appendix B: Series A: Field Investigations . . . . .	191
	Appendix C: Computer Programs . . . . .	210
	Appendix D: Data Digitized from Light Sensitive Paper . . . . .	248
	Appendix E: Example of Simplified Procedure for Estimating k and CBR . . . . .	312

## LIST OF TABLES

Table	Title	Page
1.	Summary of Nondestructive Testing Equipment and Pertinent Characteristics . . . . .	6
2.	Field Testing Equipment Development Methodology . . . . .	52
3.	Parameters of the Maximum Lateral Deflection Profile: Eglin AFB, March 1976: Site 1 . . . . .	82
4.	Parameters of the Maximum Lateral Deflection Profile: Eglin AFB, March 1976: Site 2 . . . . .	83
5.	Parameters of the Transfer Function: Eglin AFB, March 1976: Site 1 . . . . .	99
6.	Parameters of the Transfer Function: Eglin AFB, March 1976: Site 2 . . . . .	100
7.	Data Used in Lateral Distribution Study . . . . .	152
8.	Data Used in Lateral Distribution Study . . . . .	158

## LIST OF FIGURES

Figure	Title	Page
1.	Kelvin Model of Pavement-Subgrade System . . . . .	12
2.	An Overview of the Transfer Function Concept as Applied to Wheel-Pavement-Subgrade Interaction . . . . .	16
3.	Location of Signature and Relative Gage Location and Setup . . . . .	17
4.	Setup During Stationary Beam-Moving Load Operation: P-2 Fire truck . . . . .	18
5.	Overview of Method of Calculation of Signature Due to Prototype Loading . . . . .	22
6.	Typical Zero, First and Second Derivatives of the Signature . . . . .	28
7.	Determination of Parameter of Transfer-Function - A Graphical Overview of Methodology . . . . .	29
8.	Overview of Scheme for Determining the Equivalency Function . . . . .	35
9.	Overview of Scheme for Predicting Signature . . . . .	36
10.	Light Emitting Diode (LED) Beam: Schematic Details . . . . .	39
11.	LED Beam Setup . . . . .	40
12.	Light Emitting Diode Triangulation Arrangement . . . . .	42
13.	Typical LED Sensor Module . . . . .	43
14.	Magnetic Tape Recording Equipment . . . . .	44
15.	Arrangement of Data of Magnetic Tape . . . . .	45
16.	Linear Variable Differential Transformer (LVDT) Beam: Schematic Details . . . . .	47
17.	LVDT Beam Setup . . . . .	48
18.	Light Beam Recorder . . . . .	50
19.	Synopsis of Series A - Field Investigations . . . . .	54
20.	F-4 Aircraft and Pertinent Characteristics . . . . .	57

# LIST OF FIGURES (Continued)

Figure	Title	Page
21.	P-2 Fire Truck and Pertinent Characteristics . . . . .	58
22.	F-4 Load Cart . . . . .	59
23.	Site Characteristics: Series B - Field Investigations . . . . .	61
24.	C-130 Aircraft and Pertinent Characteristics . . . . .	62
25.	C-131 Aircraft and Pertinent Characteristics . . . . .	63
26.	C-135 Aircraft and Pertinent Characteristics . . . . .	64
27.	Comparison of LVDT on Beam and LVDT Installed in Pavement . . . . .	68
28.	Pavement Deflections Measured by LED System: Eglin AFB - Site 1: P-2 Fire Truck Loading . . . . .	69
29.	Pavement Deflections Measured by LVDT System: Eglin AFB - Site 1: P-2 Fire Truck Loading . . . . .	70
30.	Actual Digital Output From LED System on Light Beam Recorder . . . . .	71
31.	Analog Output from LVDT System (Typical) . . . . .	72
32.	Setup During Moving Beam-Moving Load Operation: F-4 Load Cart . . . . .	75
33.	Summary of Taxiway Deflection Data: Eglin AFB: Site 1 . . . . .	76
34.	System Response Functions F-4 Loading: Eglin AFB: Site 1 . . . . .	78
35.	Eglin AFB: Site 1: Lateral Profile of Maximum Deflections for F-4 Loading (Typical) . . . . .	80
36.	Eglin AFB: Site 2: Lateral Profile of Maximum Deflections for F-4 Loading (Typical) . . . . .	81
37.	Variability of Maximum Lateral Deflection Profile: Eglin AFB - Site 1, March 1976 . . . . .	84
38.	Variability of Maximum Lateral Deflection Profile: Eglin AFB, Site 2, March 1976 . . . . .	85



# LIST OF FIGURES (Continued)

Figure	Page
39. Comparison of Local and Site Characteristics as shown by $\beta_r$ Values: Eglin AFB, March 1976 . . . . .	86
40. Comparison of Local and Site Characteristics as shown by A-Parameter Values: Eglin AFB, March 1976 . . . . .	87
41. Effect of Two Consecutive Passes on Measured Deflection . . . . .	88
42. Calculated Equivalent Force and Components (Typical) . . . . .	91
43. Comparison of Newtonian and Convolution Solutions . . . . .	92
44. Transfer Function: Eglin AFB, Site 1 (Typical) . . . . .	93
45. Transfer Function: Eglin AFB, Site 2 (Typical) . . . . .	94
46. Comparison of Local and Site Characteristics as shown by the k-Parameters: Eglin AFB, March 1976 . . . . .	95
47. Comparison of Local and Site Characteristics as shown by the c-Parameters: Eglin AFB, March 1976 . . . . .	96
48. Comparison of the Peaks of the Transfer Function: Eglin AFB, March 1976 . . . . .	97
49. Comparison of the Time to First Peak of TDT Function: Eglin AFB, March 1976 . . . . .	98
50. Input-Output Relation (Typical) . . . . .	101
51. Typical Comparison Between Measured and Predicted Signatures . . . . .	103
52. Summary Comparison of Measured and Predicted Peak Deflections for Two Sites . . . . .	104
53. Summary of Measurement Systems . . . . .	107
54. Runway Overrun Tests: Eglin Air Force Base, March 1976 . . . . .	110
55. Sketch showing the Concept of the Criteria Used in Parameter Determination . . . . .	114
56. Comparison of Calculated and Measured Signatures . . . . .	117
57. Comparison of A-Parameters: Eglin AFB, March 1976 . . . . .	119

# LIST OF FIGURES (Continued)

Figure	Title	Page
58.	Comparison of $\beta$ -Parameters: Eglin AFB, March 1976 . . . .	120
59.	Comparison of $r$ -Parameters: Eglin AFB, March 1976 . . . .	121
60.	Comparison of Equivalent $k$ -Parameters: Eglin AFB, March 1976 . . . . .	123
61.	Comparison of Equivalent $c$ -Parameters: Eglin AFB, March 1976 . . . . .	124
62.	Comparison of Equivalent $m$ -Parameters: Eglin AFB, March 1976 . . . . .	125
63.	Locations of Stations where Relative Stiffnesses were Determined . . . . .	126
64.	Histogram of Relative Stiffnesses . . . . .	127
65.	Relationship Between the $A$ and $k$ Parameters . . . . .	129
66.	Nondestructive Evaluation Curves for Flexible Pavement, Single Wheel Load, 100 sq. in. . . .	130
67.	Frequency Characteristics of Forces at the Points of Inflection, Crossing Point and Maximum Deflection . . .	132
68.	Frequency Characteristics of Normalized Time Corresponding to the Point of Inflection and the Crossing Point . . . . .	134
69.	Approximate Correlation of CBR and $k$ -Value . . . . .	138
70.	Lateral Distribution of Aircraft Used in the Design of Airfield Pavements . . . . .	146
71.	Overview of the Concept Used in the Deflection Based $p/c$ Ratio Calculations . . . . .	149
72.	Discrete Distributions Used in Study . . . . .	153
73.	Relationship Between Cumulative Deflections and Number of Passes . . . . .	154
74.	Effects of Frequency and Characteristics of Lateral Deflection Profile of $p/c$ Ratio . . . . .	155
75.	Overview of Evaluation Scheme Using Deflection Frequency Relationship . . . . .	157

# LIST OF FIGURES (Continued)

Figure	Title	Page
A-1	Triangulation Arrangement . . . . .	175
A-2	Triangulation Parameters . . . . .	176
A-3	Laser Setup in Laboratory . . . . .	179
A-4	Typical Triangulation Displacement . . . . .	180
A-5	Normal Incidence Displacement . . . . .	181
A-6	Normalized Deflection Curves . . . . .	182
A-7	LED Triangulation Arrangement . . . . .	184
A-8	LED Displacement Curve . . . . .	185
A-9	Repackaged Electronics . . . . .	186
A-10	Test Setup for Moving Beam-Moving Load--Purdue University . . . . .	188
A-11	Flow Chart of LED System Data Reduction Software . . . . .	189
A-12	Details of Components of LVDT System . . . . .	
B-1	Eglin AFB - Site 1 (A) Site location . . . . .	192
	(B) Station locations . . . . .	192
B-2	Eglin AFB - Site 1 (A) Site profile characteristics . . . . .	193
	(B) Details of boring location . . . . .	193
B-3	Eglin AFB - Site 2 (A) Site location . . . . .	194
	(B) Station locations . . . . .	194
B-4	Eglin AFB - Site 2 (A) Site profile characteristics . . . . .	195
	(B) Details of boring location . . . . .	195
B-5	Photo Sequence of Gage Installation . . . . .	196
B-6	Details of Gages Installed in Pavement . . . . .	204
B-7	Gage Calibration Equipment (Micrometer on Mount) . . . . .	205

# LIST OF FIGURES (Concluded)

Figure	Title	Page
B-8	Typical Pass by P-2 Fire Truck . . . . .	206
B-9	Typical Results of Peak Deflections - KC135A . . . . .	208
B-10	Typical Results of Peak Deflections - P-2 Fire Truck . . . . .	209
C-1	Summary Flow Chart of Subroutine EXACFIT . . . . .	211
C-2	Details of Interpolation in Subroutine EXACFIT . . . . .	212
C-3	Definition Sketch for Signature . . . . .	215
C-4	Summary Flow Chart of Program FNDPRM . . . . .	216
C-5	Summary Flow Chart of Program PREDCT . . . . .	222

# LIST OF SYMBOLS

$m$	- equivalent mass
$c$	- equivalent damping
$k$	- equivalent stiffness
$z(t), \dot{z}(t), \ddot{z}(t)$	- pavement deflection (or signature), velocity and acceleration, respectively
$F(t), F_{sn}(t), F_x(t), F_{ln}(t)$	- loading function
$x$	- lateral distance from edge of tire print
$A(t)$	- signature
$A'_{peak}, A''_{peak}, A_{peak}$	- maximum deflection at edge of wheel, parameter of the maximum lateral dynamic deflection basin
$\beta'_{peak}, \beta''_{peak}, \beta_{peak}$	- parameter of the maximum lateral dynamic deflection profile
$r'_{peak}, r''_{peak}, r_{peak}$	- parameter of the maximum lateral dynamic deflection profile
$z_{max,j}$	- maximum deflection at gage $j$
$I(t)$	- modified input
$G(t)$	- the reduced transfer function
$s$	- a complex variable
$t$	- time
$O(t)$	- output
$\Delta T$	- time increment
$EF(t)$	- equivalency function
$T_p$	- time to peak deflection

# LIST OF SYMBOLS (Concluded)

$W(x)$	- subgrade deflection at $x$ from tire print
$p$	- pressure on subgrade
$\bar{k}$	- modulus of subgrade reaction
$CH$	- shear stiffness parameter
$E_s$	- subgrade modulus of elasticity
CBR	- California Bearing Ratio

## SECTION I

### INTRODUCTION

Today, personnel concerned with the evaluation of airfield pavements are confronted with three major problems. First, many primary pavements are old and/or are approaching early stages of deterioration. Second, the gross weight of aircraft is increasing continually, thus the demands on airfield pavements are also increasing. Third, procedures (References 1, 2, 3 and 4) used to evaluate airfield pavements are; either, destructive in nature, or, apply to only small areas of the pavement: in addition, they require considerable performance time and are therefore costly with respect to the flow of traffic.

The problem faced by the Air Force in this context has been stated by one author (Reference 5) who wrote,

"The Air Force alone owns enough pavement to be able to provide a 200-foot wide runway stretching from the state of Washington to the Southern tip of Florida. The problem of maintenance and rehabilitation of this inventory becomes more complex and critical each year. Most of the systems are over 20 years old . . . coupled with these aging pavements is the rapid growth of aircraft traffic and weights."

The need exists today for a method of pavement evaluation which would be able to quantify the stage of the aging process of a pavement and provide guidance with respect to its rehabilitation. It should be



able to do so considering the action of varying magnitudes and configurations of loads, and under varying ambient conditions. Ideally, it should be nondestructive, rapid, permit the evaluation of the entire pavement with a minimum interruption to air traffic, and should be inexpensive and easy to use.

The problem of evaluating a pavement is a complex one. The pavement section consists of various materials. These materials are far from the ideal models of classical mechanics; and they vary diurnally, seasonally and with repetitions of loading. In addition, both vehicular and non-vehicular loads applied to the pavement-subgrade system vary in magnitude, intensity, and frequency.

Recognizing the nature and scope of the problem, and the need that exists today to overcome it, research activities were initiated at Purdue University toward the development of a nondestructive pavement evaluation capability to account for the complexity and variability of the pavement-subgrade system, and simultaneously satisfy the demands imposed by practical considerations; such as mobility and ease of operation of equipment. Research in this endeavor is predicated on the use of transfer function theory as the key to pavement evaluation. This methodology has evolved over a 15 year period from concept, through theory and laboratory studies to field investigations using fixed installations (References 6, 7, 8, 9, 10, 11, 12 and 13).

## SECTION II

### LITERATURE REVIEW

The need for improving methods and developing theories to quantify adequately the complex mechanism of pavement-subgrade interaction has generated considerable activity in the area of pavement analysis and evaluation in general, and nondestructive testing in particular. In evaluation procedures, efforts are being made to eliminate or reduce destructive testing. In nondestructive testing emphasis is currently being put on the use of surface deflection measurements. In analysis, attempts are being made to deviate from the classical approaches and use probabilistic and stochastic models. Because in the recently published literature several excellent state of the art papers and literature reviews already exist (References 14, 15, 16 and 17), no attempt will be made here to repeat these works, however, a synoptic overview of the principal works is presented.

#### 2.1 Airfield Pavement Evaluation

The evaluation of airfield pavements can be categorized as destructive or nondestructive.

##### 2.1.1 Destructive Evaluation

These procedures, as the name implies, destroy parts of the system; and, generally, involve the use of test pits, laboratory and/or in situ testing. Five procedures, with minor modifications are currently in use. These are the procedures of the U. S. Federal Aviation Administration (FAA) (Reference 1); U. S. Navy Bureau of

Yards and Docks (Reference 2); the Canadian Department of Transportation (Reference 3); the British Department of the Environment (Reference 4) and the U. S. Department of the Army and the Air Force (Reference 18). Basically, the five procedures involve the use of field tests in conjunction with sampling and laboratory testing.

The FAA procedure uses California Bearing Ratio (CBR) tests conducted in accordance with procedures in MIL-STD 621A Method 101. The Navy method uses non-repetitive plate load tests conducted according to specifications of American Society for Testing and Materials (ASTM) Test Method-Designation D-1196 (Reference 19). The Canadian practice uses repetitive plate bearing tests specified in ASTM Test Method Designation D-1195 (Reference 20). The British procedure also uses repetitive plate bearing tests but these are conducted in a slightly different manner from the ASTM D-1195 Test Method. The Air Force evaluation procedure is summarized in the report of the testing program conducted in a recent (1975) evaluation. It was reported (Reference 21) that,

"Field testing consisted of 28 exploratory test pits . . . Thickness measurements were made on each pavement component, in situ density and moisture contents were determined, values of Modulus of Subgrade Reaction and CBRs were obtained and bulk samples of soil layers were taken. Core samples were extracted at 184 locations to ascertain pavement thickness and subsurface profile. Laboratory testing included classification of soils;

development of soil moisture-density relationships; Marshall testing of asphaltic concrete; and tensile splitting of Portland cement concrete cores."

The period of the evaluation was about 8 days.

The prevalent feeling concerning the use of test pits, and current destructive evaluation procedures was quite aptly put when one author (Reference 22) wrote,

"Yet most civil engineers still cannot scientifically evaluate the load carrying capacity of an airport pavement without first rendering it unserviceable in a way no aircraft could have accomplished. The resulting test pits when filled and resurfaced remain as abrupt discontinuities to uniform pavement performance."

This general feeling coupled with the many other disadvantages of destructive testing has directed research towards the development of rapid, nondestructive evaluation equipment and procedures.

#### 2.1.2 Nondestructive Evaluation

Nondestructive procedures are based on the analysis of the measured surface deflection response of a pavement-subgrade system to loads applied at the surface. The main differences among existing methods are: (1) the magnitude and manner in which the load is applied to the surface, and (2) the particular aspect of the surface disturbance that is measured, i.e., deflection magnitude, wave length, frequency. Table 1 shows a summary of the major load classes and their

**TABLE 1 SUMMARY OF NONDESTRUCTIVE TESTING EQUIPMENT AND  
PERTINENT CHARACTERISTICS**

<b>Category</b>	<b>Load Class</b>	<b>Device</b>	<b>Deflection Measurement Made</b>
<b>1</b>	<b>Static</b>	Plate (19) <sup>a</sup>	Magnitude
		Plate (20)	Magnitude
<b>2</b>	<b>Impact</b>	Washington State (58)	Magnitude
		Paris (58)	Magnitude
		German (58)	Magnitude
<b>3</b>	<b>Vibratory</b>	Shell (23)	Wave Length
		Road Rater (25)	Magnitude
		Dynaflect (23)	Magnitude
		Corp of Engr. (25)	Magnitude
		AFCEL (68)	Wave Length
<b>4</b>	<b>Vehicular</b>	Benkleman (69)	Magnitude
		California (55)	Magnitude
		Lacroix (70)	Magnitude
		TRRL (71)	Magnitude
		South Africa (23)	Curvature

<sup>a</sup>Numbers refer to references

characteristics, devices being developed and in use, and the particular aspect of the surface disturbance that is measured.

In the static load class repetitive or non-repetitive loads are applied to plates of varying sizes on the surface of the pavement. In the impact load class, weights are allowed to free-fall and impact a plate on the pavement surface. The weights may range in size from 20 lbs (Reference 23) to 500 lbs, as was used by Isaada (Reference 24). The vibratory procedures also show a considerable range in magnitude of vibratory loads and frequency of vibration. Peak vibratory loads may range from 0.75 to 25 kips and frequencies may range from 1 to 5000 hertz. Green and Hall (Reference 25) conducted a thorough study of vibratory equipment. Their work and the references cited in Table 1 provide additional details. Of the devices that use vehicular loads, the Benkleman beam measures rebound deflection, and the LaCroix and California deflectometer are somewhat automated Benkleman beams. The TRRL device employs an optical (non contact) displacement transducer for measuring deflections, and the South African apparatus measures curvature of the pavement as the wheel approaches.

## 2.2 Analysis

Numerous analytical solutions exist, employing various models, representing a pavement-subgrade system. These models are based on the theories of elasticity and viscoelasticity. Numerous equations representing their behavior under static and dynamic loading have also been solved (References 26 through 40). In 1972, Boyer (Reference 11) presented a rather definitive review of these solutions. In

addition, he employed the concept of transfer function theory along with the results of full scale field testing, using gages installed in the pavement. He proposed an "a posteriori" modelling concept to develop transfer functions and predict pavement response. Highter (Reference 13) reviewed the use of energy concepts and methods, and failure criteria relative to pavement evaluation. Using energy concepts he was able to substantiate that "a functional relationship exists between cumulative energy as measured by cumulative peak deflections imparted to a given pavement system and the condition of the system". Three sources of data were studied to verify his hypothesis. AASHO Road Test data, the Air Force base traffic records from Pease and Castle Air Force Bases, and data from field testing of overlays specifically constructed for his investigation.

A theoretical study of dynamic stiffness and its application to vibratory nondestructive testing of pavements was conducted by Weiss (Reference 41) in conjunction with the study by Green and Hall (Reference 25). Weiss developed a nonlinear vibration theory for pavements and gave a method of obtaining the shear modulus and thickness of each pavement layer. In this work a vibrator is used to generate the deflections from which the dynamic stiffness is calculated.

Wiseman (Reference 42) used the Hogg and the Hertz models to estimate pavement characteristics. The Hogg model provided the required pavement stiffness for full-depth asphalt airfield pavements. He then related the computed stiffness to projected traffic and a characteristic length using published Asphalt Institute procedures.



Wiseman also used the Hertz model to compute the single wheel load on a rigid pavement as a function of measured stiffness.

A probabilistic analysis of the response of pavement structures was undertaken by McCullough (Reference 17). He cited the application of stochastic process, in this regard by the Texas Highway Department (Reference 43), California Division of Highways (Reference 44) and the Asphalt Institute (Reference 45). He also illustrated the application of the Markov process and its theoretical relation to states of a pavement. Reliability techniques have also been reported by Darter and Hudson (Reference 46). In 1976, Moavenzadeh (Reference 47) presented a stochastic simulation model for predicting pavement performance. Recognizing the limitations of his model, he concluded that it can be used to compare various design alternatives. It also accounts for geometry, load area and intensity, random inter-arrival times, statistical variation in material properties and temperature histories.

Inherent in all analytical and stochastic models is the notion that parameters can be obtained that reflect the actual vehicular load experienced by a pavement subgrade system. At the present time, the literature shows that parameters used in analysis are obtained by static field test, laboratory testing, vibrations, impact and measurement of pavement rebound characteristics. The actual time dependent response of the pavement-subgrade system subject to one complete vehicular pass is not considered.

### SECTION III

#### THEORY AND METHODOLOGY

There exist today numerous elastic and viscoelastic solutions (References 26 through 40) to the overall vehicle-pavement-subgrade interaction problem, in addition to the results of several full scale field testing programs (References 48 through 50). Accumulated theory and prototype testing point to the following fundamental observations:

1. The characteristics of the component materials of a pavement-subgrade system vary locally, even within the small volume of a representative "homogeneous" sample.
2. Pavement-subgrade characteristics and response to loadings change with seasonal and ambient conditions.
3. Load repetitions affect the various components of the system differently.
4. A nondestructive field test conducted in situ using prototype loading better reflects the action of a pavement-subgrade system than destructive tests on samples, or tests conducted in situ using non-representative loads.
5. The pavement subgrade system exhibits three basic behavioral characteristics; namely,
  - (a) inertial characteristics,

- (b) elastic characteristics, i.e. linear and independent of time, and
- (c) viscoelastic characteristics that account for the memory and the time dependent nature of the system response.

Recognition of the complexity and variability of the pavement-subgrade system and the nature of the wheel loading-pavement-subgrade interaction problem, has led to the development of global methods of characterizing the pavement-subgrade system under prototype conditions of loadings (References 38, 51, and 52). The global concept provides a quantitative spatial evaluation rather than one limited to the very near vicinity of a point and the subsequent assumptions of homogeneity and isotropy in the case of the classical theories (References 11 and 12).

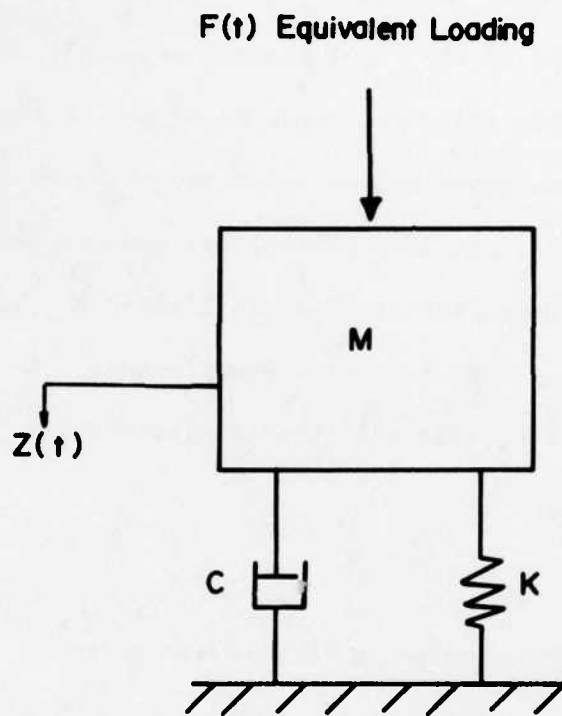
### 3.1 Hypotheses

The principal hypotheses embodied in this research are:

1. The response of a point on the surface of a pavement-subgrade system when subjected to vehicular loadings can be characterized by a (Kelvin) lumped parameter model. The three parameters of the model are  $m$ ,  $c$ , and  $k$ , as shown in Figure 1. The equation describing the hypothesized lumped parameter system is

$$m\ddot{z}(t) + c\dot{z}(t) + kz(t) = F(t) \quad (1)$$

where  $m$  represents the equivalent mass (the interacting



$$m\ddot{z}(t) + c\dot{z}(t) + kz(t) = F(t)$$

Figure 1. Kelvin Model of the Pavement Subgrade System

inertial components of the pavement-subgrade system),  $c$  is the damping (the time dependent viscoelastic or energy dissipating component), and  $k$  is the stiffness (elastic component);  $\ddot{z}(t)$ ,  $\dot{z}(t)$  and  $z(t)$  are the equivalent acceleration, velocity and deflection, respectively.  $F(t)$  is the equivalent input force due to the wheel load, (its maximum value for the F-4 aircraft, for example, is approximately 25 kips). Figure 1 shows the hypothesized model.

2. The salient characteristics of the time dependent response of the pavement-subgrade system to a complete vehicular pass can be obtained in a nondestructive manner.
3. Equivalent parameters describing the pavement-subgrade system stiffness ( $k$ ), energy dissipation ( $c$ ) and inertial ( $m$ ) characteristics can be extracted from the measured response.
4. The extracted parameters accomplish the following:
  - (a) they reflect the global structural state of the pavement-subgrade system and; whereas, they are responsive to seasonal and local variations, they can be used as the basis of a nondestructive evaluation scheme.

(b) they can be used to predict the deflection response to varying magnitudes and configurations of wheel loads.

5. Many current parameters used in conventional design and analysis can be obtained from the noted response of a pavement-subgrade system to actual vehicular loading.

The developed theory and methodology provide the following: (1) the theoretical basis of a pavement evaluation scheme. This includes the determination of the deflection response of a pavement-subgrade system to prototype loading, and the methodology of extracting parameters describing the equivalent mass, stiffness and energy dissipation characteristics of the pavement-subgrade system. (2) The methodology for predicting the deflection response of flexible pavements to prototype loadings of varying magnitudes and configurations.

### 3.2 Evaluation

The pavement evaluation scheme consists of determining the parameters inherent in the transfer function of the pavement-subgrade system. The transfer function is a mathematical expression which represents the mechanism that converts the equivalent input to an output. Figure 2 shows an overview of the input-transfer function-output interrelation as it applies to wheel load-pavement-subgrade interaction.

The basic elements of the evaluation scheme are:

(a) the signature determination, and

(b) the parameter determination.

### 3.2.1 Signature Determination

The signature is the pavement deflection-time plot corresponding to the pavement deflection at the outer edge of the tire print as shown in Figure 3. Because the mechanical setup of the measuring equipment precludes the measurement of deflections closer than 3 inches from the outer edge of the tire print, the signature is calculated from deflections measured in the field using the "stationary beam-moving load" procedure.

In this procedure (Figures 3 and 4) a cantilever beam with its pivot outside the deflection basin supports sensing elements within the deflection basin. The sensing elements measure relative motion between the pavement surface and the beam as the load vehicle travels in a direction perpendicular to the beam position. The sensing elements are positioned at different lateral distances from the load wheel and therefore record the deflection time history for one complete pass of the load vehicle at the points of measurement. The location of the tire print is determined from the impression the tire makes on silver adhesive tape placed on the pavement in its path in front of the beam. The distance from the outer edge of the tire print to the first gage is measured. From this initial measurement and the fixed intergage distances, the distance of each gage from the outer edge of the tire print is calculated [Figure 3(b)]. Figure 4 shows an Air Force P-2 fire truck about to make a pass by two stationary measurement systems.

The method of calculating the signature is as follows:



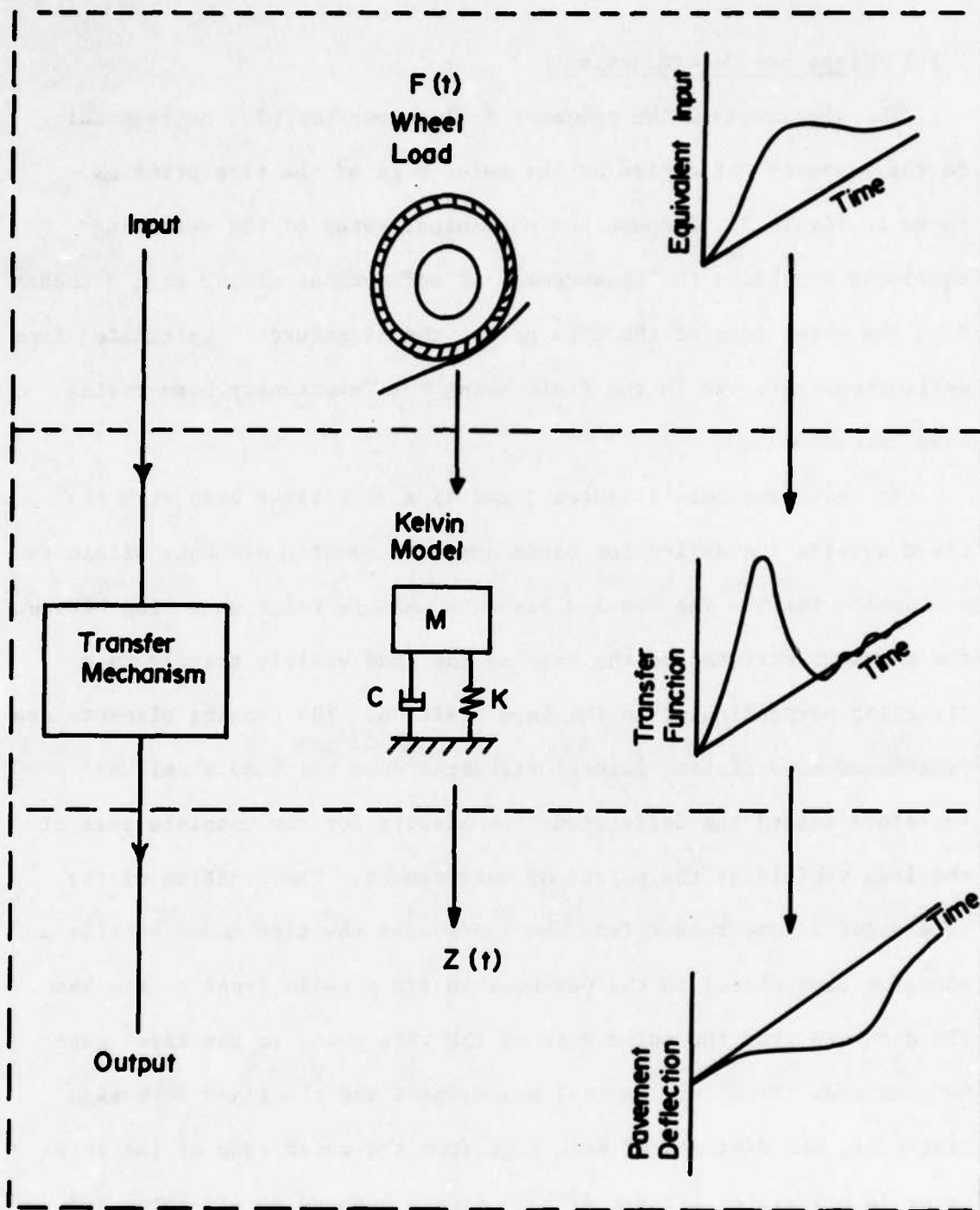
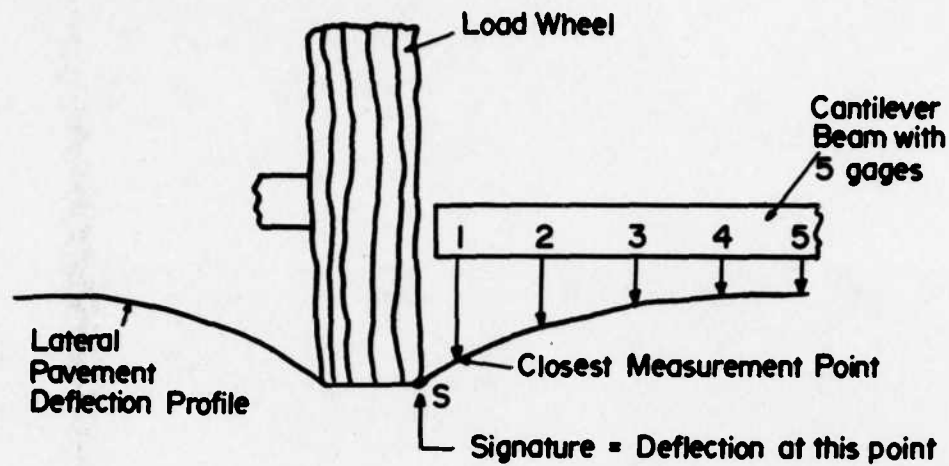
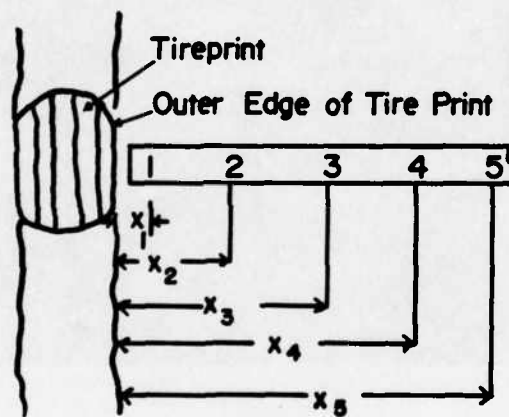


Figure 2. An Overview of the Transfer Function Concept as Applied to Wheel-Pavement Subgrade Interaction

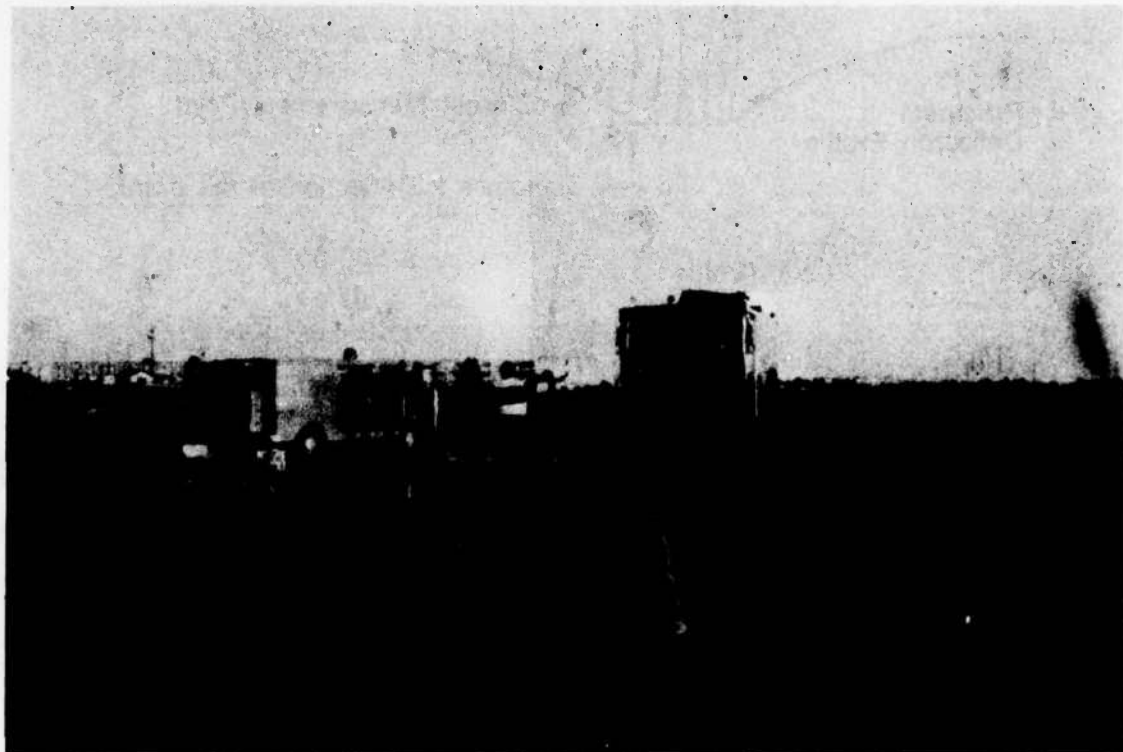


(a) Profile



(b) Plan View

**Figure 3. Location of Signature and Relative Gage Location and Setup**



**Figure 4. Setup During Stationary Beam-Moving Load Operation -  
P-2 Fire Truck**

- (a) The maximum value of the deflection,  $z_{\max}$ , at each particular gage (j) is obtained from each of the deflection-time plots recorded at said gage (j) during one pass of the vehicle. V and W of Figure 5 show  $z_{\max_1}$  and  $z_{\max_2}$  ( $z_{\max_3}$ ,  $z_{\max_4}$  and  $z_{\max_5}$  are not shown), in perspective.
- (b) The distances  $x_j$  [Figure 3(b)] from the outer edge of the tire print to each gage as recorded in the field, and the corresponding maximum gage readings,  $z_{\max_j}$ , are then fitted with a curve given by the equation

$$z_{\max_j} = A_{\text{peak}} \exp (\beta_{\text{peak}} x_j^{r_{\text{peak}}}) \quad (2)$$

where  $A_{\text{peak}}$ ,  $\beta_{\text{peak}}$  and  $r_{\text{peak}}$  are parameters describing the attenuation of the maximum values of the deflection-time plots recorded on each gage. Equation (2) is similar in form to those used by Boyer (Reference 11) and Highter (Reference 12), but has three parameters,  $A_{\text{peak}}$ ,  $\beta_{\text{peak}}$  and  $r_{\text{peak}}$ , instead of two that they used. Baladi (Reference 52) also uses a three-parameter equation to describe the attenuation of the maximum lateral deflection profile caused by vehicular loads on highways.

The curve fitting calculations are performed by the computer subroutine EXACFIT listed in Appendix C. The equations used are derived as follows:

Given the general equation of the curve in the form

$$z = A \exp (\beta x^r) \quad (2a)$$

This equation has three unknowns,  $A$ ,  $\beta$  and  $r$ . Using this basic equation and values of  $(x_1, z_{\max_1})$ ,  $(x_2, z_{\max_2})$  and  $(x_3, z_{\max_3})$ , (where the numbers in the subscripts refer to gages numbered from 1, the closest to the wheel, to 5 the farthestmost from the wheel), the following are had:

$$z_{\max_1} = A'_{\text{peak}} \exp (\beta'_{\text{peak}} x_1^{r'_{\text{peak}}}) \quad (3a)$$

$$z_{\max_2} = A'_{\text{peak}} \exp (\beta'_{\text{peak}} x_2^{r'_{\text{peak}}}) \quad (3b)$$

$$z_{\max_3} = A'_{\text{peak}} \exp (\beta'_{\text{peak}} x_3^{r'_{\text{peak}}}) \quad (3c)$$

Dividing equation (3a) by equation (3b) gives

$$z_{\max_1} / z_{\max_2} = \exp (\beta'_{\text{peak}} x_1^{r'_{\text{peak}}} - \beta'_{\text{peak}} x_2^{r'_{\text{peak}}})$$

Taking the natural logarithm of both sides produces

$$\ln z_{\max_1} - \ln z_{\max_2} = \beta'_{\text{peak}} (x_1^{r'_{\text{peak}}} - x_2^{r'_{\text{peak}}}) \quad (4)$$

Similarly from equation (3a) and (3c)

$$\ln z_{\max_1} - \ln z_{\max_3} = \beta'_{\text{peak}} (x_1^{r'_{\text{peak}}} - x_3^{r'_{\text{peak}}}) \quad (5)$$

Dividing equation (4) by equation (5) and rearranging terms gives

$$(x_1^{r'_{\text{peak}}} - x_3^{r'_{\text{peak}}}) \left( \frac{\ln z_{\text{max}_1} - \ln z_{\text{max}_2}}{\ln z_{\text{max}_1} - \ln z_{\text{max}_3}} \right) = x_1^{r'_{\text{peak}}} - x_2^{r'_{\text{peak}}} \quad (6a)$$

Equation (6a) is solved by an iteration-interpolation procedure detailed in Appendix C, and  $r'_{\text{peak}}$  is found.

$\beta'_{\text{peak}}$  is then calculated using equation (5), where

$$\beta'_{\text{peak}} = \frac{\ln z_{\text{max}_1} - \ln z_{\text{max}_3}}{x_1^{r'_{\text{peak}}} - x_3^{r'_{\text{peak}}}} \quad (5a)$$

Then  $A'_{\text{peak}}$  is calculated using equation (3a) where

$$A'_{\text{peak}} = z_{\text{max}_1} / \exp(\beta'_{\text{peak}} x_1^{r'_{\text{peak}}}) \quad (3a)$$

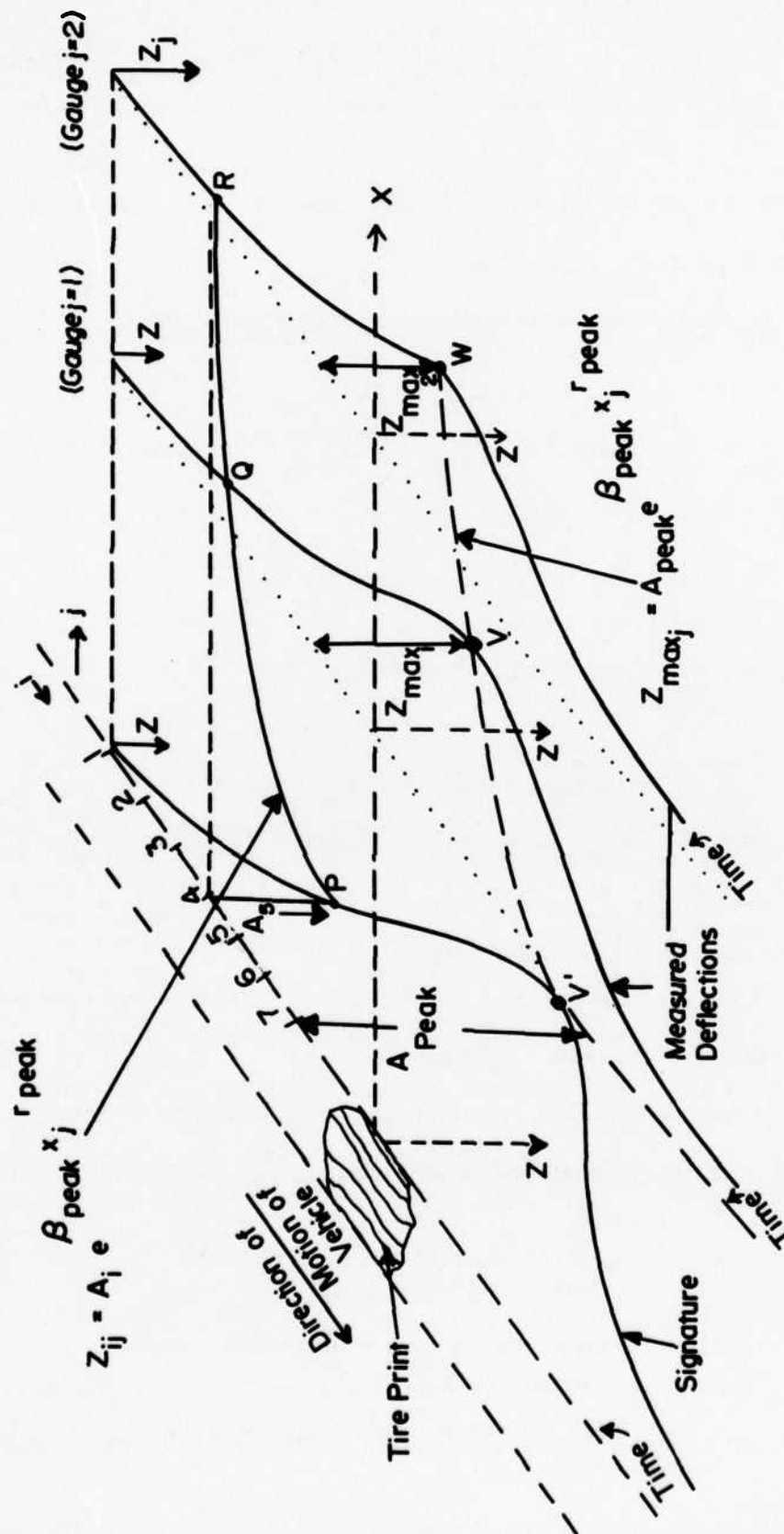
Using  $(x_1, z_{\text{max}_1})$ ,  $(x_3, z_{\text{max}_3})$  and  $(x_5, z_{\text{max}_5})$  instead of  $(x_1, z_{\text{max}_1})$ ,  $(x_2, z_{\text{max}_2})$  and  $(x_3, z_{\text{max}_3})$ , equations (3a), (3b) and (3c) are again solved to find  $r''_{\text{peak}}$ ,  $\beta''_{\text{peak}}$  and  $A''_{\text{peak}}$ . The desired  $r_{\text{peak}}$ ,  $\beta_{\text{peak}}$  and  $A_{\text{peak}}$  are found using the equations

$$r_{\text{peak}} = (r'_{\text{peak}} + r''_{\text{peak}}) / 2 \quad (7)$$

$$\beta_{\text{peak}} = (\beta'_{\text{peak}} + \beta''_{\text{peak}}) / 2 \quad (8)$$

$$A_{\text{peak}} = (A'_{\text{peak}} + A''_{\text{peak}}) / 2 \quad (9)$$

$r_{\text{peak}}$ ,  $\beta_{\text{peak}}$  and  $A_{\text{peak}}$  are the parameters which describe the maximum lateral deflection profile, partly shown in Figure 5 as the curve V'VW.



(c) The signature is calculated using the  $r_{\text{peak}}$  and  $\beta_{\text{peak}}$  parameters and the basic equation, equation (2a), in the form

$$A(t) = z_1(t) / \exp(\beta_{\text{peak}} \times r_{\text{peak}}) \quad (10)$$

where  $z_1(t)$  refers to the deflection at gage 1 (closest to the wheel), and  $t$  is the time shown discretized as 1 in Figure 5. Subroutine SIGNTR in Appendix C performs these computations.

The signature thus calculated is the pavement deflection due to prototype loading at point S in Figure 3. Using this signature as the output (Figure 2), parameters  $k$ ,  $c$ , and  $m$  describing the transfer mechanism of the three-parameter model of the pavement-subgrade system, are calculated.

### 3.2.2 Parameter Determination

The objective of the theoretical procedure is to determine the equivalent  $m$ ,  $c$  and  $k$  parameters of a pavement-subgrade from the signature obtained from actual field loadings using transfer function theory. These parameters define the transfer mechanism that converts wheel loadings to pavement deflections.

The wheel load-pavement-subgrade interaction, as shown in Figure 2, can be represented mathematically by the equation (1):

$$m\ddot{z}(t) + c\dot{z}(t) + kz(t) = F(t) \quad (1)$$

It can also be represented by the equation

$$I(t) * G(t) = \frac{F(t)}{m} * G(t) = z(t) \quad (11)$$



where  $F(t)$  is the equivalent loading (input) function,  $m$  is the equivalent mass,  $G(t)$  is the reduced transfer function,  $z(t)$  is the response and the symbol  $(*)$  represents the mathematical operation of convolution (Reference 53). In its integral form equation (11) becomes

$$z(t) = \int_0^t \frac{F(\tau)}{m} \cdot G(t-\tau) d\tau \quad (12)$$

$G(t)$ , the reduced transfer function in equations (11) and (12) is obtained from equation (1) as follows:

Consider the basic equation of the model:

$$m\ddot{z}(t) + c\dot{z}(t) + kz(t) = F(t) \quad (1)$$

taking the Laplace transform of both sides, imposing initial conditions (pavement is assumed to be at rest prior to loading) of  $z(0) = \dot{z}(0) = 0$ , and transposing terms, yields:

$$\bar{z}(s) = \frac{\bar{f}(s)}{m} \cdot \left( \frac{1}{s^2 + \frac{c}{m}s + \frac{k}{m}} \right)$$

where the bars denote the transformed function. The reduced transfer function is defined as

$$\bar{G}(s) = \frac{1}{s^2 + \frac{c}{m}s + \frac{k}{m}}$$

Inverting  $\bar{G}(s)$  gives,

$$G(t) = \begin{bmatrix} \frac{1}{\frac{k}{m} - \frac{c^2}{4m^2}} e^{-\frac{c}{2m} \cdot t} \\ \frac{k}{m} - \frac{c^2}{4m^2} \end{bmatrix} \begin{bmatrix} \sin \frac{k}{m} - \frac{c^2}{4m^2} t \\ \end{bmatrix} \quad (13a)$$

if  $k/m < \frac{c^2}{4m^2}$ , namely, the system is overdamped, then

$$G(t) = \begin{bmatrix} \frac{1}{\frac{c^2}{4m^2} - \frac{k}{m}} e^{-\frac{c}{2m} \cdot t} \\ \frac{c^2}{4m^2} - \frac{k}{m} \end{bmatrix} \begin{bmatrix} \sinh \frac{c^2}{4m^2} - \frac{k}{m} t \\ \end{bmatrix} \quad (13b)$$

Two ways to obtain the equivalent input (loading function)  $F(t)$  will be pursued in this work. The first way is by the direct substitution in the equation

$$m\ddot{z}(t) + c\dot{z}(t) + kz(t) = F(t) \quad (1)$$

of the calculated values of  $\dot{z}(t)$ ,  $z(t)$  and  $z(t)$  obtained from the measured deflections, and the parameters of the transfer mechanism  $m$ ,  $c$  and  $k$ . The second method is by implicit convolution using equations (11) and (12). The implicit discrete form of equation (12) is given (Reference 53) by the equation

$$I(i) = \frac{O(i)/\Delta T - \sum_{m=1}^{k=i-1} I(m) \cdot G(k+2-m)}{I(1)} \quad (14)$$

where  $G()$  = the reduced transfer function

$O(i)$  = the output  $z(i)$

$m \times I(i) = F(i)$  = the equivalent loading function (15)

$\Delta T$  = time increment

and, the initial value of  $I(i) = I(1)$  is given by the equation

$$I(1) = \frac{O(1)}{G(1) \cdot \Delta T}$$

The same two arguments above lead to two ways of finding the output  $z(t)$ , given the forcing function and the parameters  $m$ ,  $c$ ,  $k$ . The first is by the closed form solution of equation (1). The second is by explicit convolution using the equation

$$O(i) = z(i) = \sum_{j=1}^i G(i) \cdot I(i - j + 1) \Delta T \quad (16)$$

where  $z()$ ,  $G()$ ,  $I()$  and  $\Delta T$  are as defined in equation (14).

During field testing, only the deflections with time are measured, and from these deflections the signature  $A(t)$  in equation (10) can be obtained as discussed previously. How then are the parameters of transfer function and the loading functions determined?

In concept, the methodology used is as follows: The signature  $A(t)$  is taken to be equivalent to the response  $z(t)$  in equations (11) to (16) as discussed in the previous section entitled "Signature Determination". The input function  $F(t)$  is now known initially. It is assumed however that the maximum value of  $F(t)$  is the wheel load, or approximately 25 kips (Reference 54) for the F-4 aircraft, which is the main vehicle of interest in the present study. Using the signature  $z(t)$ , the maximum assumed value (25 kips) of the equivalent input, and the equations developed previously in this section, the  $k$ ,  $c$ , and  $m$  parameters of the pavement-subgrade system are determined.

The detailed procedure for finding  $k$ ,  $c$ , and  $m$  is as follows:

- (1) The signature is differentiated numerically to yield the time history of the velocity  $\dot{z}(t)$  and the acceleration  $\ddot{z}(t)$ . Typical plots of  $\dot{z}(t)$ ,  $\ddot{z}(t)$ , and  $z(t)$  are shown in Figure 6.
- (2) The components of the equivalent force, due to each of the three parameters, on the left hand side of the basic equation (1), are then considered for three special conditions, labelled as sections (1), (2), and (3) in Figure 7.

At section (1), the point of inflection of the signature, the following equations hold:

$$\ddot{z}(t_1) = 0$$

$$m\ddot{z}(t_1) = 0$$

hence,

$$c\dot{z}(t_1) + k z(t_1) = F(t_1) \quad (17a)$$

At section (3), the maximum deflection response, the following equations hold:

$$\dot{z}(t_3) = 0$$

$$c\dot{z}(t_3) = 0$$

hence,

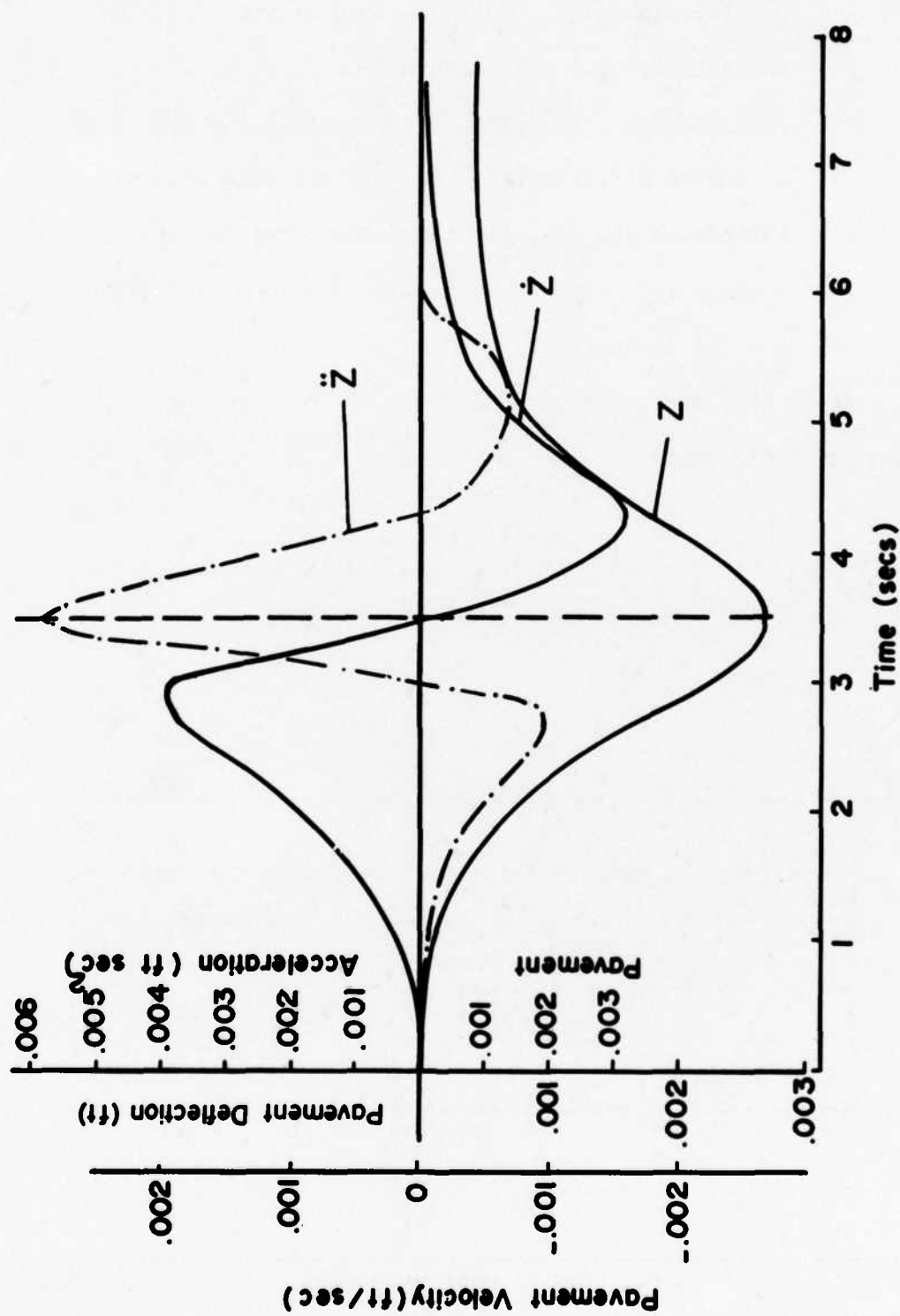


Figure 6. Zero, First and Second Derivatives of the Measured Displacement Function (Typical)

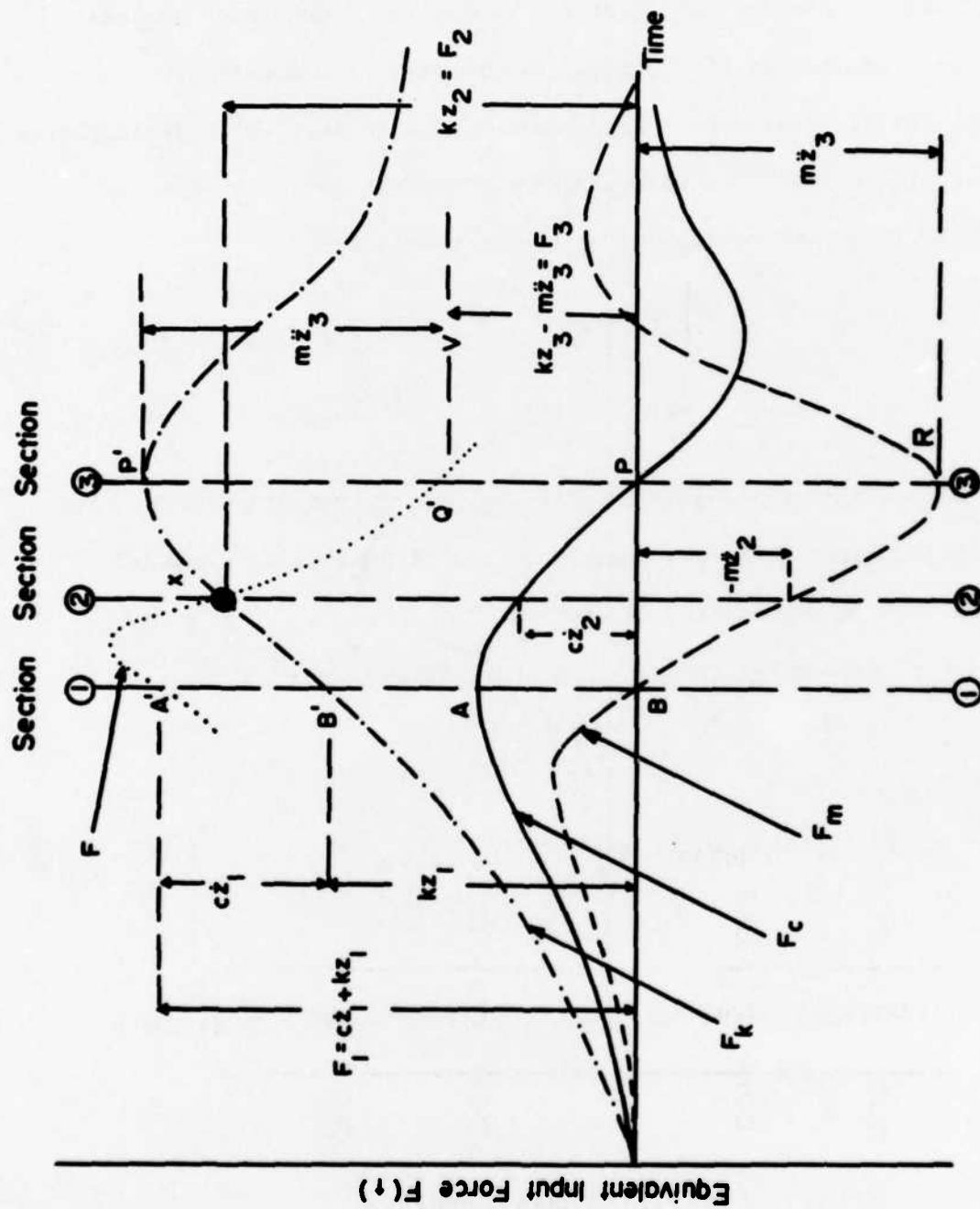


Figure 7. Determination of Parameters of Transfer Function - A Graphical Overview of Methodology

$$m\ddot{z}(t_3) + kz(t_3) = F(t_3) \quad (17)$$

The third special condition occurs, for each deflection data set, at a time between the time corresponding to the point of inflection [section (1)] and the maximum deflection [section (3)]. With reference to Figure 7, with increasing times from section (1) to section (3), the stiffness component  $[kz(t)]$  of the equivalent input force increases from  $B'$  to a maximum at  $P'$ . During this passage, the damping component  $[cz(t)]$  decreases from a maximum of  $A$  to zero ( $P$ ). Similarly, the inertial component  $[mz(t)]$  decreases from zero ( $B$ ) to a negative value of  $R$ . The time corresponding to the conditions,

$$c\dot{z}(t_2) = -m\ddot{z}(t_2) \quad (18)$$

$$\text{and, hence, } kz(t_2) = F(t_2) \quad (19)$$

will be called the crossing point. It provides the final special condition for determining the measure of the parameters  $m$ ,  $c$  and  $k$ . This condition is represented as section (2) of Figure 7. It should be noted that between section (1) and the crossing point,

$$kz(t) \leq F(t_2)$$

and between the crossing point and section (3)

$$kz(t) > F(t_2)$$

In concept, therefore, the crossing point represents the time at which the Winkler hypothesis (Reference 55) is satisfied.

(3) Using the equation in paragraph (2) and the developed method, an iterative procedure, given in detail in Appendix C was used to determine the  $k$ ,  $c$  and  $m$  parameters in this study. Briefly the procedure is as follows:

The signature of the load vehicle is obtained as described in the section entitled "Signature Determination". A first trial value of  $k$  is taken as a fraction ( $AA1 < 1.0$ )<sup>1</sup> of the wheel load (25 kips) divided by the maximum value of the signature. Then it is assumed that another fraction ( $AA2 < 1$ ) of the wheel load acts at the time corresponding to section (3) Figure 7. The first trial value of  $m$  is calculated for the conditions at section (3) using equation (17). The initial trial value of the  $c$  parameters is then computed using equation (18) at the first estimated crossing point in the data set, i.e., at the first discrete interval of time after section (1). Using these first estimates of  $k$ ,  $c$  and  $m$  the transfer function  $G(t)$  [equation (13)] is had [EXACT 1]<sup>1</sup>. Next the loading function  $F(t)$  is obtained by implicit convolution [equations (14) and (15) and NWCONV] in the time domain using the signature deflection  $z(t)$  is output and  $G(t)$ . The maximum value of  $F(t)$  is then found. A check is made to see if this (maximum) value of  $F(t)$  satisfies the necessary (500 pound) criterion that,

---

<sup>1</sup>Capital letters in parentheses refer to computer programs or symbols used in computer programs in Appendix C.



$$24,500 \text{ lb} \leq F(t) \text{ maximum} < 25,500 \text{ lb}$$

(20)

If this criterion is not satisfied, the next crossing point is selected,  $c$  is recalculated and the same procedure is followed to obtain the maximum value of  $F(t)$ , which is again examined with respect to the previously stated criterion. This process is repeated until the possible crossing points are exhausted i.e. section (3) Figure 7 is reached, or the maximum value  $F(t)$  satisfies the previously stated criterion, whichever occurs first.

If all possible crossing point times are exhausted a new value of  $m$  is calculated by incrementing the value of  $AA2$ . Using the first trial value of  $k$  and the second trial value of  $m$  a new  $c$  is calculated for the first estimated crossing point. The procedure is repeated, checking the maximum value of  $F(t)$  against the 500 pound criterion. If this criterion is not satisfied the sequence of crossing points is again stepped through. If these are exhausted a next trial value of  $m$  is assumed and the entire process is repeated. If the incremented value of  $AA2$  reaches unity, a second trial value of  $k$  is calculated by incrementing  $AA1$ , and the entire procedure, including a new sequence of  $m$  and  $c$  values, is examined at all possible crossing points. This process is repeated until the 500 pound criterion (equation 20) is satisfied.

If the 500 pound criterion is satisfied, a new  $c$  value is calculated for conditions corresponding to the time at the inflection point of the signature (section (1), Figure 7, equation 17a); using the current  $k$  value and the force obtained by convolution, corresponding to the time of inflection. If this new  $c$  value does not correspond to the

c value which satisfied conditions at the crossing point and the 500 pound criterion, the iteration process is continued by selecting another crossing point and repeating the entire procedure. If the c values do correspond then the corresponding k, c, and m values are the desired parameters.

### 3.3 Prediction of Pavement Response (Signature)

The theory and methodology for signature and parameter determination developed in the previous sections were used to predict the signature of a vehicle (vehicle A) at a site prior to the actual passage of the vehicle at that location. This was done by first obtaining signatures of both a standard vehicle and vehicle A at another site, and the signature of the standard vehicle at the new site. This is accomplished by using an equivalency function.

The equivalency function is defined as the ratio of the loading (input) function of a vehicle,  $F_1(t)$ , and the loading function of the standard vehicle,  $F_2(t)$ , both obtained at the same location (at a standard site). This relationship is given by the equation.

$$\text{Equivalency Function} = EF(t) = \frac{F_1(t)}{F_2(t)} \quad (21)$$

The procedure for determining the equivalency function is as follows: with reference to Figure 8, Block I, at a standard site the signature due to a standard vehicle is obtained as discussed in the section entitled "Signature Determination". Using this signature as output, the transfer function,  $G_2(t)$ , of the standard site and the loading  $F_2(t)$  of the standard vehicle at the standard site are determined as previously discussed in the section entitled "Parameter

Determination". Next the signature of A (the vehicle whose response is to be predicted) is obtained at the standard site. Using the transfer function of the standard site as determined by the standard vehicle and the signature of vehicle A at the standard site, the loading function  $F_1(t)$  of vehicle A is obtained by implicit convolution using equation 14 and 15, and subroutine NWCONV (Appendix C). Once the equivalency function is had from equation 21, the predicted signature is obtained as follows:

First, the signature of the standard vehicle,  $z(t)$ , its loading function  $F_{sA}(t)$  and the transfer function  $G_A(t)$  are obtained at the new site as discussed in the preceding paragraph. These functions are shown schematically in Block III Figure 9. Next the loading function  $F_{1A}(t)$ , of vehicle A at the new site is calculated using the equation

$$EF(t) \times F_{sA}(t) = F_{1A}(t) \quad (22)$$

Equation 22 is represented in Figure 9 as the connection between the loading function of Block III and the equivalency function at the point labelled  $\beta$ .

The predicted signature of vehicle A at the new site is computed by the explicit convolution of the loading function of vehicle A at the new site and the transfer function of the new site as determined by the standard vehicle, using equation (16),

$$z(i) = \sum_{j=1}^i G(i) \cdot I(i - j + 1) \Delta T$$

where  $G(i)$  = transfer function of the new site

$I( )$  = the equivalent loading function of vehicle A at the new

# Standard Site

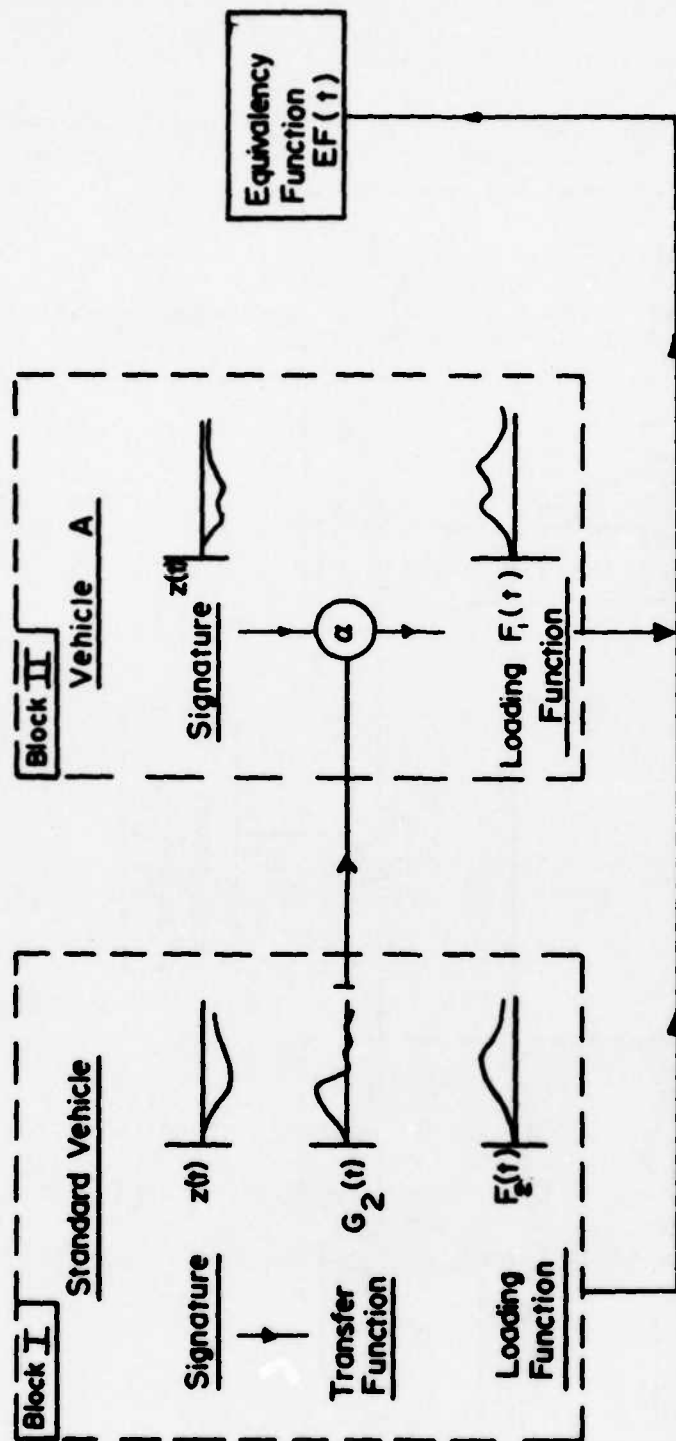


Figure 8. Overview of Scheme for Determining the Equivalency Function

New Site

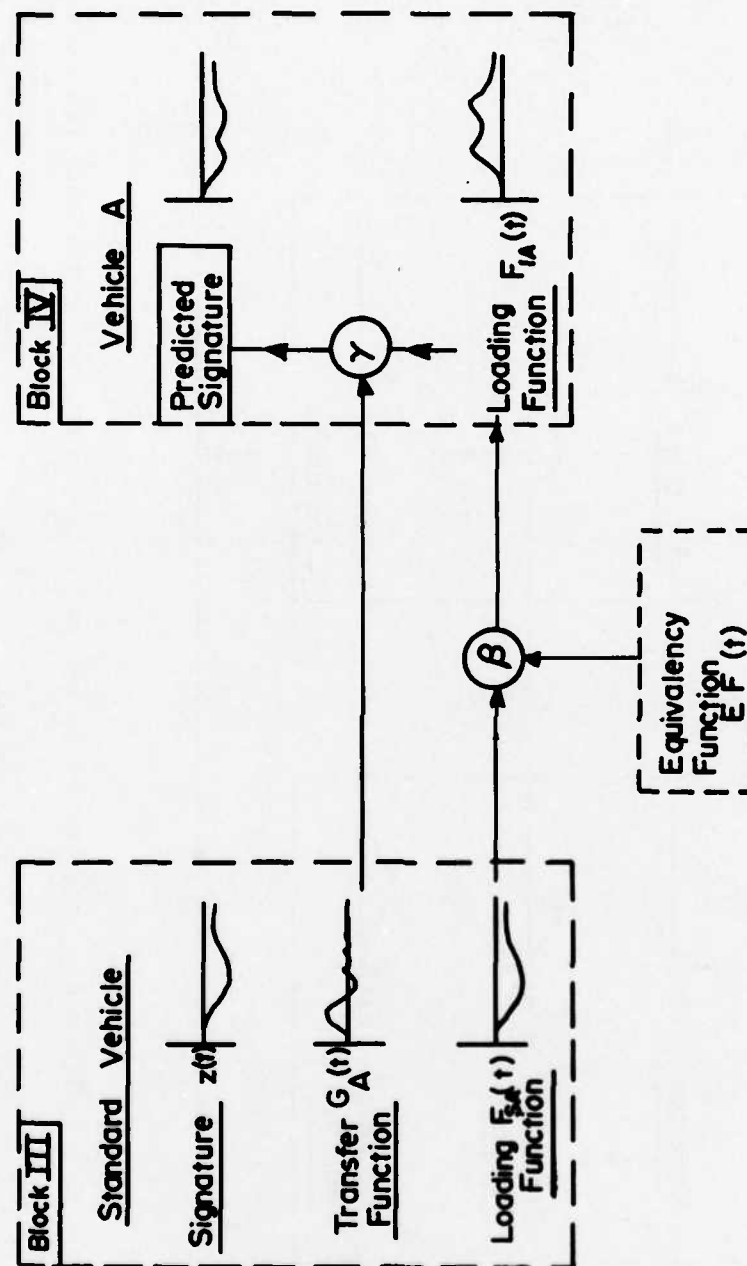


Figure 9. Overview of Scheme for Predicting the Signature

site (see equations 11 and 15)

$z(i)$  = the predicted signature

$\Delta T$  = the time increment

$j$  = dummy variable, and

$i$  = dummy variable indicating the time interval number

The explicit convolution is represented in Figure 9, Block IV as the connection between the equivalent loading and the transfer function at the point labelled  $\gamma$  of Figure 9.

The computer program PREDCT that performs the noted calculations to generate the predicted signature is given in Appendix C.

The evaluation and prediction methodologies are clearly dependent on the availability of reliable equipment for measuring pavement deflections.

## SECTION IV

### NEW INSTRUMENTATION FOR DEFLECTION MEASUREMENT

Two mobile systems were developed during this study for the measurement of pavement deflections: the Light Emitting Diode (LED) system and the Linear Variable Differential Transformer (LVDT) system.<sup>3</sup>

The LED system is essentially an optical system which does not make contact within the deflection basin of the pavement. On the other hand the sensing elements of the LVDT system make contact with the pavement surface. A summary of the research effort expended in the development of these systems and their basic developments is presented below.

#### 4.1 The LED System

The LED measurement system consists of three major operational sections: they are,

- a. the beam
- b. the sensor modules, and
- c. the recording system

##### a. The Beam

The beam is made of aluminum. Its principal function is to support the sensors above the pavement surface. It is designed so that a 20-mile-per-hour gust of wind will deflect the end of the beam less than 0.004 in. Figure 10 shows schematic details of the beam. Figure 11 shows the LED beam setup. Seven LED sensor modules are shown between the channel of the beam.

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<sup>3</sup> The LVDT system was developed by Baladi (Reference 52) as part of his research effort, sponsored by the Federal Highway Administration.

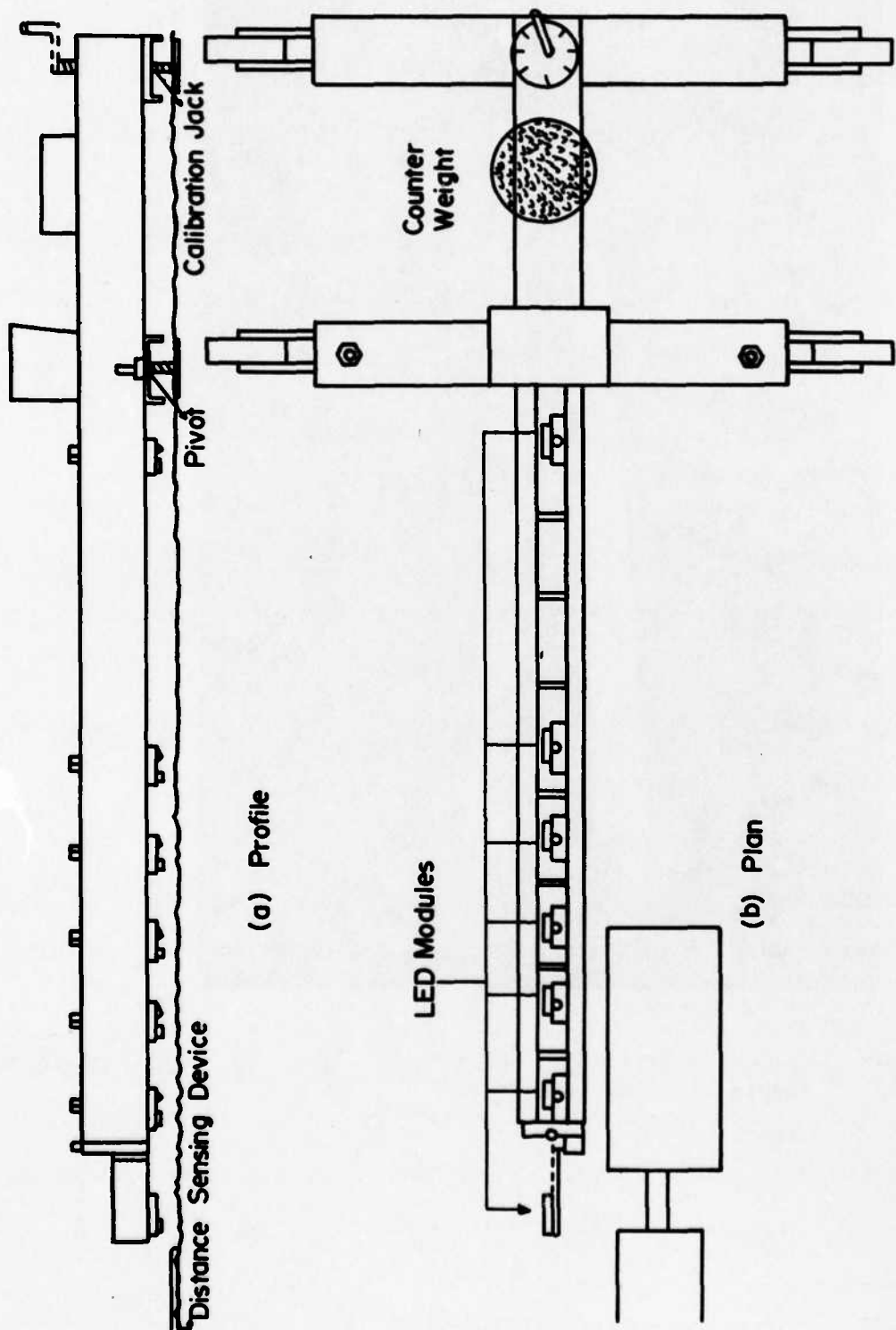
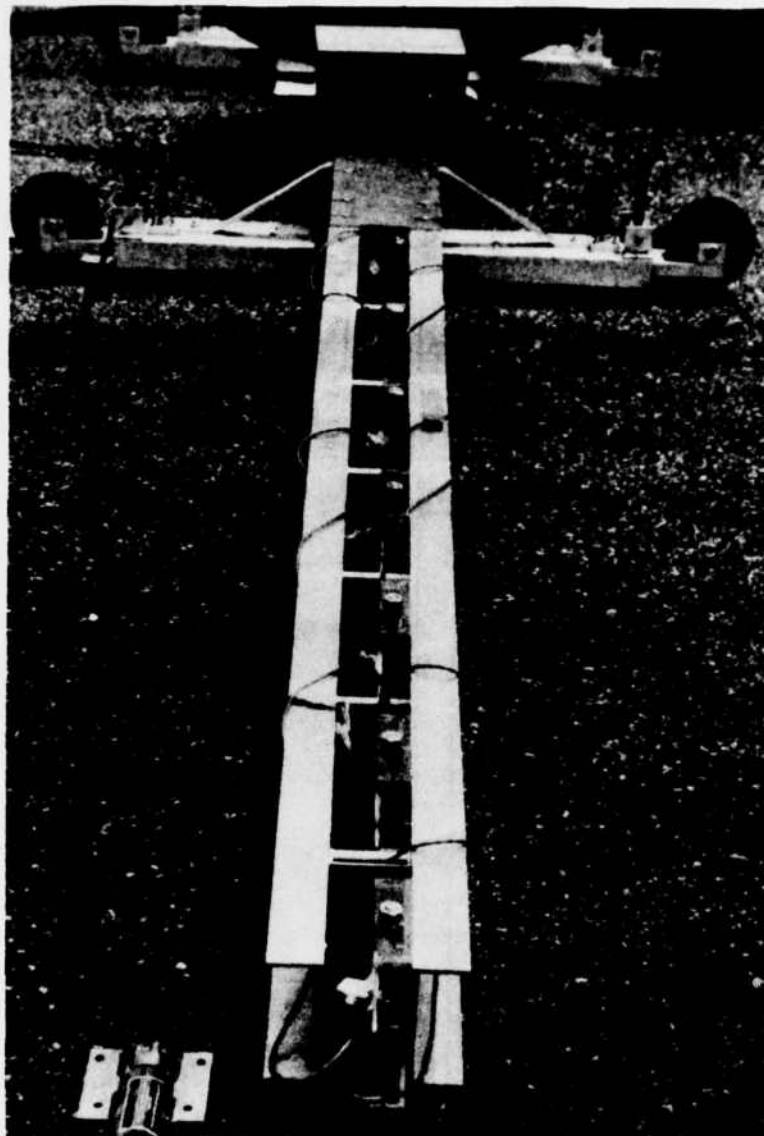


Figure 10. Light Emitting Diode (LED) Beam Schematic Details





**Figure 11. LED Beam Setup**

#### b. Sensor Modules

Several ways of obtaining deflections using optical, non-contact techniques were considered prior to selection of the final sensor. These methods can be categorized under two general classes; namely, point methods and global methods. The point methods considered were focal point displacement, beam triangulation, retro-reflector beam displacement methods, diffraction gages, interferometers, Moire gages and grating gages. The global techniques considered were holography and Moire contour techniques.

The technique selected for development was the beam triangulation method, using a light emitting diode as the coherent light source. Figure 12 shows the basic geometrical optics of the beam triangulation method. Basically, pavement deflection is measured by the amount of displacement of the reflected light impinging on the collector lens. Research has established that a line of light impinging on the surface of small chips of various materials, asphalt, concrete, and sand paper, produces a reflected signal that can be normalized to produce a linear position measurement independent of surface reflectivity. The sensors have a range of 0.2 in and an accuracy of 0.0005 in. Figure 13 shows a complete sensor module ready for mounting on the beam. Additional details are given in Appendix A.

#### c. The Recording System

Signals from the sensors are collected on a magnetic tape unit. Figure 14 shows the recorder<sup>4</sup> used during this investigation. Figure 15

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<sup>4</sup>A light beam recorder was also used in some special tests.

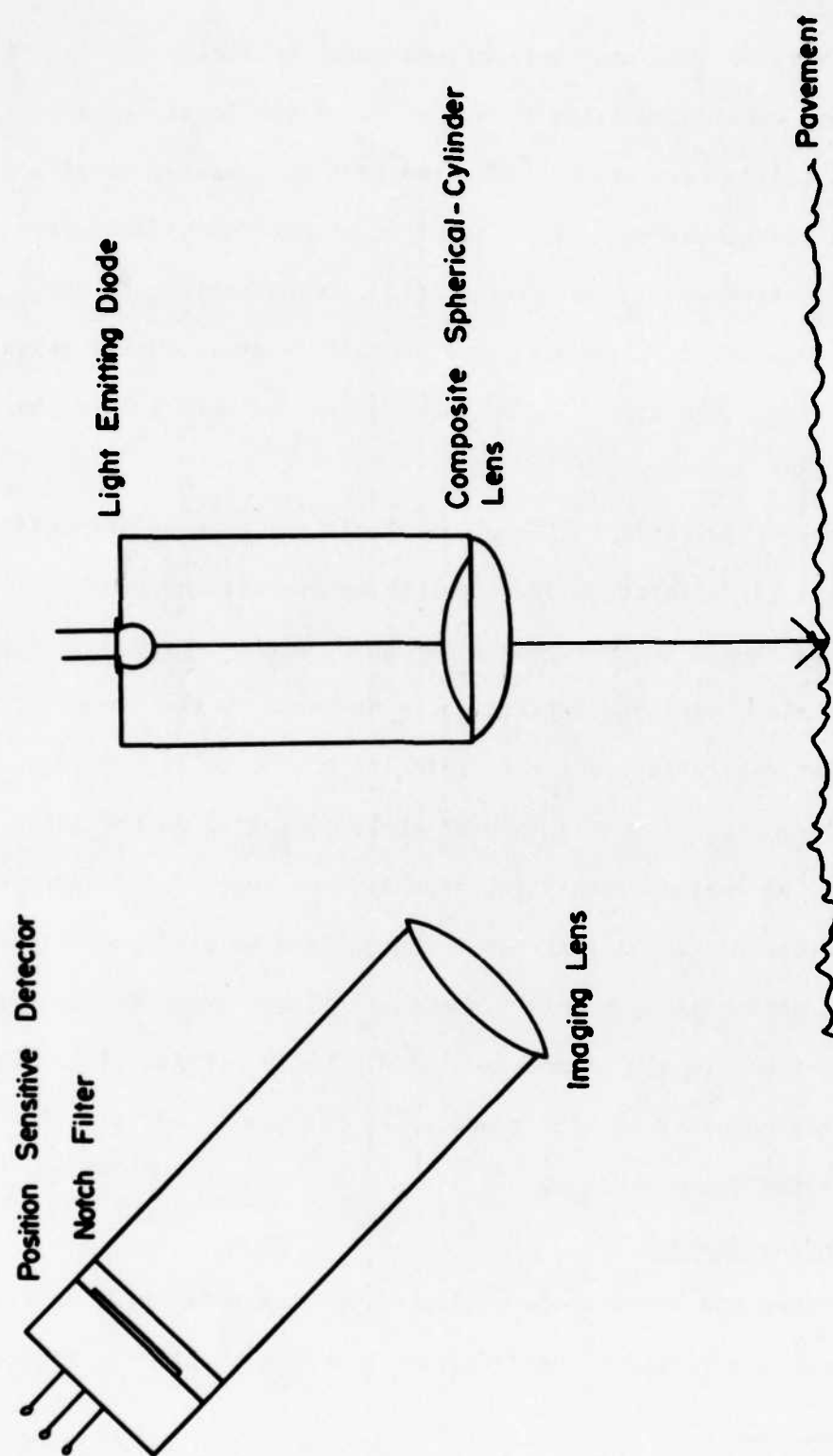
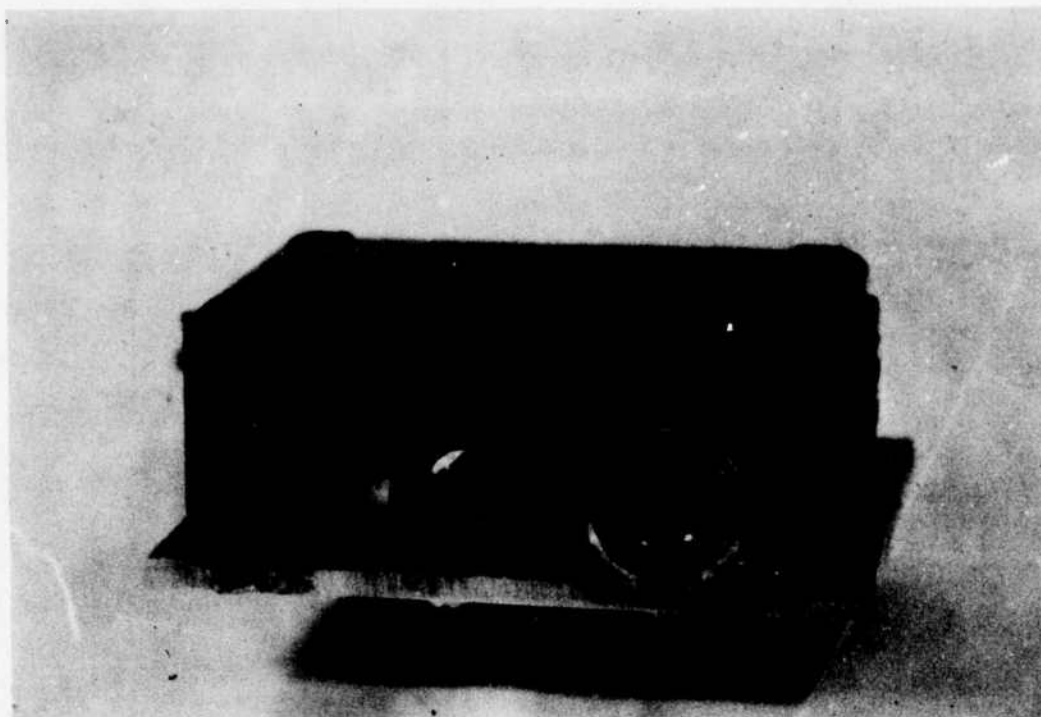
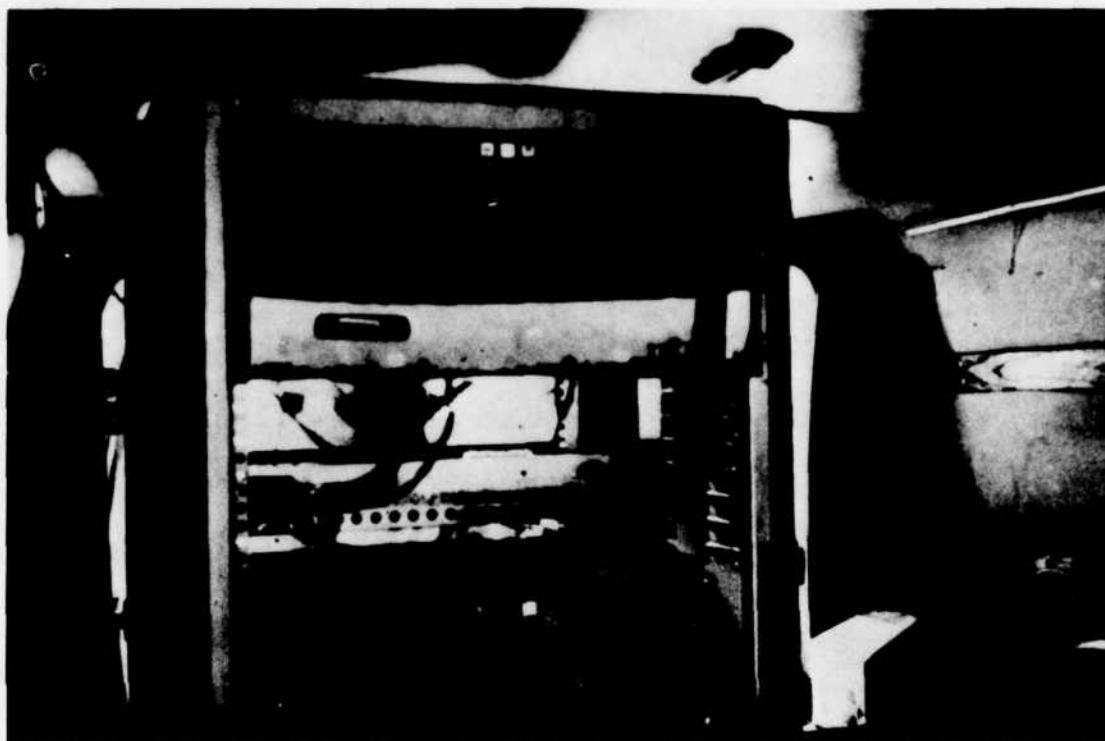


Figure 12. Light Emitting Diode Triangulation Arrangement



**Figure 13. Typical LED Sensor Module**



**Figure 14. Magnetic Tape Recording Equipment**

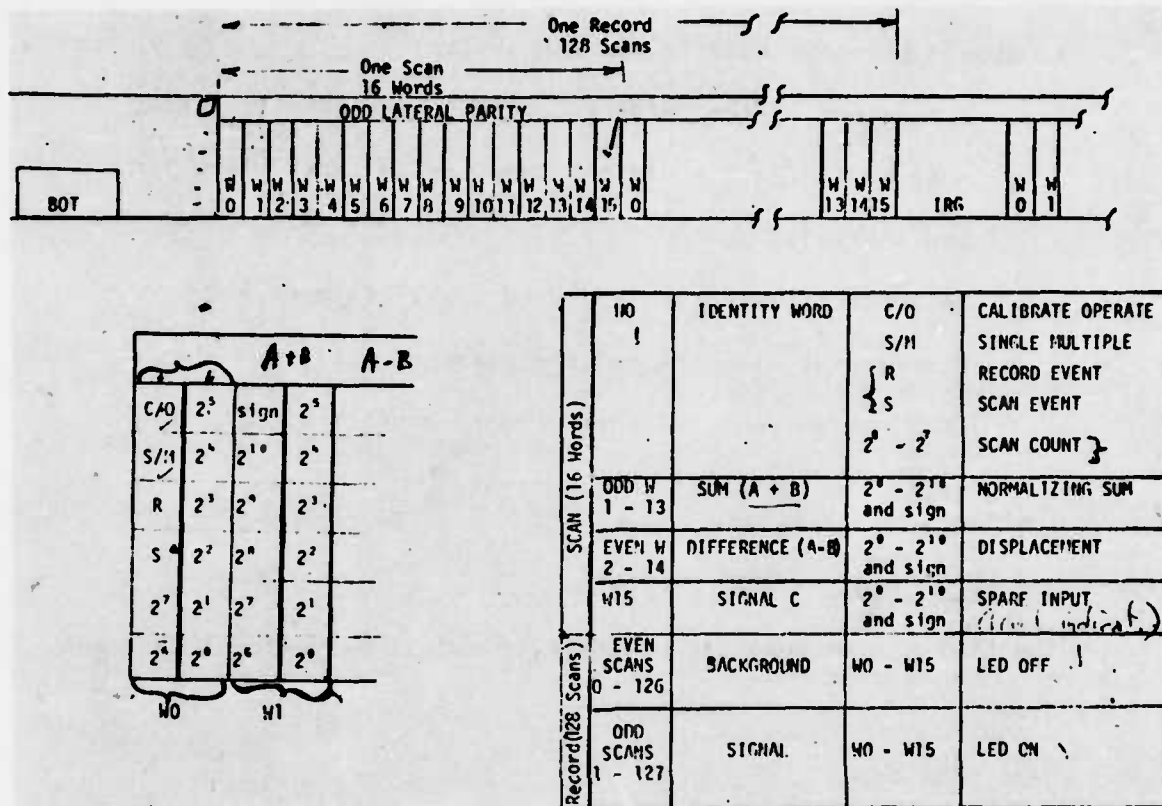


Figure 15. Arrangement of Data on Magnetic Tape (After Murphy [Reference 56])

demonstrates the basic arrangement of the data on the tape. Additional details on the tape decoding and data reduction computer programs are presented in Appendix C.

It should be noted that in the LED system:

1. The output, after being recorded on the magnetic tape, must be fed into a digital computer for data reduction and analysis, and
2. No contact (excepting infrared light) is made between the sensing elements and the pavement surface. The LVDT system required some (minor) contact within the deflection basin of the pavement.

#### 4.2 The LVDT System

The LVDT system consists of three principal operational sections.

They are:

- a. the beam
- b. the sensor elements
- c. the recording system

##### a. The Beam

The beam is a modified wide flange aluminum I-beam. Its dimensions and principal features are shown schematically in Figure 16. A picture of the beam, set up in position for measurements, is shown in Figure 17.

##### b. The Sensors

The sensors are LVDT's. These are fixed on the beam as shown in Figure 17, with the sensing elements in contact, through adjustable jacks, with the pavement surface. The relative movement between the

- ① Two Way Screw Jack
- ② 3" O.D. Pipe
- ③ Web without Flanges  
(for Counterweight)
- ④ Slots for LVDT (s)

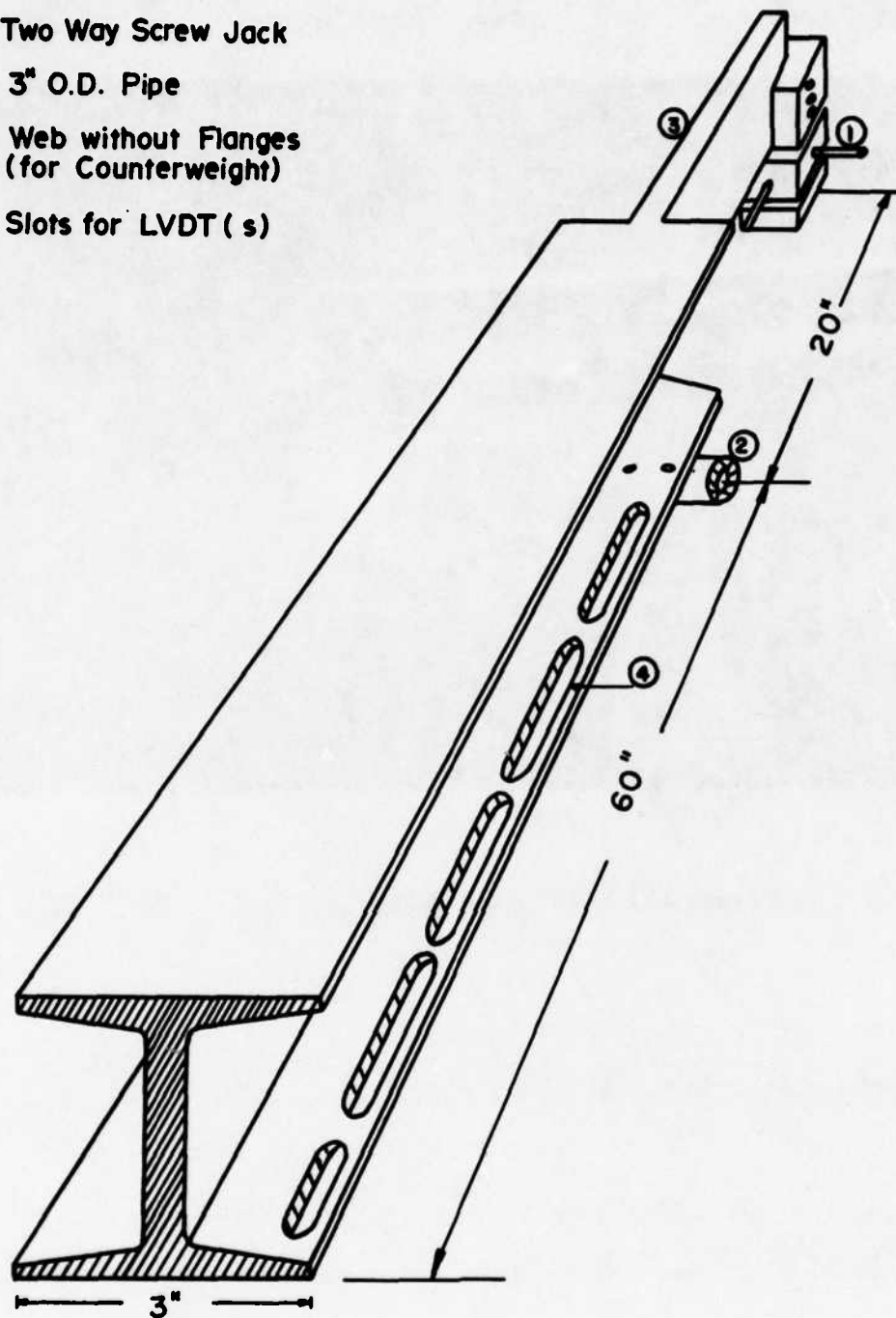
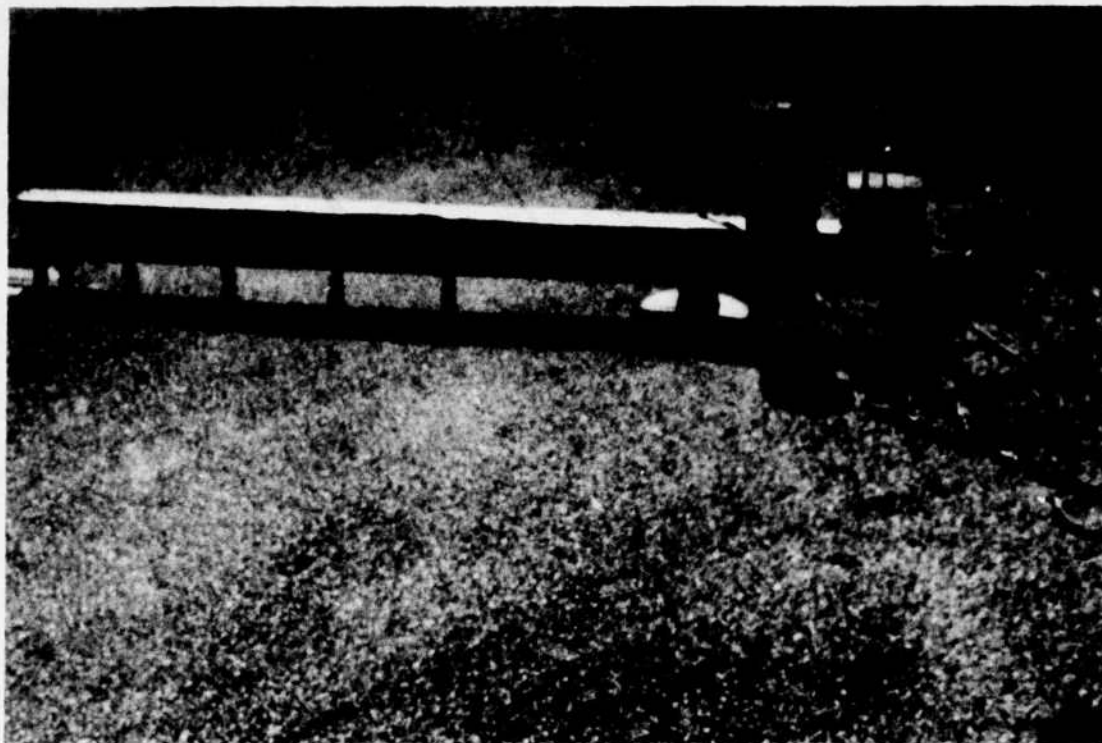


Figure 16. LVDT Beam Schematic Details





**Figure 17. LVDT Beam Setup**

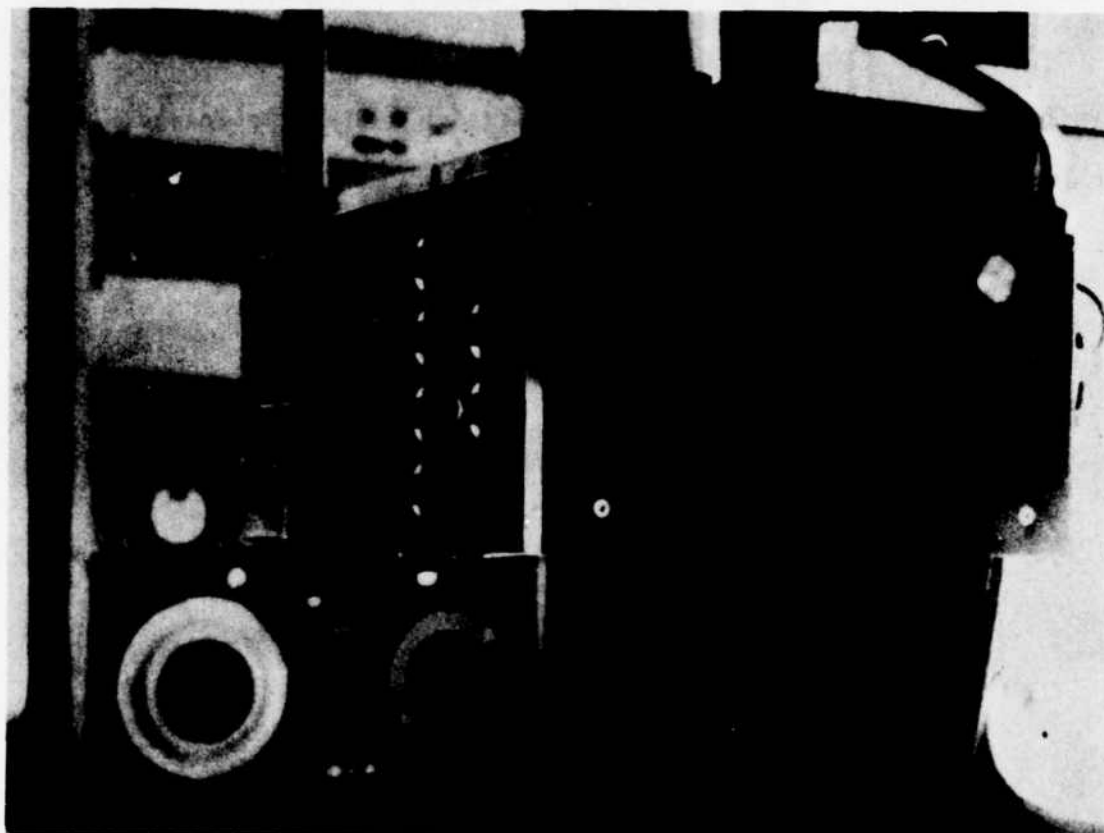
core of the sensing element and the induction coil of the LVDT, fixed on the beam, produces a signal which is a measure of the displacement.

c. The Recording System

The LVDT recording system is a six channelled light beam recorder. Figure 18 shows the recorder used in this study. An analogue signal is recorded on light sensitive paper tape. The paper tape output can be converted to digital data by using a digitizing system (Reference 57) which automatically provides punch data cards.

It should be noted that, although the LVDT system requires contact between the pavement and the sensor, its simplicity, directness of data collection and ease of operation make it very adaptable for general use.

The LVDT and the LED systems were both used at various stages of this study.



**Figure 18. Project Light Beam Recorder**

## SECTION V

### FIELD INVESTIGATIONS

The results of two series of field investigations were used in the validation of the evaluation and prediction schemes discussed previously. The first series of field investigations, Series A, was conducted during the course of this project. The second series, Series B, had been conducted in 1972 at Kirtland AFB and the basic data were reported by Boyer (Reference 11).

#### 5.1 Series A Field Investigations

The principal objectives of this series of field investigations were:

1. To verify that the new nondestructive testing equipment, i.e., LED beam (and LVDT beam), can provide measurements of pavement deflection consistent with destructive test measurements.
2. To use the NDT (nondestructive testing) equipment to obtain deflection measurements for several different vehicles at different sites, for the purposes of providing initial input into the evaluation scheme developed in conjunction with the NDT equipment.
3. To show that the evaluation and prediction schemes are consistent with the factual information currently available.

The methodology evolved over the period of this study therefore reflects the need to satisfy the principal objectives.

The basic methodology with respect to equipment development, shown in Table 2, evolved over the period of this study. As can be seen from

TABLE 2. FIELD TESTING METHODOLOGY OF DEVELOPMENT

Stage	Method of Measuring Deflections	Features of Method	Distribution of Measurements
1.	Gages Installed in Pavement	(a) Destructive (b) Fixed	(a) Along one line
2.	LVDT Beam	(a) Nondestructive (b) Contact (c) Stationary	(a) Along one line and/or Global
3.	LED Beam	(a) Nondestructive (b) Noncontact (c) Stationary	(a) Along one line and/or Global
4.	LED Beam	(a) Nondestructive (b) Noncontact (c) Moving	(a) Global

Table 2 the method of measurement of deflections progressed in four steps from destructive fixed instrumentation, namely gages installed in the pavement, to noncontact, nondestructive instrumentation. Details of the gage installations, LVDT beam and the LED measurement systems are presented in Appendices A and B.

Deflection measurements were obtained during each step using different vehicles at different sites. The developed instrumentation was used as available for measurement purposes as shown in Figure 19. Figure 19 also shows a synopsis of the observed characteristics of the test sites, instrumentation and loading vehicles used in the Series A field investigation. Details of the sites and testing program conducted at each site during each phase are presented in Appendix B.

It should be recognized that the sites selected reflect reasonably well the extremes of the range of the airfield pavement conditions. Site 1 at Eglin AFB is a functionally failed flexible pavement and Site 2 is an in-service taxiway. The loading vehicles used also reflect a range of tire pressures using airfield pavements. The F-4 aircraft and the P-2 fire truck have tire pressures of 255 psi and 55 psi, respectively. The contrast in gross static wheel load also spans a reasonable range. The F-4 aircraft and the P-2 fire truck have gross single wheel<sup>5</sup> loads of approximately 25 kips and 8 kips, respectively. Figures 20 and 21 show the F-4 aircraft and the P-2 fire truck, respectively, and their pertinent characteristics. Figure 22 shows the F-4 load-cart loaded and unloaded. When loaded the central load wheel exerts a load on the pavement equivalent to a single main gear of the

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<sup>5</sup>For the F-4, this refers to the main gear.

(a) EGLIN AFB: SITE 1

<u>General Site Description:</u> Severely Cracked: used as parking area.		
Date	Loading	Instrumentation
5-75	(a) P-2 Fire truck (b) F-4 Aircraft	(a) Gages installed in pavement
11-75	(a) P-2 Fire truck (b) F-4 Aircraft	(a) Gages installed (b) LVDT Beam (c) LED Beam <sup>a</sup>
3-76	(a) F-4 Load Cart	(a) LVDT Beam

Figure 19. Synopsis of Series A Field Investigation

(b) EGLIN AFB: SITE 2

<u>General Site Description:</u> Few cracks: in use as a taxiway		
Date	Loading	Instrumentation
5-75	(a) P-2 Fire truck	(a) Gages installed
11-75	(a) P-2 Fire truck	(a) Gages installed (b) LVDT Beam
3-76	(a) F-4 Load Cart	(a) LVDT Beam

Figure 19. (Continued)



(c) PEASE AFB

<u>General Site Description:</u> Uncracked in-service runway: Rutted by several passes of KC-135A Aircraft and P-2 Fire truck		
Date	Loading	Instrumentation
7-75	(a) P-2 Fire truck (b) KC-135A Aircraft	LVDT Beam

(d) EGLIN AFB: TAXIWAY

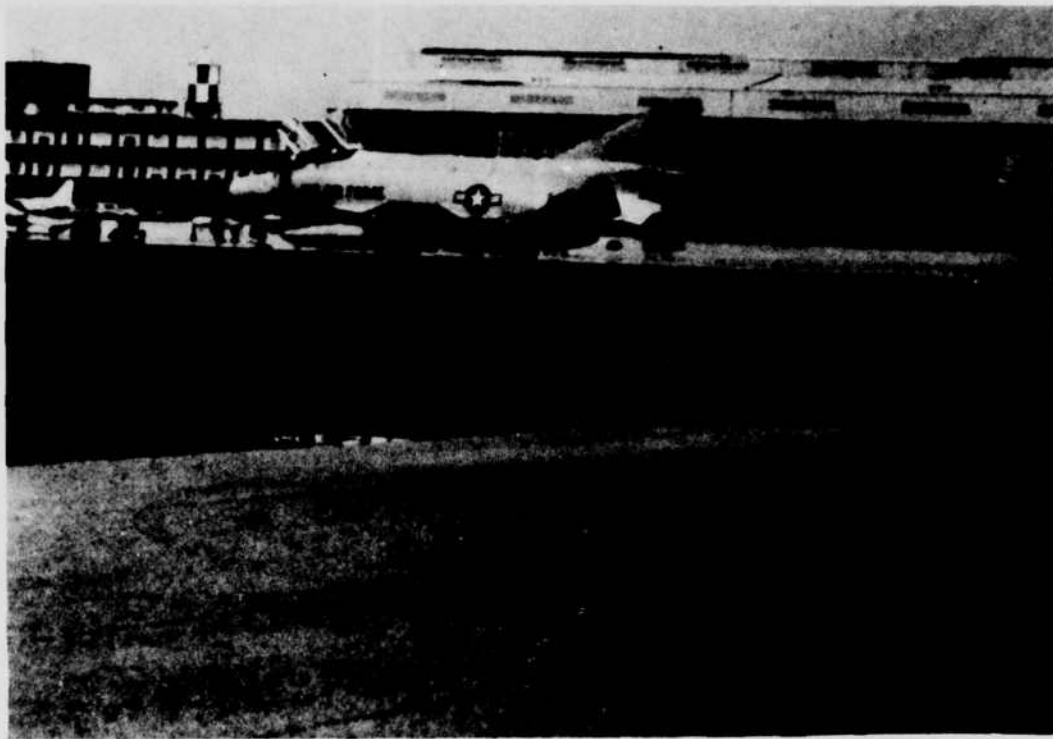
<u>General Site Description:</u> Cracked not-in service taxiway		
Date	Loading	Instrumentation
6-76 <sup>b</sup>	F-4 Load Cart	(a) LED Beam <sup>c</sup> (b) LVDT Beam

a Stationary Beam - Moving Load operation

b 6000 feet of runway were also tested on this date.

c Moving Beam - Moving Load operation

Figure 19. (Concluded)



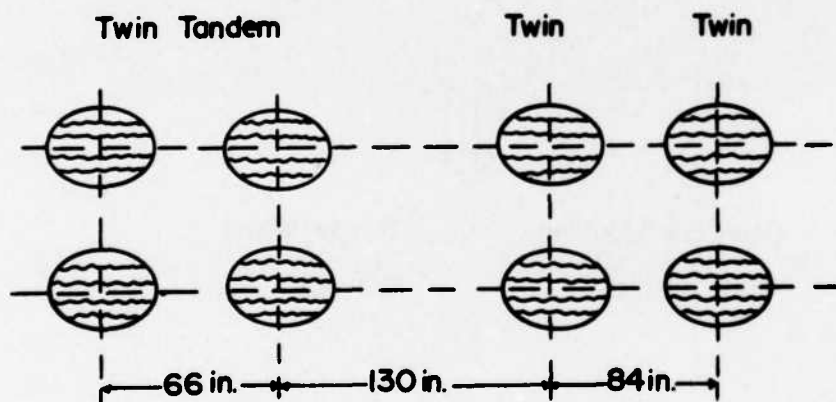
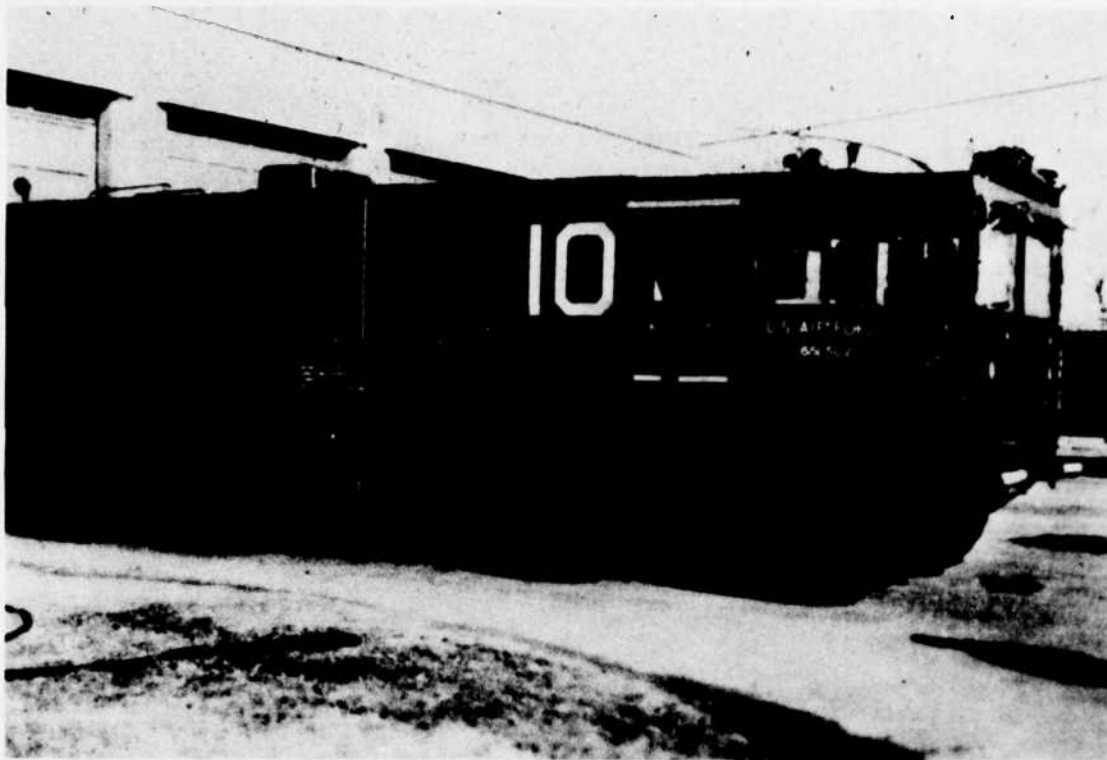
**Gear Configuration**

**Single Wheel**

**Test Weight**

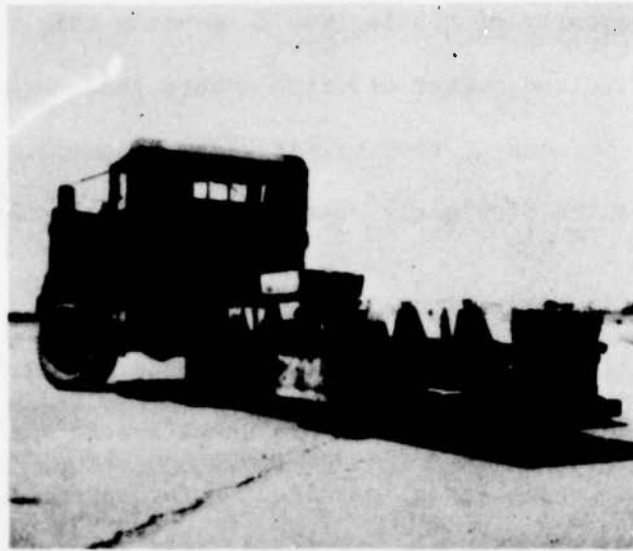
**25 Kips**

**Figure 20. F-4 Aircraft and Pertinent Characteristics**



STD. TEST WEIGHT 66,000 lb

**Figure 21. P-2 Fire Truck and Pertinent Characteristics**



**(a) Loaded**



**(b) Unloaded**

**Figure 22. F-4 Load Cart**

F-4 aircraft. The majority of testing was done using this vehicle.

Because of the limited number of prime movers that were made available during the periods of testing, it became necessary to utilize some test results previously reported by Boyer (Reference 11).

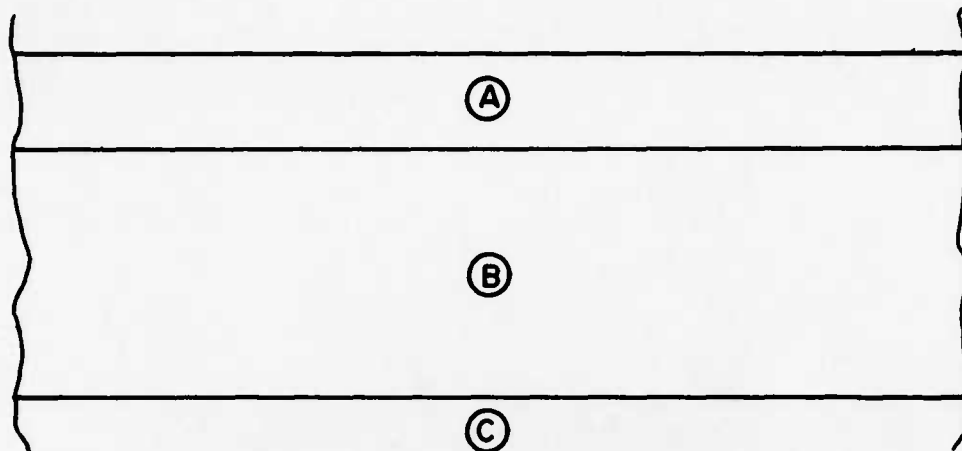
## 5.2 Series B Field Investigations

The field investigations in Series B were conducted by Boyer at Kirtland AFB in New Mexico in 1972. In his investigation deflection measurements were made using gages installed in the pavement in a manner similar to the procedure used in the Series A field investigations. For details on his instrumentation and methodology the reader should refer to the original reference (Reference 11). The pavement characteristics at the three sites reported are shown in Figure 23. The prime movers and their characteristics are shown in Figures 24 through 26.

As previously stated the series B data provide additional information required to test the evaluation and prediction schemes. The gear configuration of the C-130, C-135 and C-131 provide, in addition to a variation in gross load and tire pressures, a loading function due to multiple and sequential wheel loads, and combinations thereof. The C-131 (single-twin) is an example of a multiple but not sequential loading function. The C-130 (single-tandem) is an example of a sequential<sup>6</sup> but partially multiple, loading function. The C-135 (twin-tandem) is an example of sequential and a multiple loading

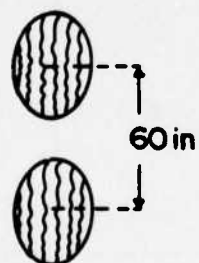
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<sup>6</sup>The P-2 fire truck is an example of a purely sequential loading function.



Test Site No.	Taxiway No.	(A) Asphaltic Concrete(in)	(B) Base Course (in)	(C) Subgrade
1	6	3	9	Silt / Sand
2	2	6.5	8	Silt / Sand
3	8	10	6	Highly Compacted Silt / Sand

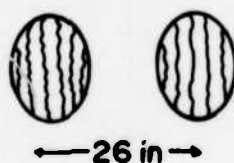
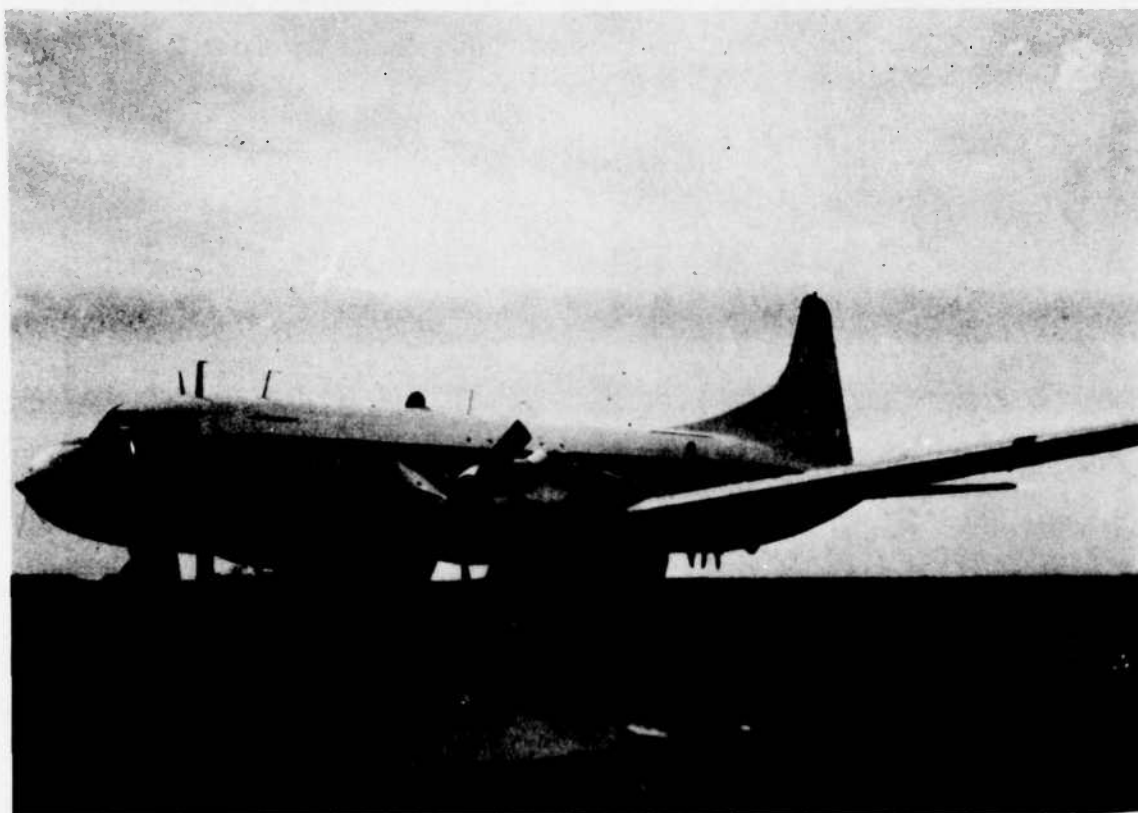
**Figure 23. Site Characteristics Series B Field Investigations (Reference 11)**



Gear Configuration  
STD. Test Weight

Single Tandem  
90 Kips (Gear load)

Figure 24. C-130 Aircraft and Pertinent Characteristics

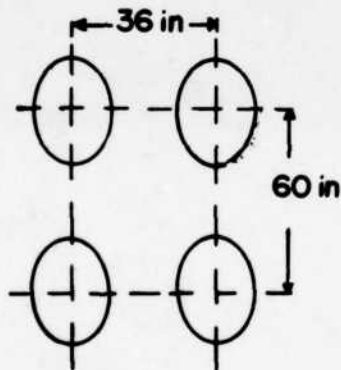


Gear Configuration  
STD. Test Weight

Single Twin  
20 Kips (Gear load)

**Figure 25. C-131 Aircraft and Pertinent Characteristics**





**Gear Configuration**  
**STD. Test Weight**

**Twin-Tandem**  
**20 Kips (Gear load)**

**Figure 26. C-135 Aircraft and Pertinent Characteristics**

function.

The data from the Series A and the Series B Field investigations were analyzed using the evaluation and prediction schemes previously presented.

## SECTION VI

### RESULTS

This research effort encompasses a broad spectrum of engineering activity ranging from the development of NDT equipment and a procedure for nondestructively evaluating flexible pavements, to the development of a methodology for predicting the deflection response of various pavements to different aircraft. This section presents the following:

1. typical results of equipment field verification tests,
2. results of the evaluation of the two sites (Series A: Field Investigations) using the developed evaluation scheme, and,
3. results of the application of the prediction methodology to three different aircrafts at three different sites (Series B: Field Investigations).

#### 6.1 Equipment

It is necessary during the development of new equipment for measurement of pavement deflections to show that the new equipment provides measurements which are consistent with those obtained using established measurement systems. It is assumed that the LVDTs installed in the pavement comprise the absolute measurement system.

##### 6.1.1 The LVDT System

The verification check of the LVDT system consisted of a comparison between pavement deflections measured by an LVDT mounted on the beam and an LVDT installed in the pavement as shown in Appendix B of this report.

Figure 27 shows a comparison of the pavement deflection measured

by an LVDT installed in the pavement and an LVDT mounted on the beam, and produced by the same pass of a P-2 fire truck during the testing sequence conducted at Eglin AFB, at Site 1 on November 17, 1975.

The results show that the installed LVDT and the LVDT mounted on the beam give basically the same measurements.

#### 6.1.2 The LED System

The verification checking of the LED system consisted of two phases: a laboratory and a field testing phase.

The laboratory phase was conducted by Science Applications Incorporated, and is summarized in Appendix A of this report. The principal field checkout consisted of a comparison between the output<sup>7</sup> from an LED on the LED beam and the output from an LVDT mounted on the LVDT beam.

Figures 28 and 29 show the pavement deflections measured by the LED system and the LVDT system, respectively, and produced by one pass of a P-2 fire truck (Figure 21), during the testing sequence at Eglin AFB, Site 1, on November 19, 1975. Figures 30 and 31 show the actual digital output from the LED system and the analog output from the LVDT system as recorded by the light beam recorder. Since the deflections shown were measured for two separate passes of the P-2 fire truck, a direct comparison of measured deflections can not be made.

As stated previously a direct comparison of the measurements made by the two beams (LED and LVDT) could not be made since it is

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<sup>7</sup> Due to persistent problems of compatibility between the LED modules and the magnetic tape recording unit, the LED output was recorded on a light beam recorder.

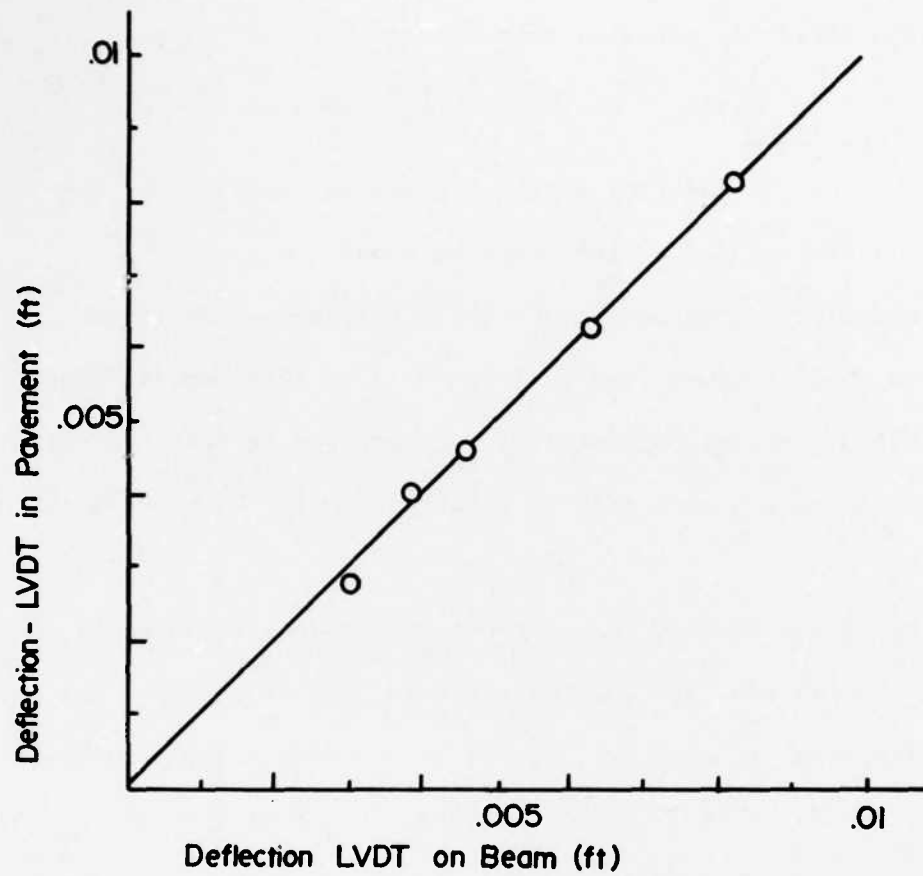


Figure 27. Comparison of LVDT on Beam and LVDT Installed in Pavement

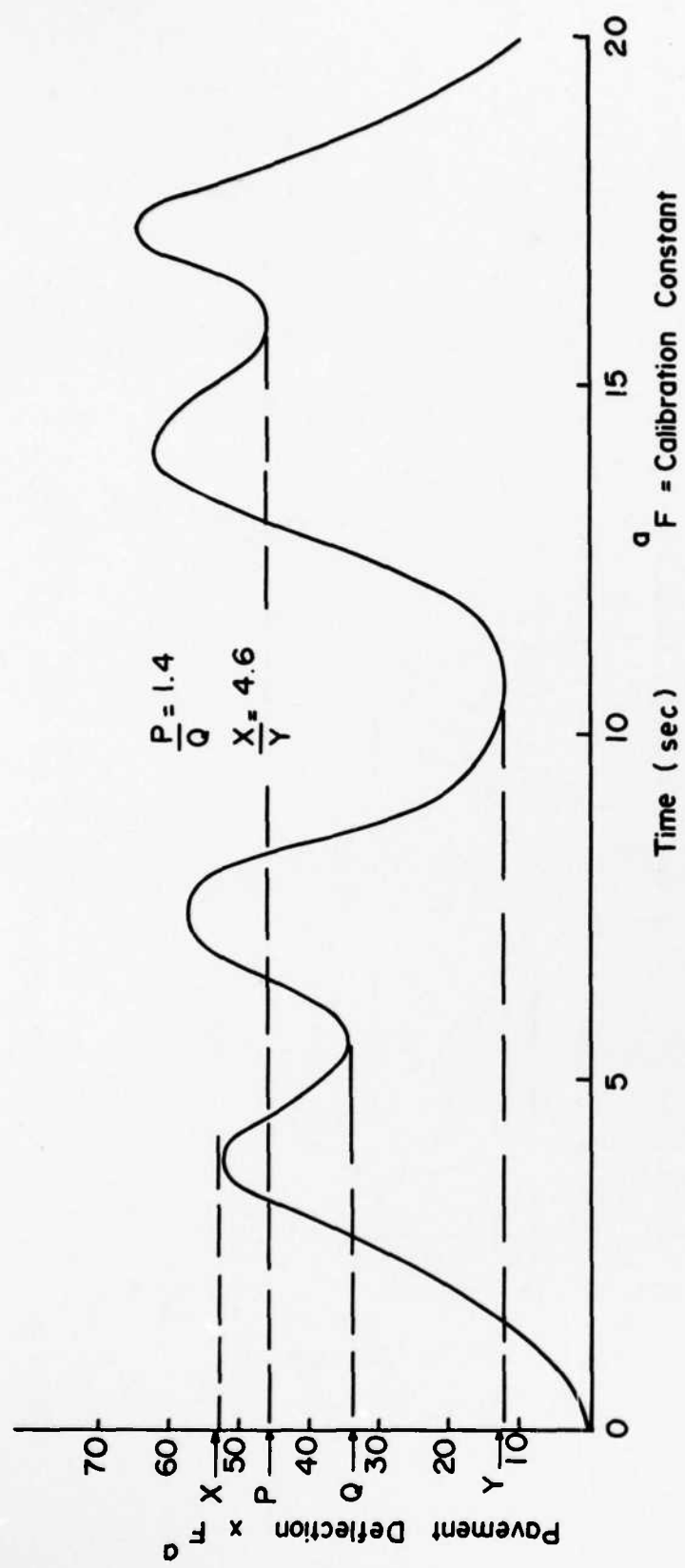


Figure 28. Pavement Deflections Measured by LED System:  
Eglin AFB - Site 1: P-2 Fire Truck Loading

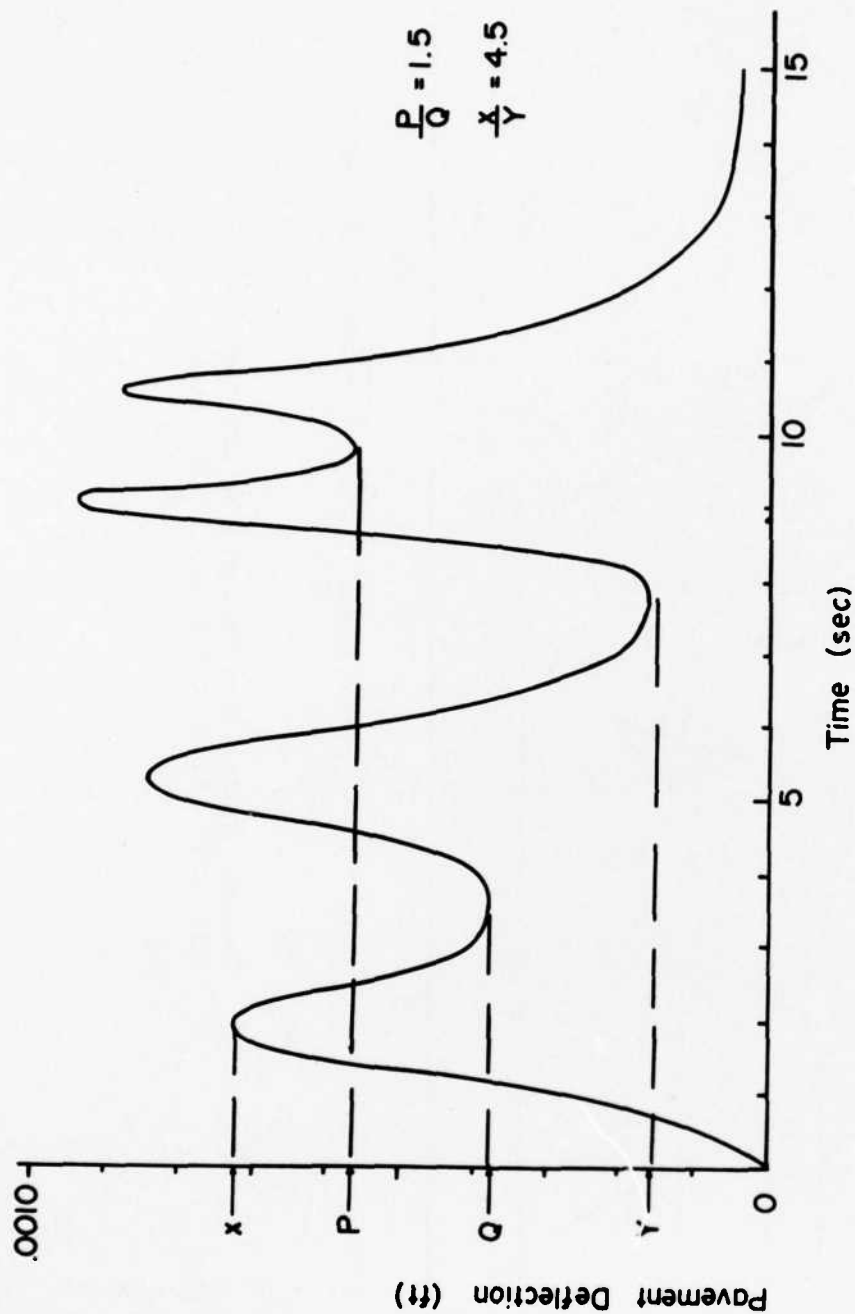


Figure 29. Pavement Deflection of Gage Closest to Edge of Wheel Measured by LVDT System: Eglin AFB - Site 1: P-2 Fire Truck Loading

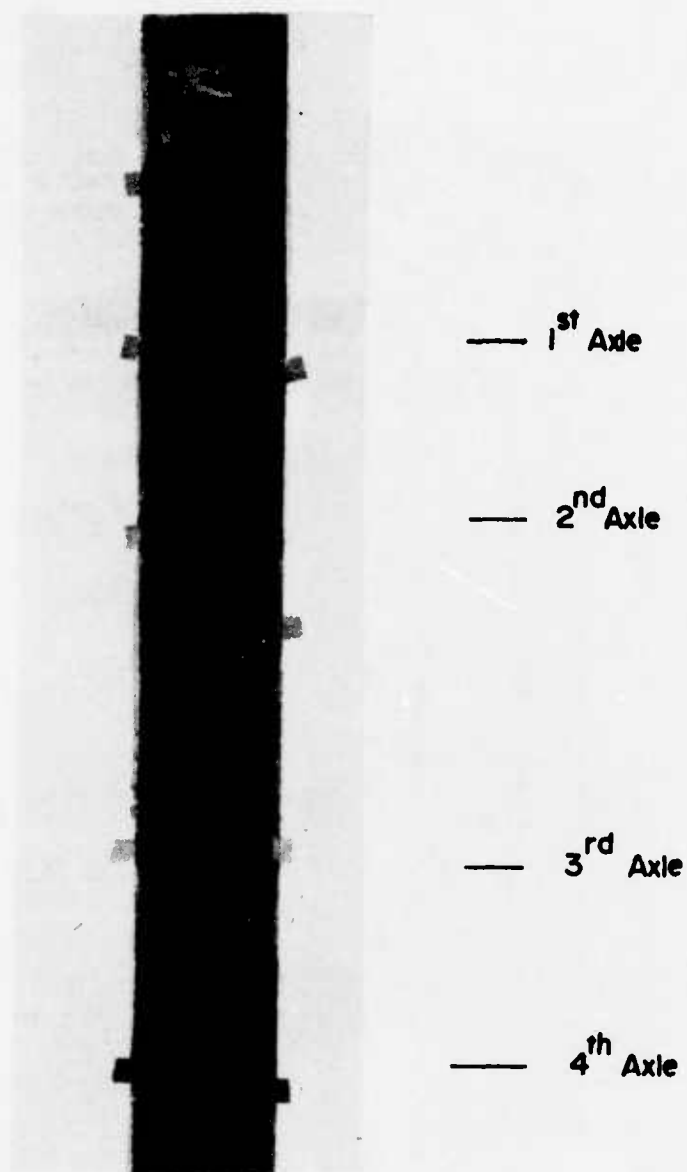


Figure 30. Actual Digital Output From LED System On Light Beam Recorder: P-2 Fire Truck Is Loading Vehicle



DT is time  
increment



Dots indicate points  
used in digitizing light  
beam output

1<sup>st</sup>  
Axle

— 2<sup>nd</sup> Axle

— 3<sup>rd</sup> Axle

— 4<sup>th</sup> Axle

Figure 31. Analog Output From LVDT System: P-2 Fire Truck

impossible to get the two beams over the same point at the same time. Thus, a comparison was made of significant points on the measured deflection plots; e.g., peaks and troughs. The points P, Q, X and Y were selected, where P is the minimum deflection between the second two peaks of the deflection time plot; Q is the minimum deflection between the first two peaks; X is the first peak and Y is the minimum between the first two peaks and the last two peaks. The ratios P/Q and X/Y are thus dimensionless, and are independent of the system (dependent) calibration constants. That is,

$$\frac{X}{Y} = \frac{\text{Actual Light Beam Recorder Output at point X times Constant}}{\text{Actual Light Beam Recorder Output at point Y times Constant}}$$

$$= \frac{\text{Pavement Deflection corresponding to X}}{\text{Pavement Deflection corresponding to Y}}$$

Figures 28 and 29 show that the corresponding ratios have essentially the same values. Both the P/Q and the X/Y ratios differ by only 0.1.

From the discernable deflection observable at point Y in Figure 28 and Figure 29, it can be seen that measurements of less than 0.0001 feet are obtainable by both the LED and LVDT systems.

In June 1976, both the LVDT and the LED systems were used in connection with a study to investigate the difference in the dynamic response of aircraft.

A mechanical system was designed to allow the LED beam to be rigidly mounted on the F-4 load cart. The system was fabricated at Tyndall Air Force Base by Air Force personnel and was then transported to Eglin AFB. At Eglin, 2000 feet of taxiway and 1 1/4 miles of runway

were tested using the LED system attached to the F-4 load cart as shown in Figure 32. The LED measured deflections due to the load wheel of the F-4 load cart as the load cart moved at creep speeds over the pavement. LED measurements were made continuously. The LVDT system was used to make deflection measurements at stations 100 feet apart as the load cart passed in front of the stationary beam. The continuous measurements made by the LED were synchronized with the LVDT stations by the use of an electronic event marker of the LED system. The synchronization allowed the time at which the load wheel passed the LVDT stations to be recorded on the magnetic tape to within 0.25 sec as follows. At the instant the load wheel passed the LVDT station marked on the taxiway, a button was depressed on the control panel of the LED system. This caused a digital record to be made on magnetic tape. Since the scan rate was four scans per second, an event marker could be recorded to within 0.25 seconds, which constituted one scan. Figure 33 shows a summary of the taxiway deflection data. The deflections on the dashed line in Figure 33 were measured at locations offset by about 20 feet from the previous measurement locations. Listing of typical measurements<sup>8</sup> made by the LED system is given in Appendix D.

The results shown on Figures 28 and 29 indicate that the pavement deflection measurements with the LED system are consistent with those of the LVDT system, in form; and the LED can measure deflections with the desired accuracy in a field environment.

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<sup>8</sup>

The LED system data reduction software, a complete listing of all the taxiway data, and a copy of the data (on magnetic tape) has previously been supplied to the Civil Engineering Center, Tyndall AFB, Florida.

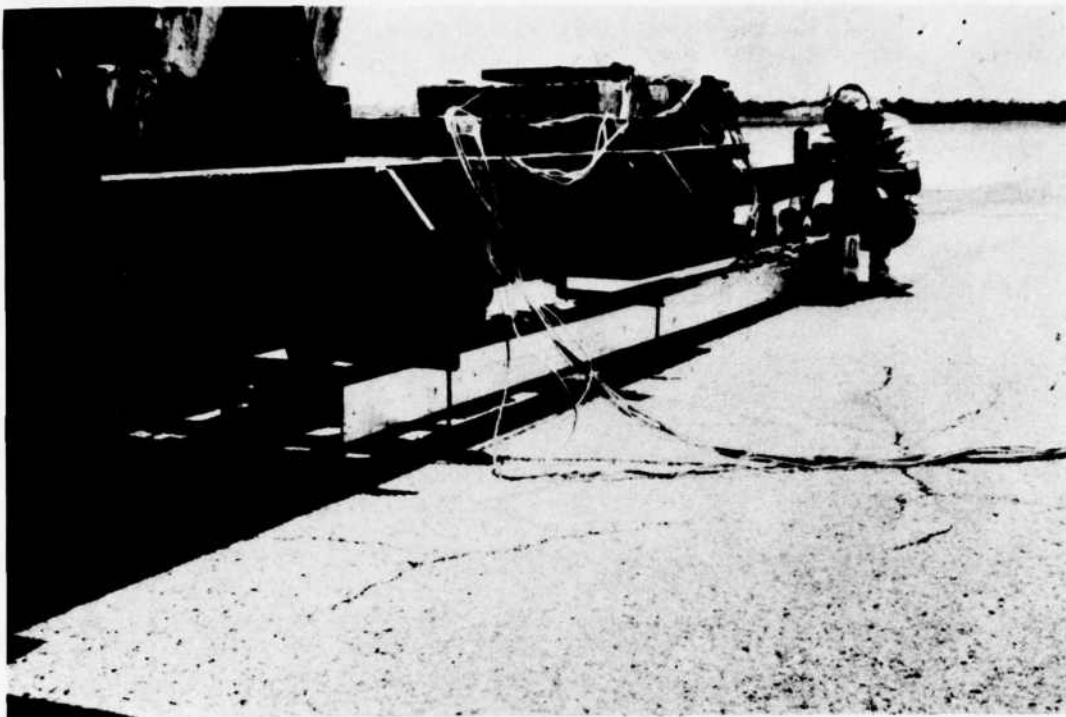


Figure 32. Setup During Moving Beam - Moving Load Operation:  
F-4 Load Cart

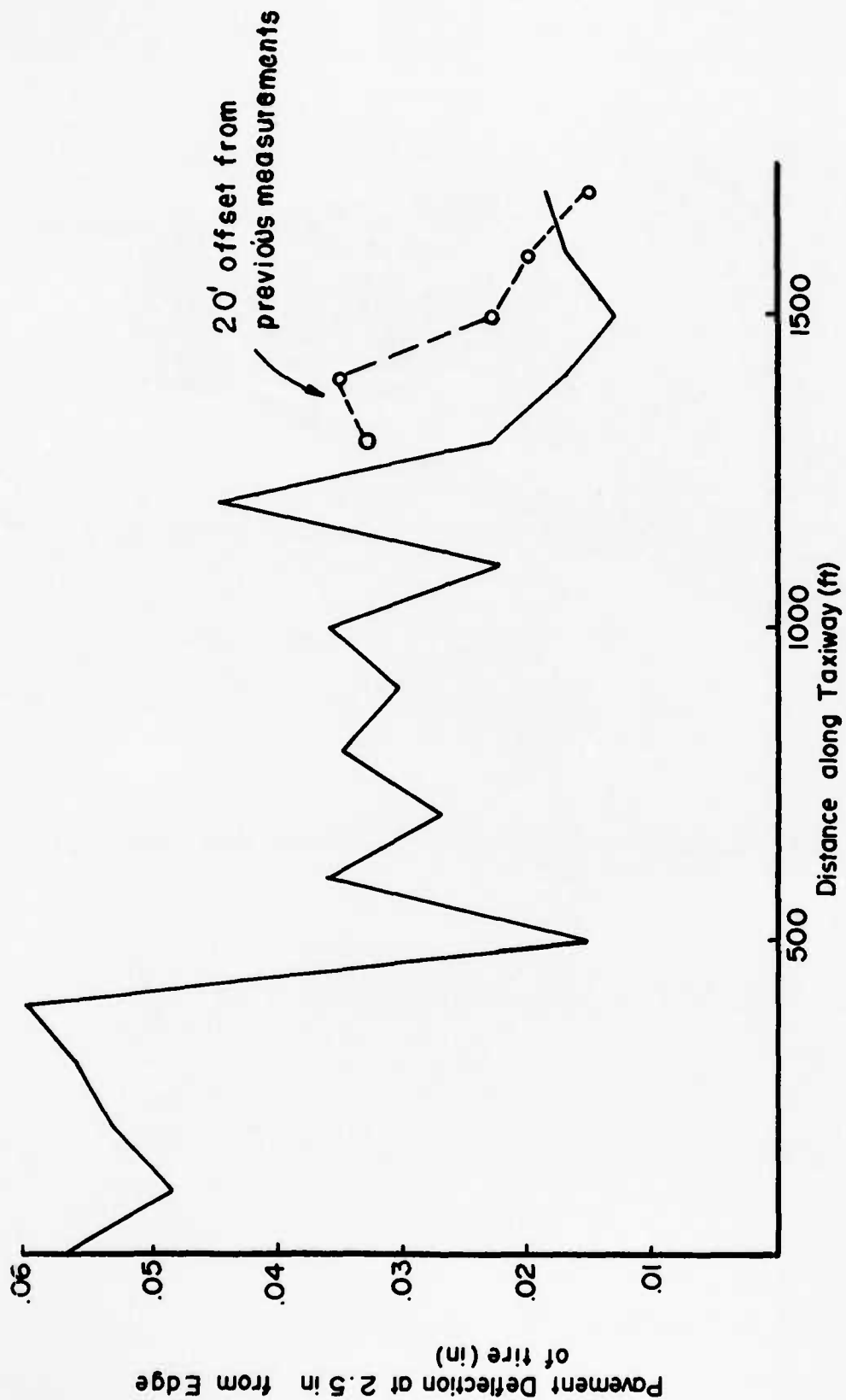


Figure 33. Summary of Taxiway Deflection Measurements-Eglin AFB 1976

## 6.2 Evaluation

Evaluation, as presented here, consists of the following:

1. determining the parameters  $A_{peak}$ ,  $\beta_{peak}$ , and  $r_{peak}$  of the maximum lateral deflection profile due to F-4 loadings,
2. obtaining the  $k$ ,  $c$ , and  $m$  parameters of the transfer function, and
3. relating the determined parameters to performance.

The two sites in Series A field investigation are compared using the data obtained during the field testing program conducted at Eglin AFB in March 1976.

As the F-4 aircraft is the vehicle of primary interest in this study only the results obtained using the F-4 load cart are presented in this section. A more complete listing of the data base and results is given in Appendix D.

Briefly, the evaluation procedure consisted of measuring pavement deflections using the LVDT beam as the F-4 load cart passed in a direction perpendicular to the stationary LVDT beam. From these deflections, the parameters  $A_{peak}$ ,  $\beta_{peak}$ , and  $r_{peak}$  of the maximum lateral deflection profile, and the signature were determined as discussed in detail in paragraph 3.2.1. The  $k$ ,  $c$ , and  $m$  parameters at each site were then obtained using the methodology of paragraph 3.2.2.

### 6.2.1 Pavement Deflections

Figure 34 shows a typical set of deflection functions due to the F-4 load cart as measured by the LVDT beam. Gage 1, which recorded

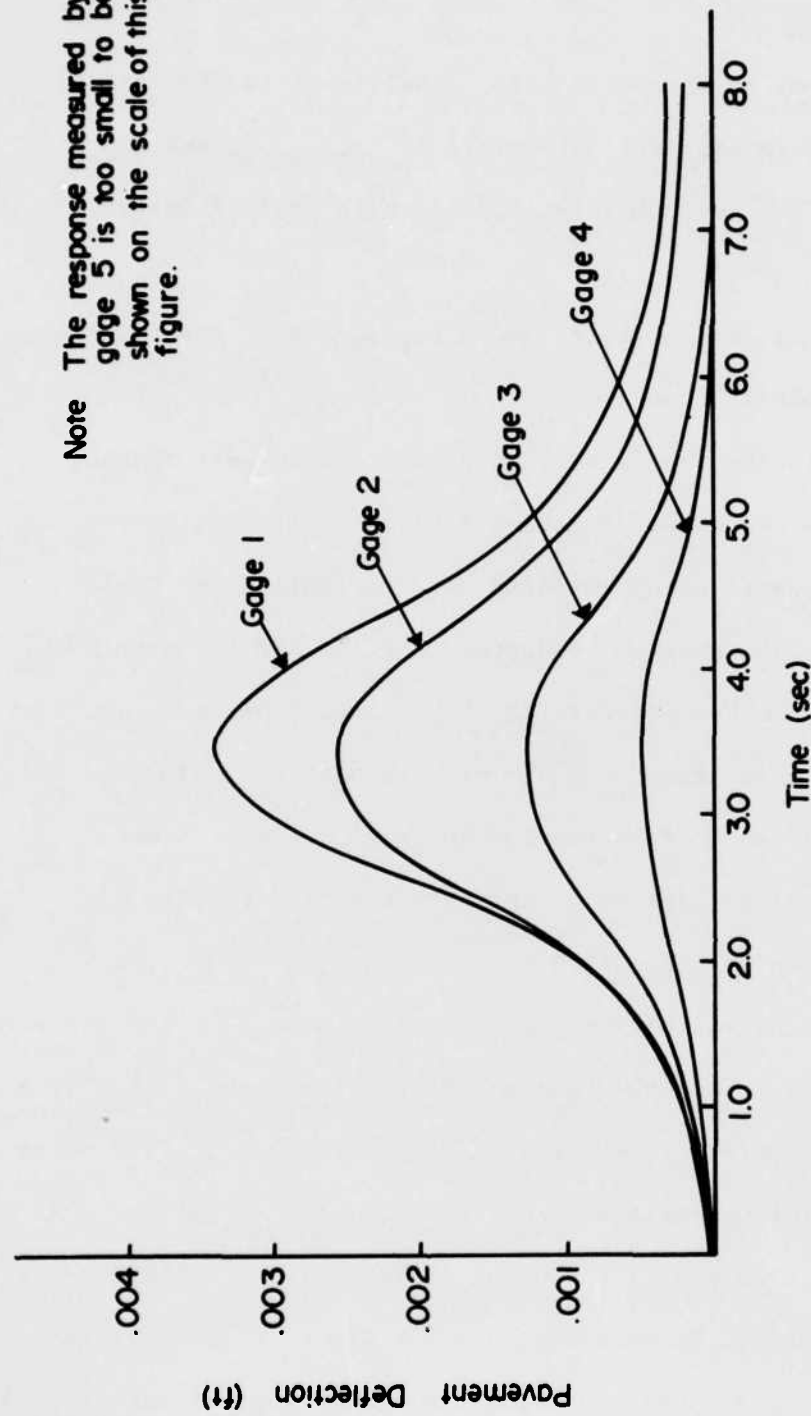


Figure 34. System Response Functions F-4 Loading: Eglin Site 1 (Typical)

the largest deflection is located closest to the wheel. Figure 35 shows the maximum deflection of each gage plotted against the distance of the gage from the edge of the tire print. The dashed line through the points G-1 through G-5 is the lateral profile of maximum deflections at Site<sup>9</sup> 1 for one pass of the F-4 load cart. Figure 35 also shows the  $A_{peak}$ ,  $\beta_{peak}$ , and  $r_{peak}$  parameters determined as discussed in paragraph 3.2.1 and the maximum deflections at each gage calculated by equation 2. Figure 36 shows a similar plot for one pass of the F-4 load cart at Site 2. Tables 3 and 4 give the stations<sup>10</sup> and values of the  $A_{peak}$ ,  $\beta_{peak}$ , and  $r_{peak}$  value for Sites 1 and 2, respectively. Figures 37 and 38 show the variability in the measured maximum lateral deflection values for Sites 1 and 2, respectively. Figures 39 and 40 show a comparison of the local and site characteristics at the two sites as given by the  $A_{peak}$ ,  $\beta_{peak}$ , and  $r_{peak}$  values. "Local" refers to a station or location at a "site". The lines in these figures are drawn for convenience and do not represent continuity of parameter values. Figure 41 shows the typical effects of two consecutive passes on the maximum lateral pavement deflection profiles.

These results show the following:

1. The gage (Gage 1, Figure 34) closest to the wheel records the maximum deflection and retains the most permanent set after the wheel load has passed. The gage (Gage 4, Figure 34) farthest from the wheel does the opposite; namely,

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<sup>9</sup> Sites are indicated in Figures B-1(a) and B-3(a).

<sup>10</sup> Stations are given in Appendix B, Figures B-1(b) and B-3(b).



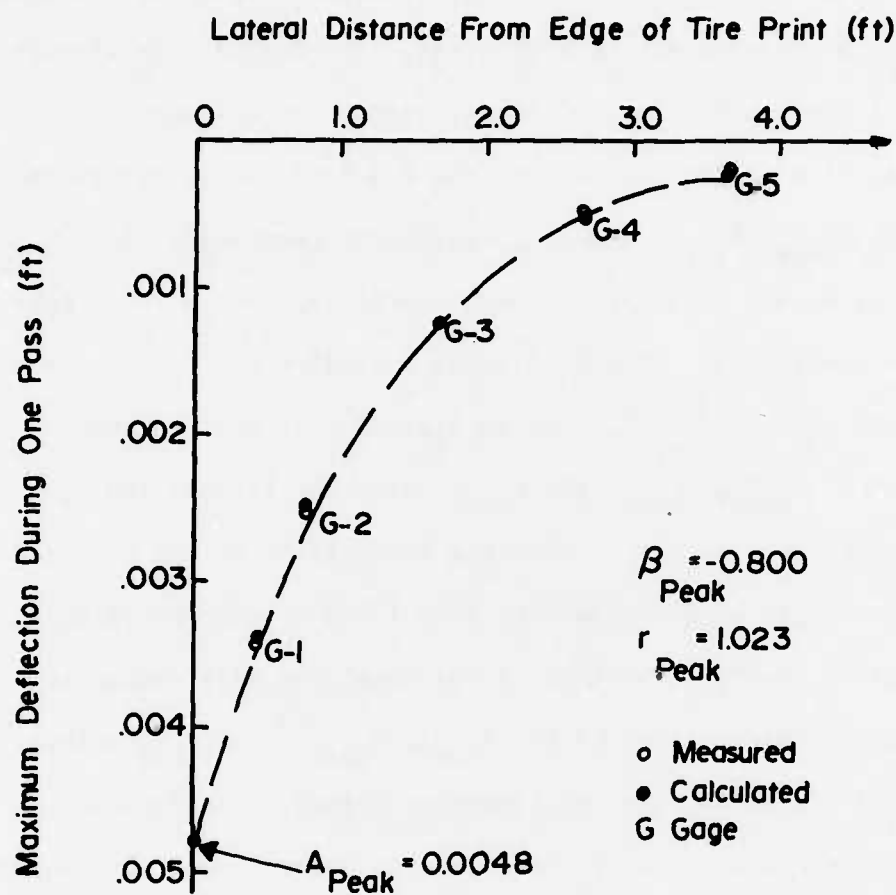


Figure 35. Eglin AFB: Site 1 Lateral Profile of Maximum Deflections for F-4 Loading (Typical)

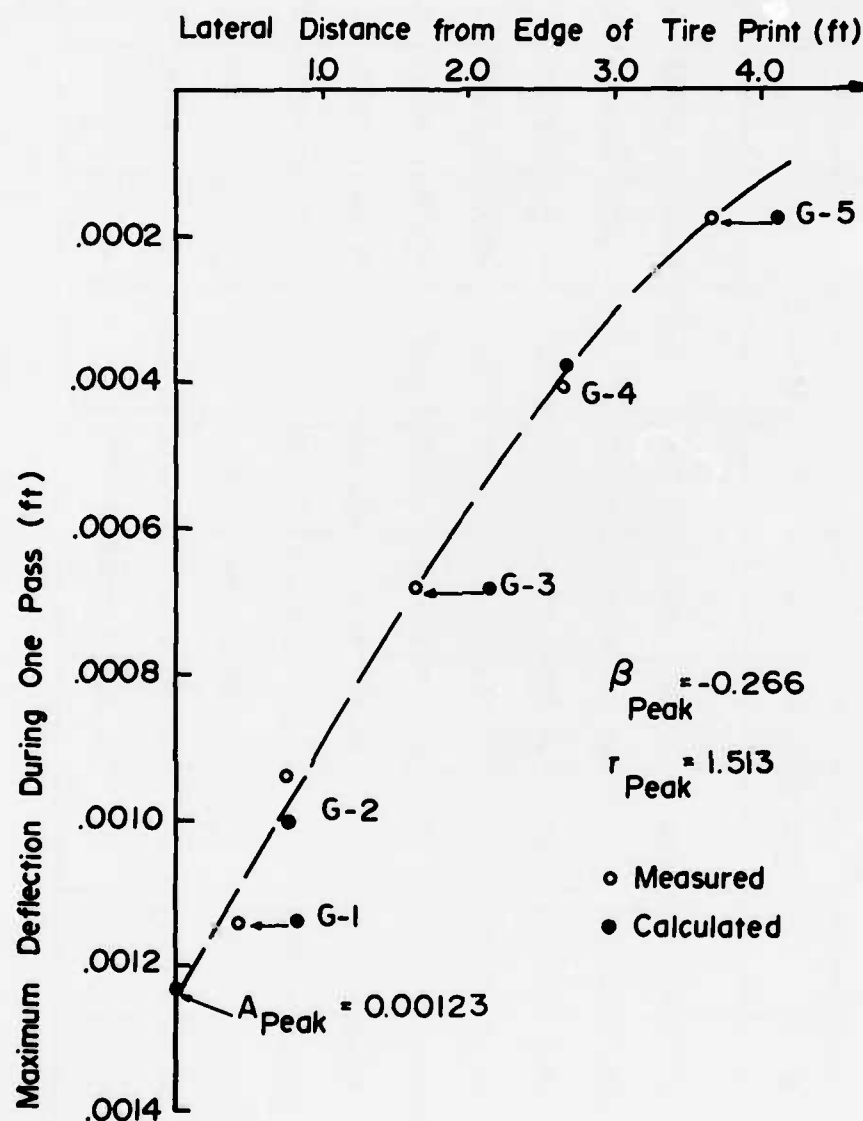


Figure 36. Eglin AFB: Site 2 Lateral Profile of Maximum Deflection for F-4 Loading (Typical)

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NONCONTACT NONDESTRUCTIVE DETERMINATION OF PAVEMENT  
DEFLECTION UNDER MOVING LOADS(U) PURDUE RESEARCH  
FOUNDATION LAFAYETTE IN M E HARR ET AL AUG 77

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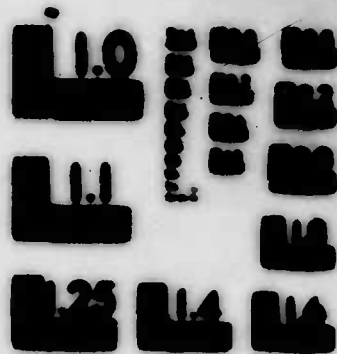
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NL





RESOLUTION TEST CHART  
NATIONAL BUREAU OF STANDARDS-1963-A

TABLE 1. Parameters of the various linear regression curves, 1953-54, 1954-55, 1955-56, 1956-57

Station	$\bar{r}$	$\bar{A}$	$\bar{B}$	Station	$\bar{r}$	$\bar{A}$	$\bar{B}$	Station	$\bar{r}$	$\bar{A}$	$\bar{B}$	Station	$\bar{r}$	$\bar{A}$	$\bar{B}$
11	-0.823	0.00102	-0.737	21	-0.827	0.00106	-0.734	31	-0.823	0.00102	-0.734	41	-0.823	0.00102	-0.734
	-0.823	0.00107	-0.735		-0.824	0.00105	-0.735		-0.823	0.00102	-0.734		-0.823	0.00102	-0.734
21	-0.749	0.00102	-0.737	31	-0.733	0.00106	-0.734	41	-0.823	0.00102	-0.734	51	-0.823	0.00102	-0.734
	-0.823	0.00102	-0.735		-0.734	0.00105	-0.735		-0.823	0.00102	-0.734		-0.823	0.00102	-0.734
31	-0.823	0.00102	-0.734	41	-0.773	0.00107	-0.734	51	-0.823	0.00102	-0.734	61	-0.823	0.00102	-0.734
	-0.823	0.00102	-0.734		-0.824	0.00105	-0.735		-0.823	0.00102	-0.734		-0.823	0.00102	-0.734
41	-0.823	0.00102	-0.734	51	-0.823	0.00102	-0.734	61	-0.823	0.00102	-0.734	71	-0.823	0.00102	-0.734
	-0.823	0.00102	-0.734		-0.823	0.00102	-0.734		-0.823	0.00102	-0.734		-0.823	0.00102	-0.734
51	-0.823	0.00102	-0.734	61	-0.823	0.00102	-0.734	71	-0.823	0.00102	-0.734	81	-0.823	0.00102	-0.734
	-0.823	0.00102	-0.734		-0.823	0.00102	-0.734		-0.823	0.00102	-0.734		-0.823	0.00102	-0.734

of  $\bar{r}$  and  $\bar{A}$  and  $\bar{B}$  are given in Table 1.  $\bar{r}$  and  $\bar{A}$  are given in Table 1.

TABLE 1. PARAMETERS OF THE HIGHER LAMINAL DEFORMATION FURTHER, WITH AN. WITH 1976. WITH 2

Station	Dr	A	0	Station	Dr	A	0	Station	Dr	A	0
A1	-0.440	0.00000	-0.445	B1	-0.472	0.00153	-0.365	C1	-0.501	0.00172	-0.401
A2	-0.542	0.00000	-0.504	B2	-0.470	0.00139	-0.270	C2	-0.570	0.00236	-1.200
A3	-0.543	0.00001	-0.250	B3	-0.477	0.00112	-0.400	C3	-0.451	0.00140	-0.301
A4	-0.541	0.00130	-0.215	B4	-0.500	0.00130	-0.476	C4	-0.502	0.00139	-0.300
A5	-0.570	0.00140	-0.244	B5	-0.500	0.00130	-0.475	C5	-0.400	0.00135	-0.256
	-0.570	0.00126	-0.235		-0.475	0.00134	-0.387		-0.501	0.00139	-0.300
	-0.570	0.00143	-0.242		-0.503	0.00134	-0.230		-0.530	0.00135	-0.300
	-0.500	0.00175	-0.400		-0.400	0.00130	-0.230		-0.737	0.00097	-0.701
	0.777	0.00040	-0.070		-0.400	0.00130	-0.200		-0.506	0.00144	-0.500

a) See Appendix Table 1.

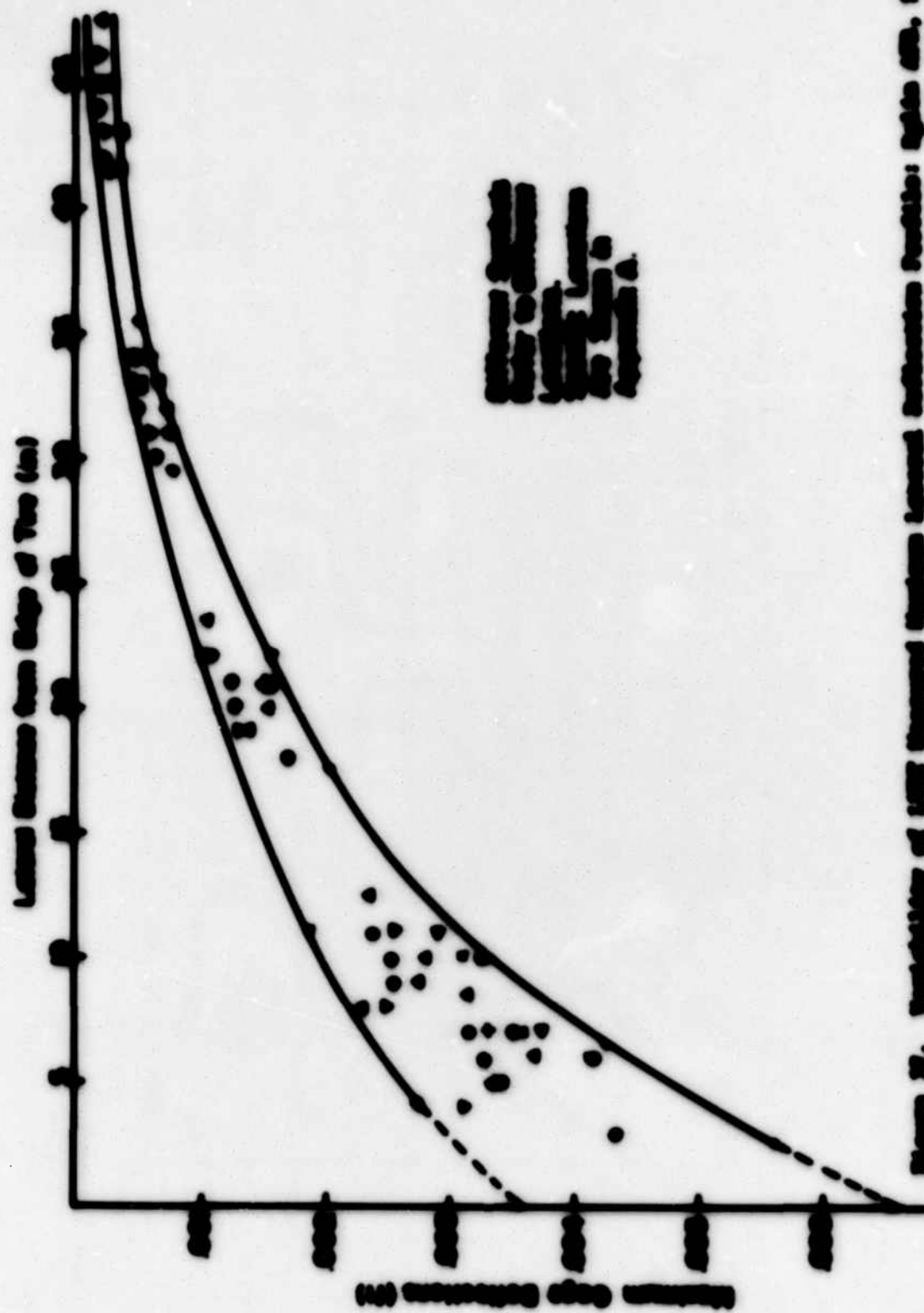


Figure 27. Relationship of LAI measured between leaves and leaflets: Right side, 1970; Left side, 1971.

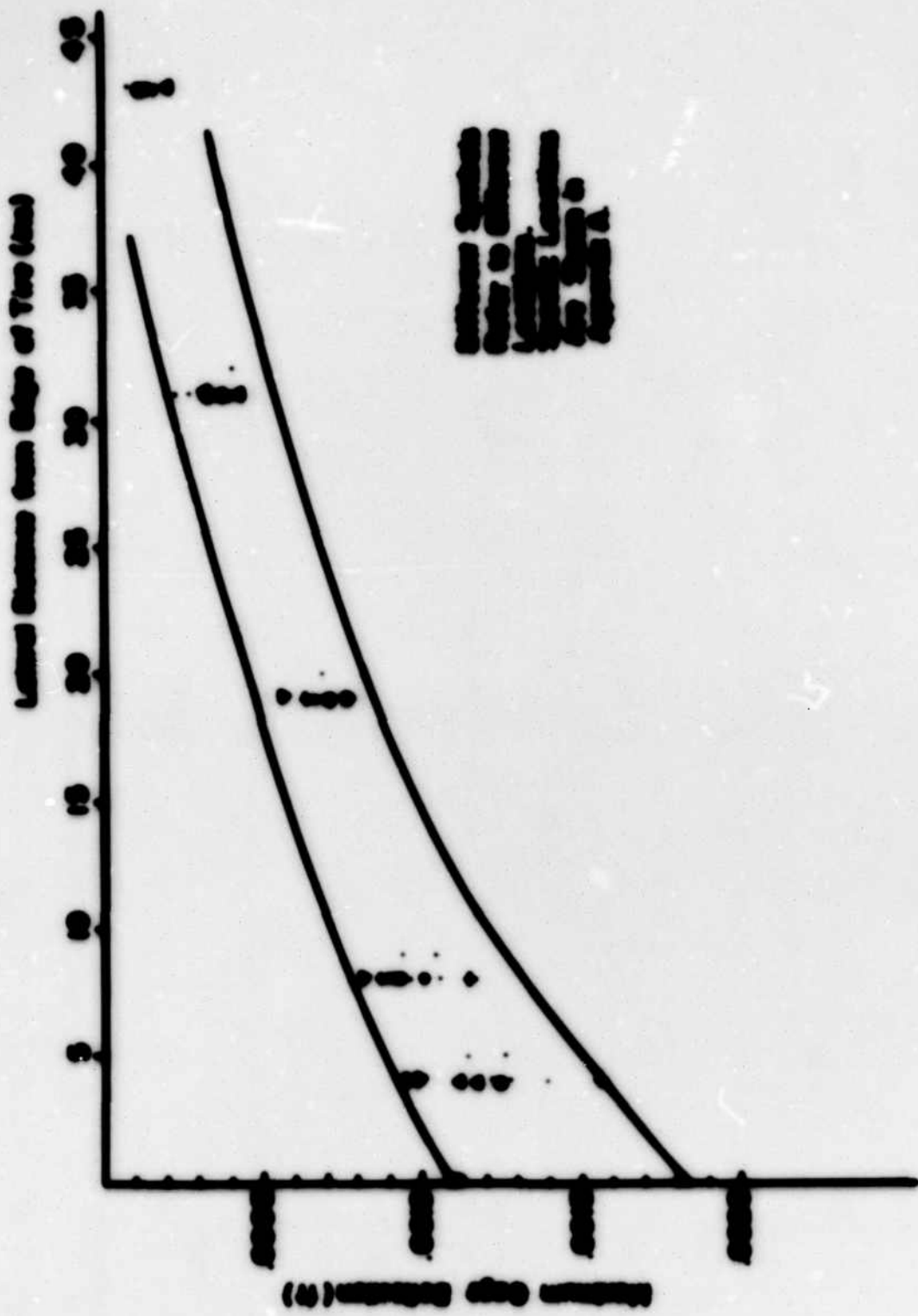


Figure 21. Relationship of Maximum Lateral Distance from Edge of Tree to Maximum Edge Distance.



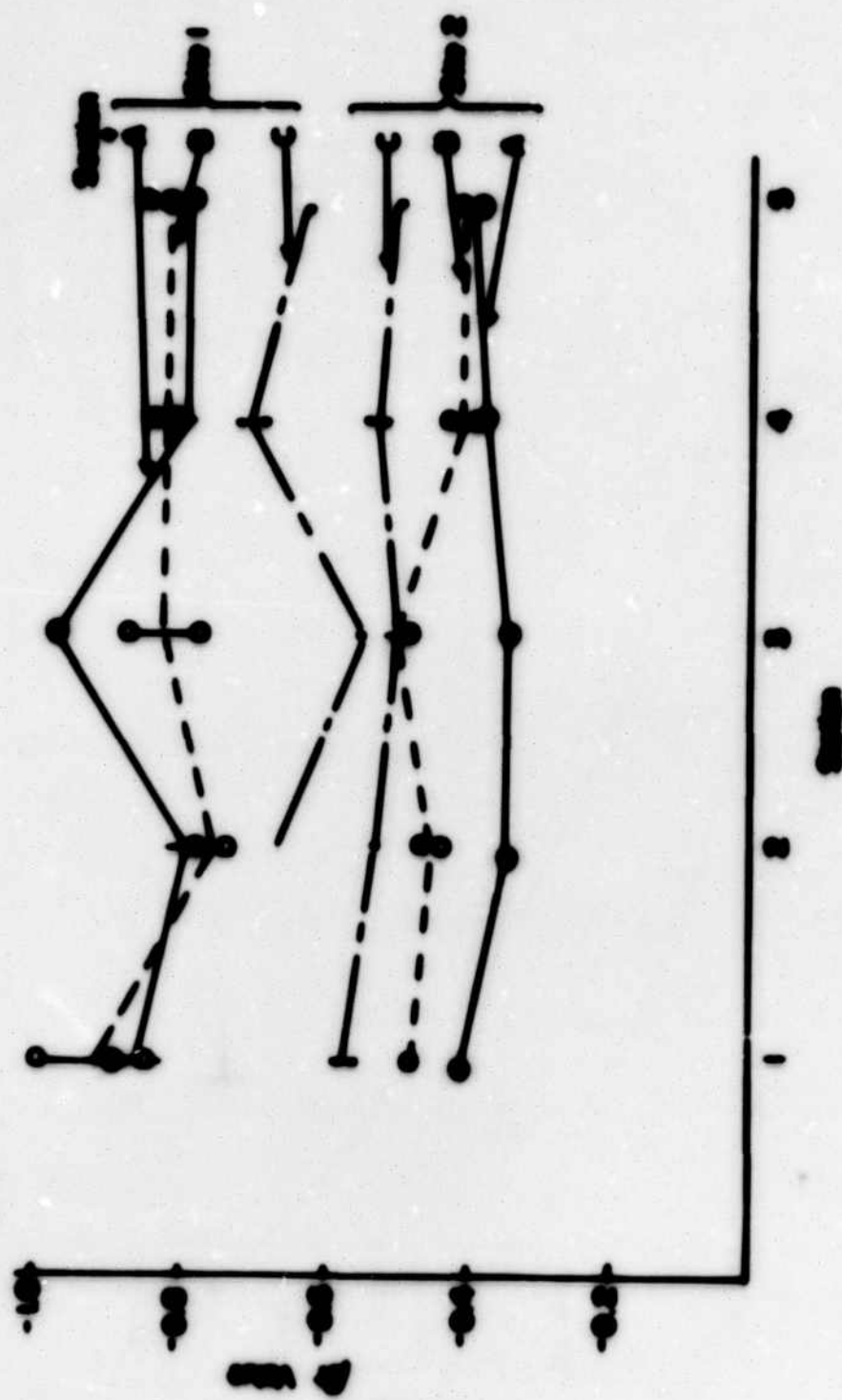


Figure 29. Comparison of Level and Site Characteristics as shown by  
Air volume: Right side, March 1971

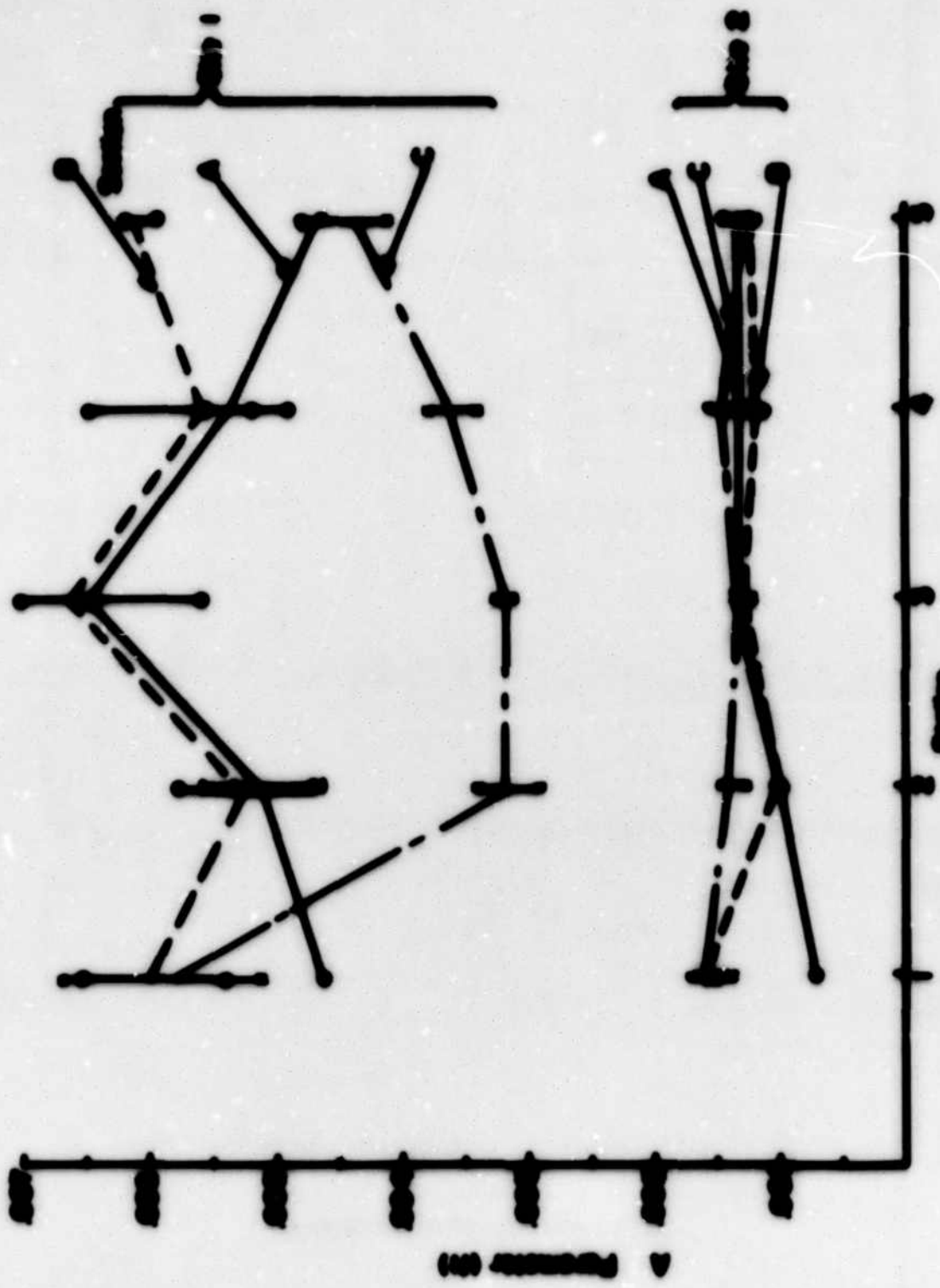


Figure 1. Comparison of the frequency of the two series, A and B, over time. The frequency of series A is generally higher than that of series B.



Figure 41. Effect of the Orientation of the Tree on the Lateral Distance

records the smallest deflection and shows no permanent set. The amount of permanent set increases as distance from the wheel decreases.

2. The peakness of deflection-time plots decreases as the distance from the wheel increases (Figure 34).
3. The width of the measured maximum lateral deflection basin is about 4 feet to 5 feet for both Site 1 (Figure 35) and Site 2 (Figure 36).
4. The maximum measured deflection at Site 1 is about three to four times the maximum deflection at Site 2.
5. There is a close fit between the calculated and measured maximum lateral deflection profiles.
6. There is considerable variability in the measured maximum lateral deflection profile at both Site 1 and Site 2, over the areas tested (Figures 37 and 38).
7. The absolute values of  $r_{peak}$  and  $\delta_{peak}$  are consistently larger for Site 2 than Site 1, and the  $A_{peak}$  values are smaller for Site 2 than Site 1.
8. Short term repetition of load decreases the measured deflection i.e. the second pass of the F-4 load cart produced less deflections than the first pass (Figure 41).

### **6.2.2 Transfer Functions**

Transfer functions were calculated using the theory and methodology presented in paragraph 3.2.2. Briefly, the procedure involved finding the transfer function which, when convoluted implicitly with the signature yielded an equivalent input, which satisfied certain

specified conditions.

Figure 42 shows the calculated equivalent force and the components of the force on the left hand side of equation 1. Figure 43 shows a comparison of the equivalent force calculated by implicit convolution (equation 15) and by direct substitution in equation 1. Figures 44 and 45 show typical transfer functions for Sites 1 and 2, respectively. Tables 5 and 6 list the parameters of the transfer function for the two sites tested. Station labels (A1, A2 etc) correspond to station locations shown in Appendix B. The  $b$ ,  $c$ , and  $a$  parameters were obtained from deflections measured at each location. Where two values are given at the same station, the first listed value corresponds to a forward pass and the second, to a backward pass of the F-4 load cart. Additional entries designate the repetition of the cycle. Figures 46 and 47 show a comparison of the local and site characteristics as given by the equivalent stiffness ( $b$ ) and damping ( $c$ ) parameters. Figures 48 (TDT is time dependent transfer) and 49 show a comparison of the magnitude of the first peaks and the time to the first peak of the transfer functions having the parameters listed in Tables 5 and 6, respectively. Figure 50 shows the input force,  $F(t)$ , and the signature  $s(t)$  for one pass of the F-4 load cart. These results show the following:

1. the numerical procedure used to find the transfer function is consistent with the developed theory, both in the determination of the force components (Figure 42), and implicit convolution techniques to obtain the equivalent force (Figure 43).

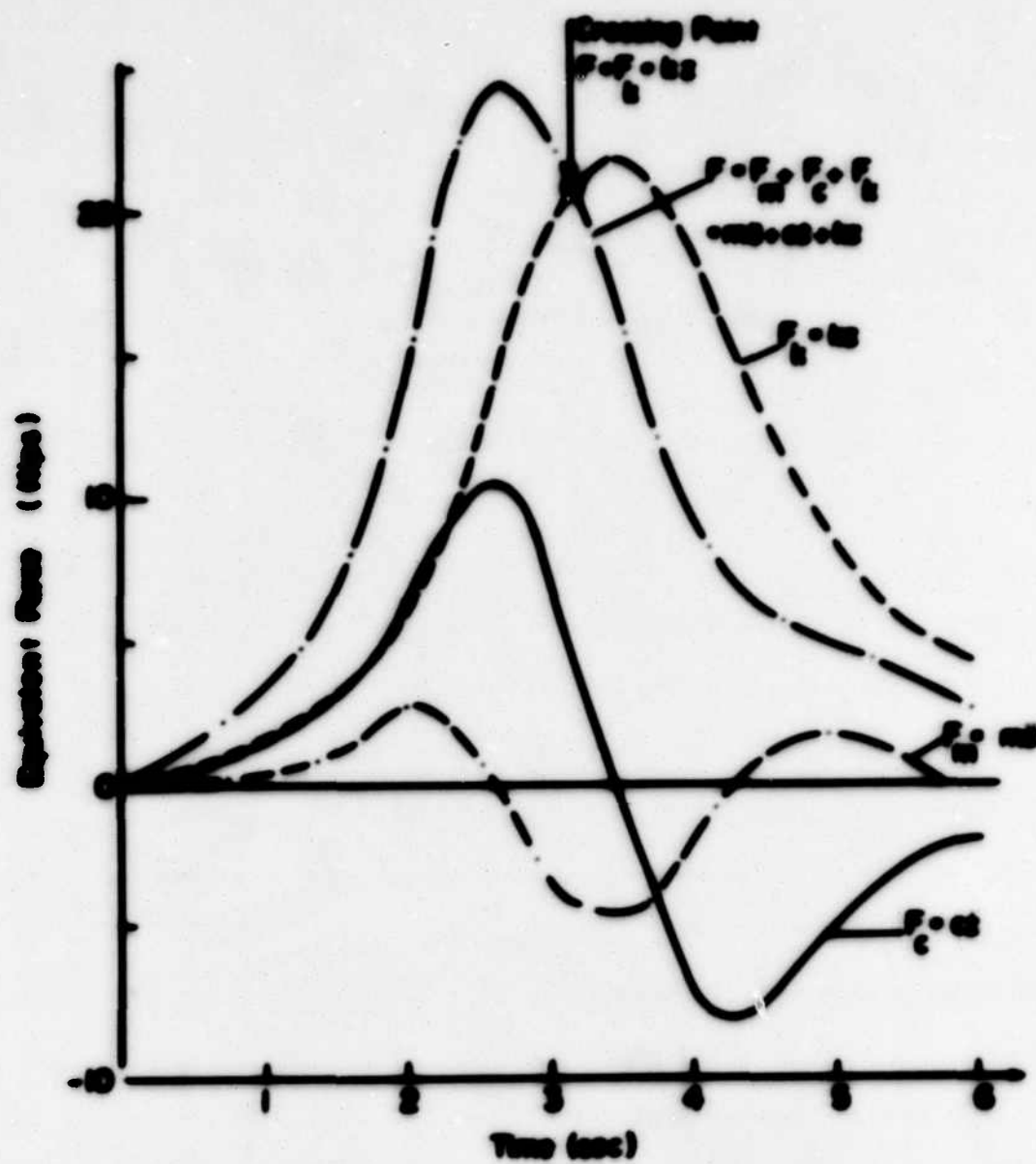


Figure 42. Calculated Equivalent Force and Components (Typical)



Figure 43. Comparison of Newtonian and Coriolis Justness (Typical)

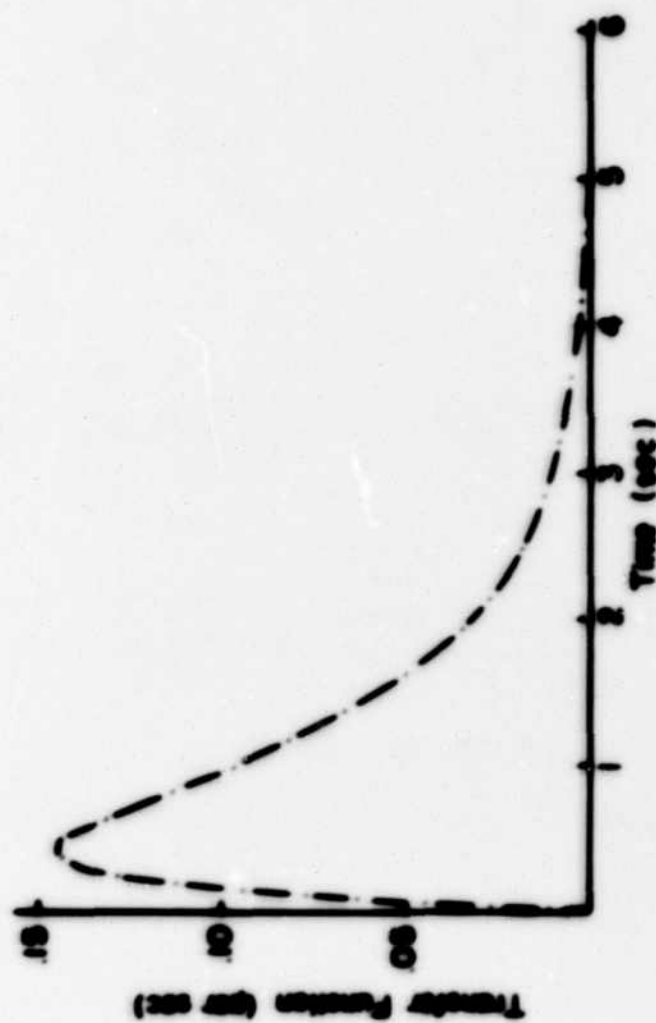


Figure 44. Transfer Function: Eglin AFB Site 1 (Typical)



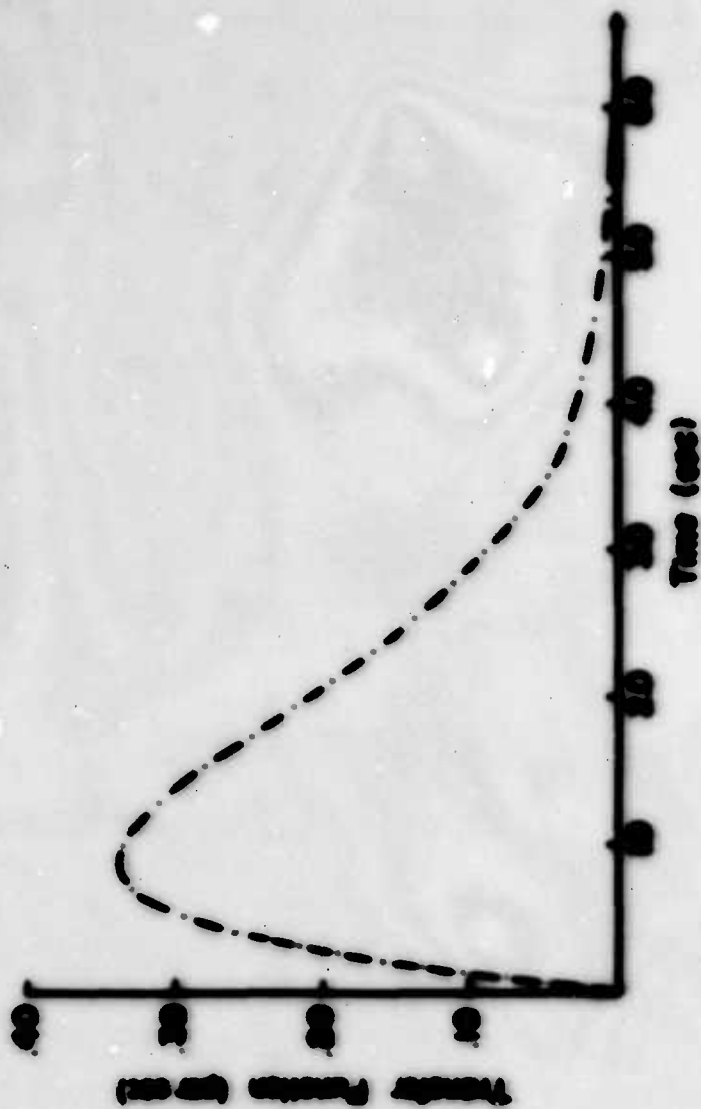


Figure 45. Transfer Function: Split AFB Site 2 (Typical)

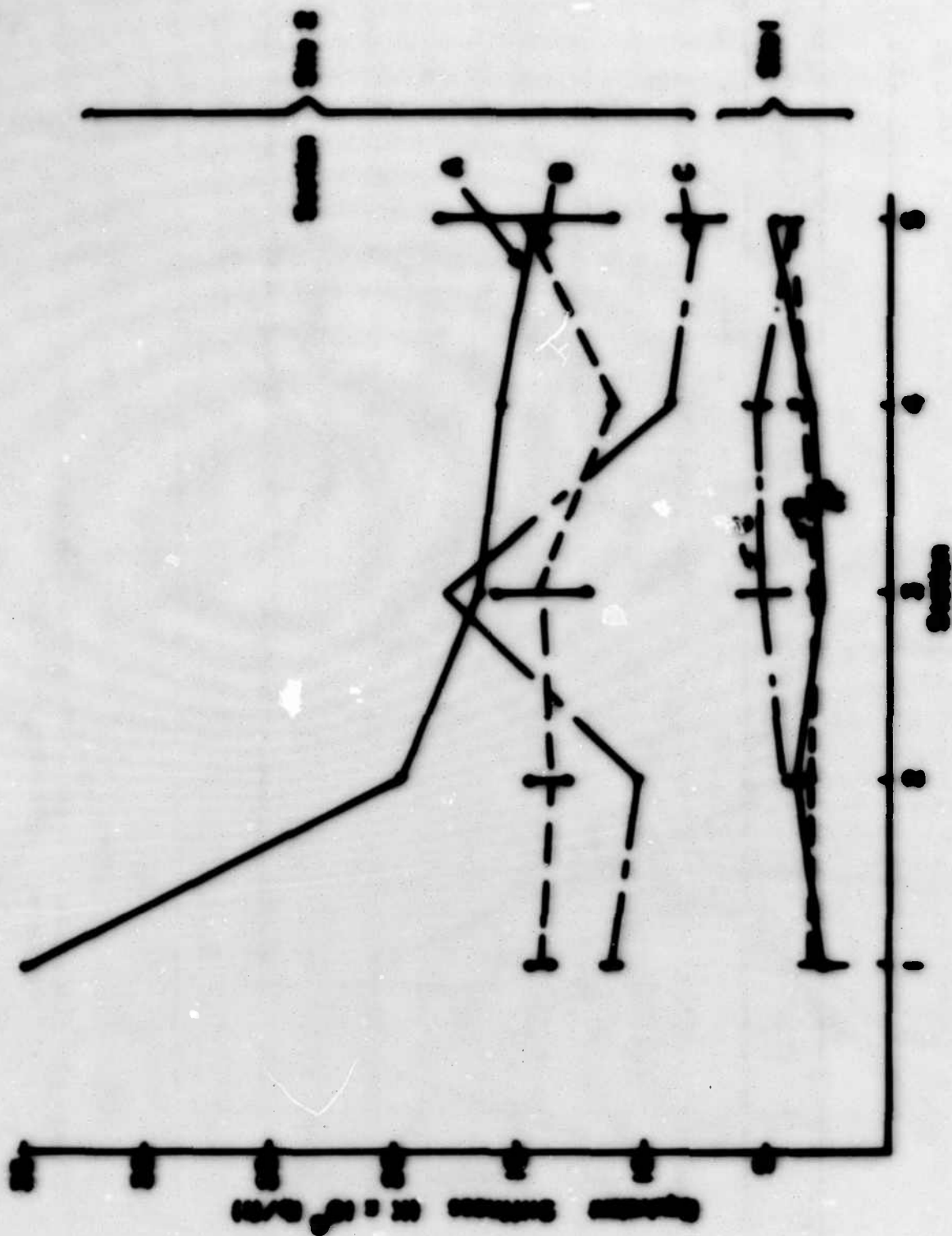


Figure 44. Comparison of Level and Size Characteristics of Rivers by 5-Station:  
River A, River B, River C

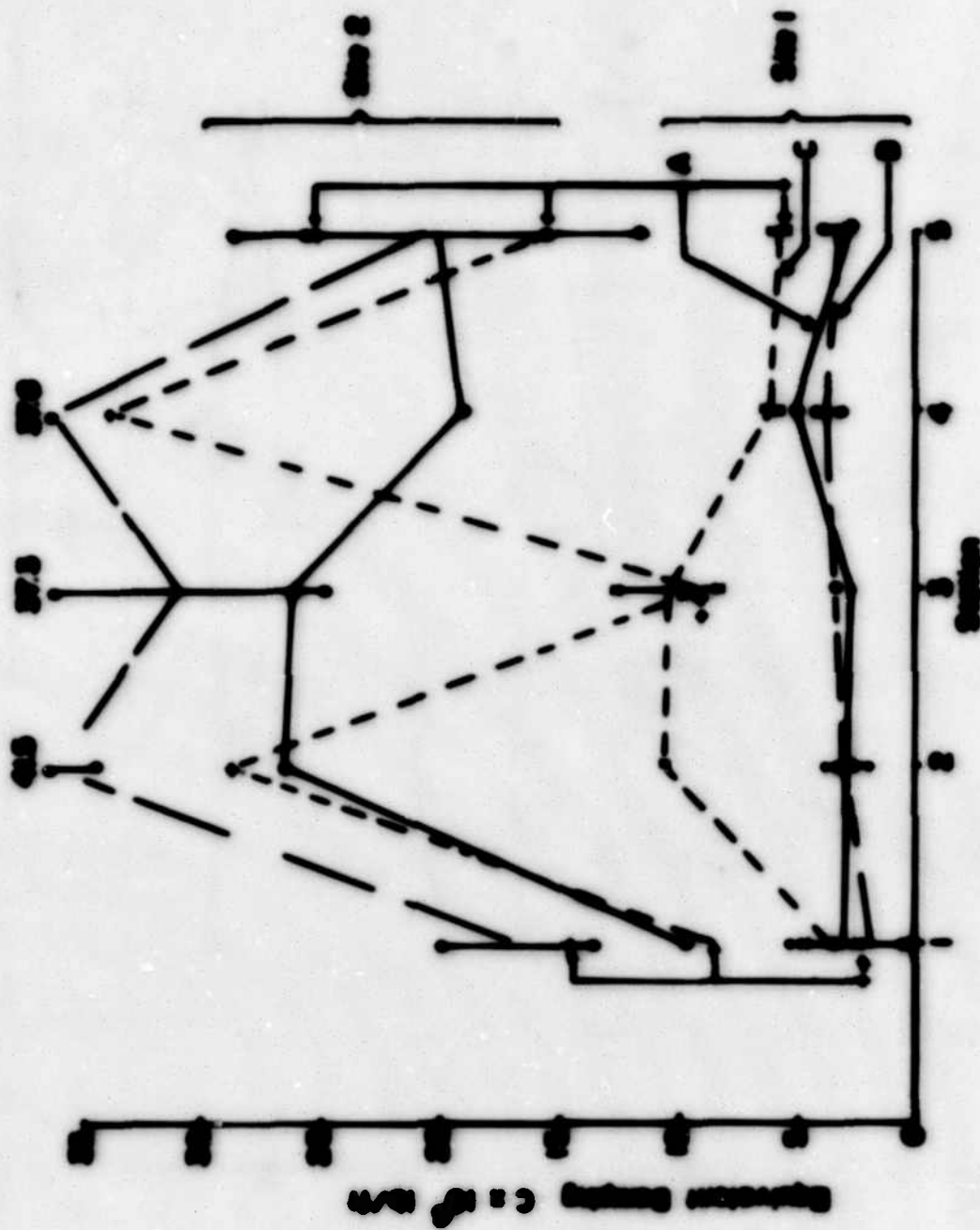


Figure 47. Comparison of land and site characteristics as shown by  
C-Document: April 1976, March 1976

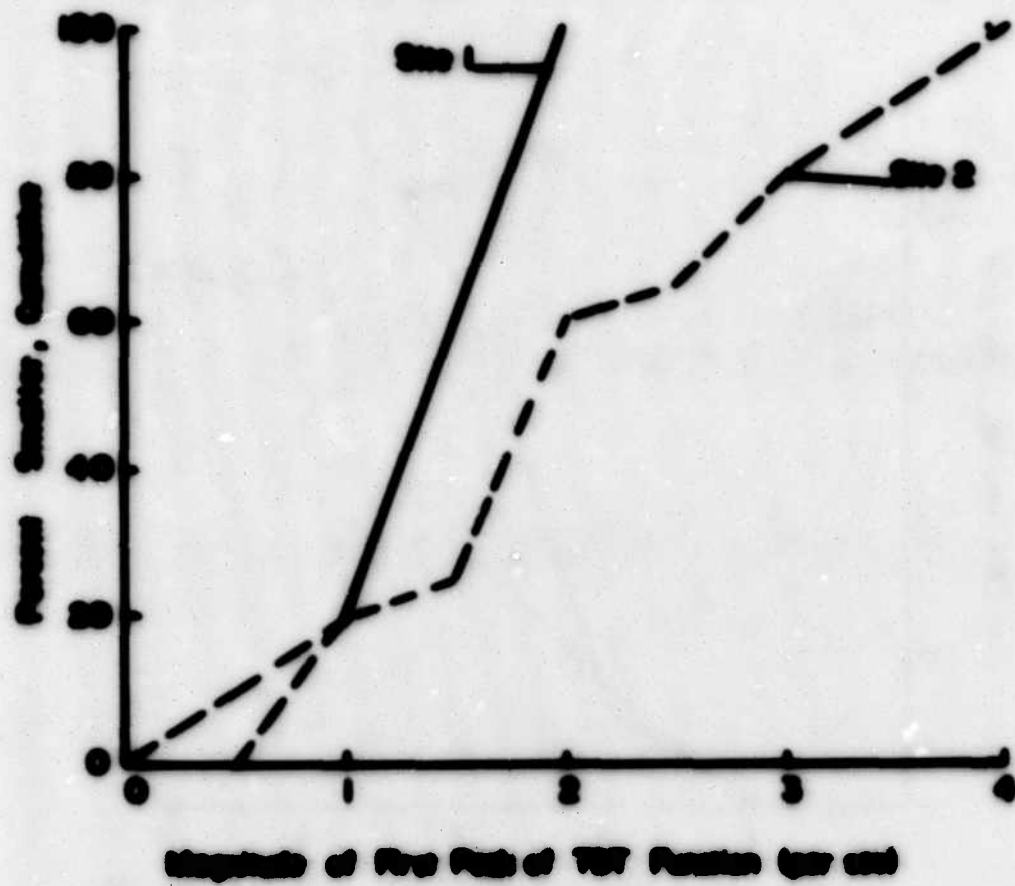


Figure 46. Comparison of The Peaks of The Transfer Function: Eglin  
AFB March 1956

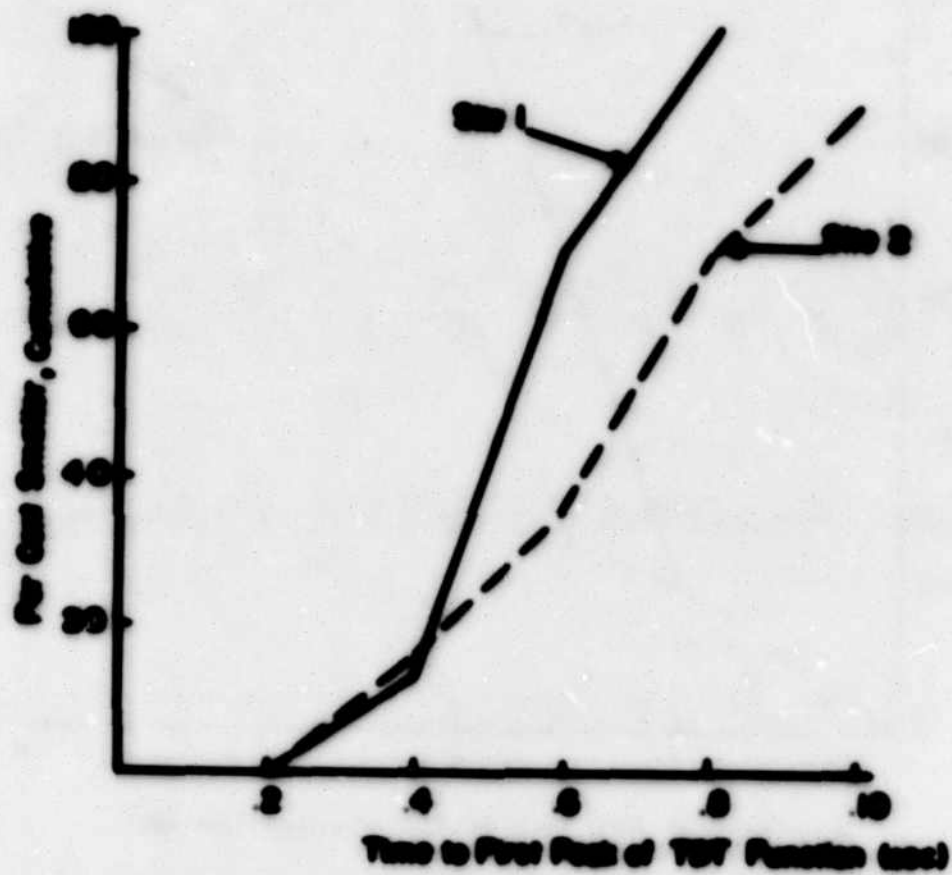


Figure 40. Comparison of Time to First Peak of TWT Function: Eglin AFB, March 1976

TABLE 3. PARAMETERS OF THE CHARGED PARTICLES. BELLS AND. SERIES 2076. SERIES 2

Station	$h \times 10^6$ 20/70	$e \times 10^6$ 20-000/70	$m \times 10^6$ charge	Position	$h \times 10^6$ 20/70	$e \times 10^6$ 20-000/70	$m \times 10^6$ charge	Position	$h \times 10^6$ 20/70	$e \times 10^6$ 20-000/70	$m \times 10^6$ charge
A1	3.405	5.000	9.543	B1	3.051	0.309	2.473	C1	3.003	2.300	1.974
A2	3.744	0.400	330.0	B2	2.600	3.307	7.006	C2	3.604	4.707	5.002
	4.366	2.330	4.907		3.007	2.027	1.040		4.346	20.400	0.300
	3.000	3.400	0.500		4.004	3.437	0.000		-	-	-
A3	4.092	3.924	6.496	B3	2.002	3.300	2.070	C3	4.007	12.973	12.700
	2.732	2.750	3.000		2.363	3.304	4.004		6.000	0.000	20.000
A4	3.094	5.000	20.700	B4	3.706	4.000	5.300	C4	4.000	6.373	7.553
A5	-	-	-	B5	2.006	3.007	5.000	C5	5.636	5.660	12.700
	4.626	3.000	9.000		3.003	2.606	4.500		3.902	5.066	12.770
	4.670	2.000	0.300		3.700	3.004	7.007		3.942	5.075	7.347

TABLE 6. PARAMETERS OF THE TRANSMISSION FUNCTIONS, JULY 1970, MONTH 1976, SERIES 2

Station	$h = 2d^0$ 20/70	$c = 2d^0$ 20-cm/70	$h = 2d^0$ 20/70	$c = 2d^0$ 20-cm/70	Station	$h = 2d^0$ 20/70	$c = 2d^0$ 20-cm/70	$h = 2d^0$ 20/70	$c = 2d^0$ 20-cm/70	Station	$h = 2d^0$ 20/70	$c = 2d^0$ 20-cm/70	$h = 2d^0$ 20/70	$c = 2d^0$ 20-cm/70
A1	22.20	9.005	146.0	22	B1	13.46	20.00	42.00	C1	20.96	2.22	673.0		
A2	-	-	-	22	B2	24.94	13.06	33.95	C2	7.00	24.00	22.00		
A3	20.73	26.90	100.1	22	B3	11.5	24.06	20.0	C3	-	-	-		
A4	26.90	26.03	104.1	23	B4	13.1	24.90	07.9	C4	20.25	20.75	57.50		
A5	-	-	-	23	B5	15.02	24.06	06.25	C5	27.97	9.257	24.47		
	15.00	20.03	10.06	24	B6	22.00	27.33	20.00		-	-	-		
	0.00	20.90	45.63	24	B7	-	-	-		-	-	-		
	13.1	21.46	24.57	25	B8	22.00	27.00	06.00		0.000	30.00	79.90		
				25	B9	17.30	15.40	03.97		26.70	5.44	22.27		
						20.00	25.90	20.0		0.244	25.00	20.00		



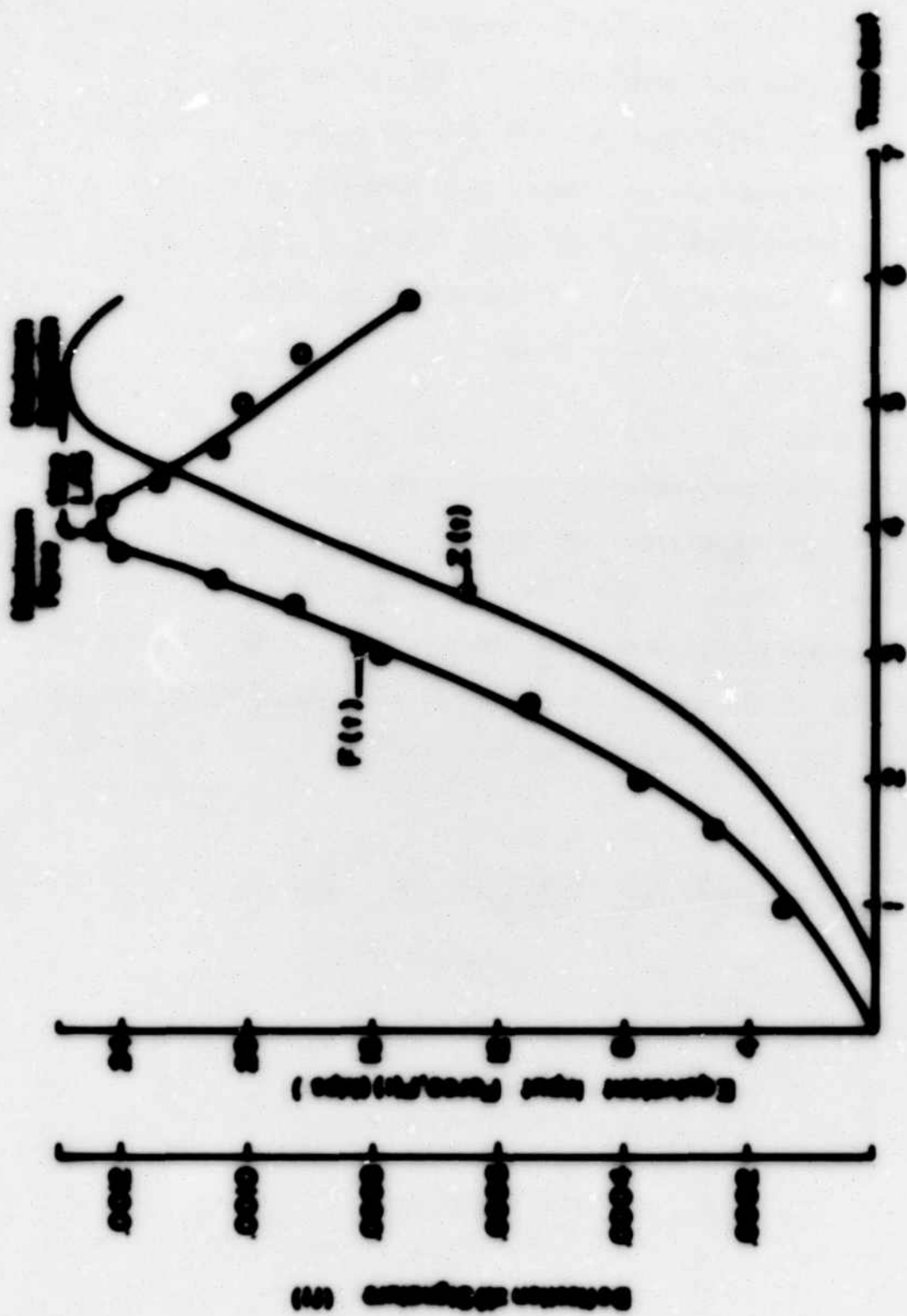


Figure 10. Temperature vs. Conversion (Typical)



2. Both sites are over critically damped (Figures 44 and 45).
3. Site 2 has consistently larger  $b$ ,  $c$ , and  $n$  parameters than Site 1 (Tables 5 and 6 and Figures 46 and 47).
4. Minor differences occur between the peaks of the transfer functions and the time to first peak for the two sites tested (Figures 48 and 49).
5. The maximum deflection lags behind the maximum input force by about 1.0 second (Figure 50).

### 6.3 Prediction

The methodology developed previously was used to predict the peak deflection response of the C-130 and the C-135 at Sites 2 and 3 (paragraph 3.2, Series B Field Investigation). The C-131 and Site 1 were the standard vehicle and site, respectively. Figure 51 shows a typical plot of the predicted and measured signature. Figure 52 shows a summary plot of the measured and predicted peak dynamic deflections.

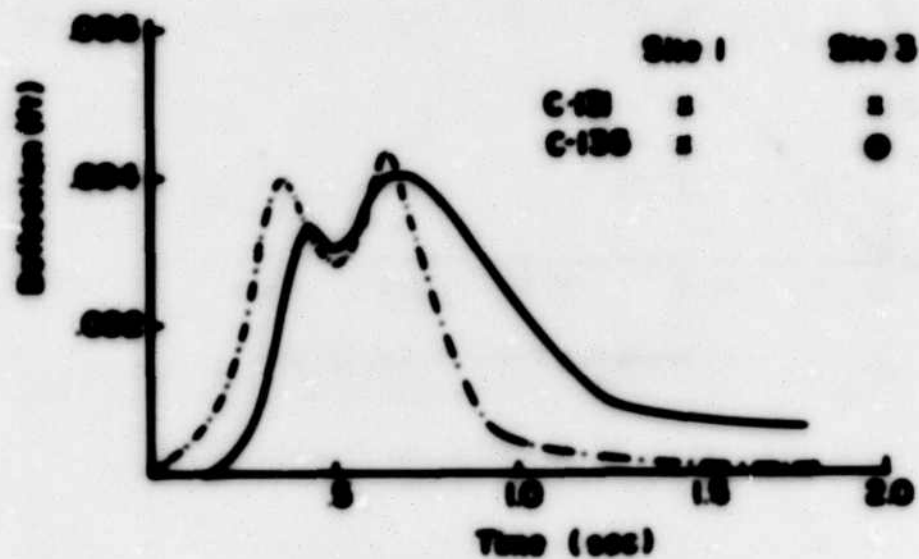
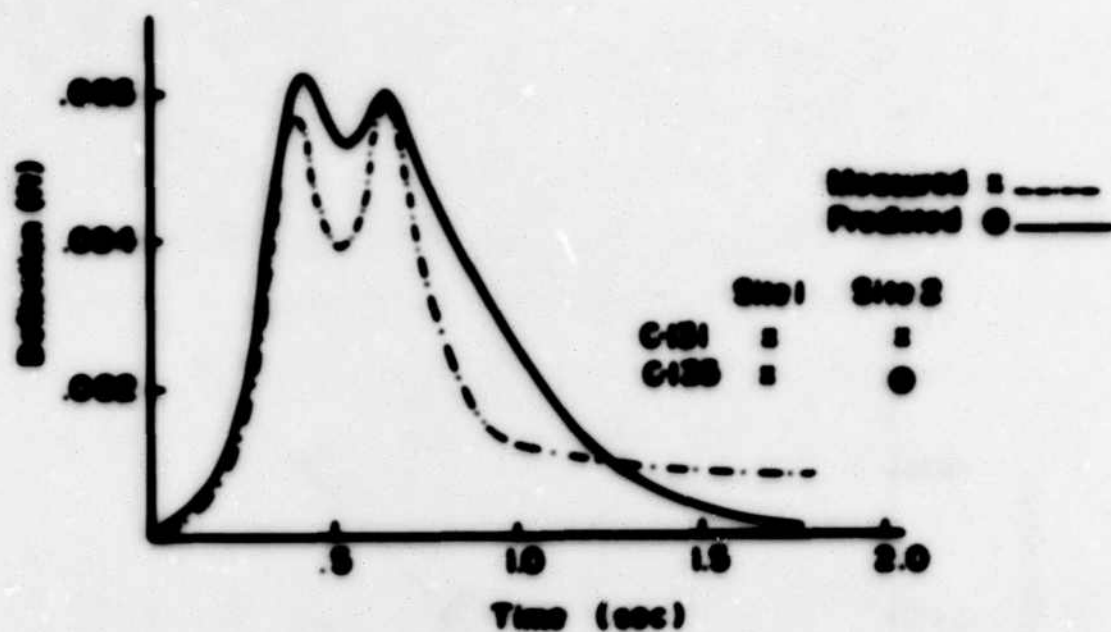
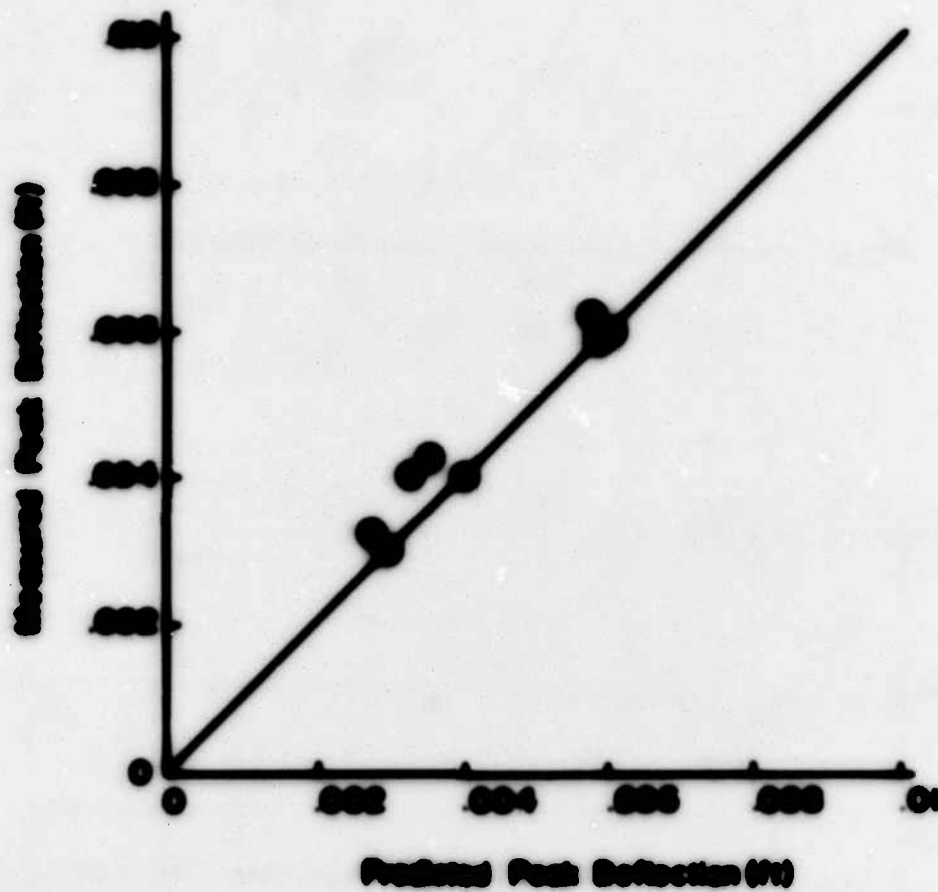


Figure 31. Typical Comparison Between Measured and Predicted Signature



**Figure 32. Comparison of Measured and Predicted Peak Reflections for Two Sites**

## **SECTION VII**

### **DISCUSSION**

The scope of this work includes equipment development, pavement evaluation, and prediction of pavement response. The significance of the results and the reliability and practical applicability of the equipment are discussed in this section.

#### **7.1 Equipment**

Several optical systems were considered during the initial stages of the development of this study. The first system used a laser as a coherent light source. The initial concept was that the laser would be positioned off the pavement and shoot at either the moving load vehicles or reflectors on the pavement surface. Changes in the position of the reflected light beam impinging on a fixed surface would indicate deflections.

It was next thought that, rather than having a laser fixed at a particular location off the pavement, a cantilever beam with its pivot outside the deflection basin would yield a more versatile and mobile system. The beam would support lasers which would shoot down on the pavement surface. Changes in the light beam reflected from the surface and impinging on collector lens on the beam would indicate pavement deflections. Several lasers would have to be purchased and mounted on a cantilever beam. The expense and bulkiness of the lasers prompted a search for a more compact, inexpensive coherent light source. Light emitting diodes on a cantilever beam were finally selected as the broadband noncontact system for measuring pavement deflections.

The deflection measuring equipment (LED beam) developed in this

work has a demonstrated capability of measuring pavement deflections on the order of 0.001 inch in a field environment. The companion LVDT beam<sup>11</sup> was found to be more rugged, reasonably simple to use, and very reliable. The breadboard LED system is somewhat more delicate. Special care had to be taken when in the moving mode, to ensure the safety of the lenses of the LEDs. Considerable problems also arose with the compatibility of the LED module and the magnetic tape recording system. These may be a result of the fact that the magnetic tape recording system was designed for use with another system, and thus the finer variations in the electronics which may not have affected the operation of the original design, may have been amplified when the system was used in conjunction with the LED modules. Although efforts were made to reduce these problems at Purdue University other still undiscovered incompatibilities between the LED sensor modules and the magnetic tape recording system may still exist.

Figure 53 shows a summary of measurement systems available today. It can be seen that actual vehicular loads are applied only in the procedures using the Benham beam, and the California and LaCroix deflectometer. It should be noted however that for these only the rebound deflections are measured. The total time response for one complete pass of a vehicle is not measured by any current device excepting those reported in this study. Under normal operating conditions a vehicle passes over a pavement without pause. This situation is very different from the conditions modeled by the Benham beam or the California or LaCroix deflectometers. For

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<sup>11</sup> Developed under contract with the Federal Highway Administration.



these the testing procedure starts at a minimum deflection under static loading. The vehicle then moves away and the residual deflection is recorded. The complete load cycle is not recorded by this stopping and starting procedure even though an actual vehicle is used.

Vibratory techniques also model a situation which is not representative of prototype vehicular loading on a pavement-subgrade system. The procedure for conducting vibratory tests generally consists of preloading a pavement-subgrade system by applying a static preload to the pavement surface through a plate of a specified size. At a certain preload level the steady state vibratory load is then applied at a designated frequency. Pavement deflection or a certain aspect thereof is then measured. There are significant differences between this procedure and the prototype loading of a pavement-subgrade system. First, a vehicle does not apply a static preload to the pavement-subgrade system. As previously mentioned, vehicular loading under normal operating conditions is applied to the system without pause. Second, a steady state vibratory force applied vertically dissipates approximately 67 percent of its total energy as Raleigh waves, 26 percent as shear waves and 7 percent as compression waves (Reference 39). The bulk (67 percent) of the energy is therefore dissipated by generating surface disturbances at distances in excess of 20 feet from the vibratory load as evidenced by ground motion at these distances. Prototype loading, however, generally dissipates its energy at distances of less than 5 feet. For the F-4 aircraft the surface effect of the prototype load only extended between 4 to 5 feet from the wheel.

Impact and quasi-static loading likewise do not model prototype



vehicular loading. The time of impact loading is extremely small compared with the time a pavement section actually feels vehicular loads. On the other hand for quasi-static loading, the time of loading is very large compared with that of prototype vehicular loading. In addition, for impact loading, a major portion of the input energy is used to generate surface disturbances similar to steady state vibratory loading. Prototype loading, however, generates little lateral surface disturbances but effects of prototype surface loading are felt at depths of greater than 10 feet (Reference 60). Another important aspect of prototype loadings will be illustrated by an actual example.

During the Wash field investigation a request was made by the Air Force officials at Eglin AFB that a runway overrun area be evaluated to determine whether it was adequate for use by F-4 aircraft. Figure 34(a) shows the area before prototype loading. Figure 34(b) shows the section after the first passage of the F-4 load cart. The test vehicle run through the pavement. It is doubtful that any available steady state vibratory loading testing apparatus (that dissipates a large measure of its energy as Raleigh waves) would have demonstrated the discovered inadequacy. The significance of this experience may be summarized as follows: An evaluation scheme that uses prototype loading in conjunction with nondestructive measurements of pavement-subgrade response provides, not only measurements of its response, but more importantly a test of necessity.

The speed of operation or the number of tests per day shown in Figure 33 indicates results vary from very slow to 3000 per day. The literature (Reference 23), however, shows the upper limit to be overly





(a) Before



(b) After

Figure 34. Runway Overrun Test - Eglin AFB: March 1976

optimistic. On the other hand, the operational speed of the broadband LUT and LED systems are indisputable.

In June 1976, both the LUT and the LED systems were used at Eglin Air Force Base to help investigate the difference between loaded and unloaded profiles. Measurements were made on 2,000 feet of runway using both systems. The LUT stationary beam-moving load operation was used to measure the system response at 100-foot intervals. The LED beam was fixed to the P-4 load cart and was used in conjunction with the LUT measurements to provide an estimate of deflections between the 100-foot LUT stations. The average time for setup, including manually moving the LUT beam between locations and positioning the load cart, was 7 to 10 minutes. In addition to the 2000 feet of runway, the LED system mounted to the load cart was used to test 1 1/4 miles of runway. The runway testing took less than 1 hour after initial setup.

It is important to note also that in the stationary beam-moving load mode the LED and LUT beams both provide the complete deflection-time response of a pavement-subgrade due to prototype loading, that is, the entire dynamic deflection basin is obtained. No other instrumentation system currently available has demonstrated this capability. Furthermore, the LED system does it without making mechanical contact with the pavement surface.

## **7.2 Evaluation**

The evaluation procedure consists of measuring pavement deflections due to prototype loadings. From these deflections the signature and parameters of the maximum lateral dynamic deflection profile and the transfer function are obtained using the computer program detailed in

Appendix C. The parameters of the maximum lateral dynamic deflection profile and the transfer function are then related to performance.

### 7.2.1 Concrete Model in Computer Program

The developed computer program determines the  $m$ ,  $c$ , and  $k$  parameters of the equation that describes the behavior of the hypothesized model of vehicle-pavement-subgrade interaction. The equation of the model,

$$m\ddot{s}(t) + c\dot{s}(t) + ks(t) = F(t)$$

describes at best an approximation to physical reality. The lumped parameters represent average measures of the actual inertial ( $m$ ), damping ( $c$ ), and stiffness ( $k$ ) characteristics of the real system.  $F(t)$  represents an input force at time  $t$ , and  $s(t)$ ,  $\dot{s}(t)$ , and  $\ddot{s}(t)$  represent the signature and its first and second derivatives.

Research (Reference 61) has shown that when a vehicle is in motion,  $F(t)$  may have instantaneous values varying from 30 percent greater to 20 percent less than the static wheel load. The wide range is caused by many factors including both pavement and vehicle characteristics. The maximum  $F(t)$  of 25 kips used to establish the 300-pound criterion (see pages      through      ) in the computer program is then simply a convenient approximation to actual maximum values which may range from 12.5 kips to 37.5 kips. The 300-pound criterion then serves as a normalizing function and in effect has little physical significance, except in the sense that 25 kips is close to the static wheel load.

The lumped parameters of the transfer function represent measures of the inertial ( $m$ ), stiffness ( $k$ ), and damping ( $c$ ) characteristics of

the pavement-subgrade system. Local<sup>12</sup> characteristics may vary significantly; however, when the overall interaction mechanism is translated to surface deflections, local variations lose their significance.

In the computer program, FEMFEM parameters of the transfer function were obtained using an iteration-interpolation procedure detailed in paragraph 1.2.2. Conditions at time corresponding to the maximum deflection, the crossing point, and the point of inflection had to be satisfied. Two criteria were used. The first criterion was that the input load obtained by implicit convolution had to be between 24,500 and 25,500 pounds. The second and final criterion was that the  $c$  value satisfied the conditions at the crossing point and simultaneously satisfied conditions at the point of inflection. All forces were obtained by implicit convolution of the signature  $s(t)$  and the transfer function using a series of trial values of  $h$ ,  $c$ , and  $n$ .

With reference to Figure 55, in concept the first criterion ensures that the maximum force lies within the crosshatched area. The second criterion ensures that the convolution and Newtonian solutions are very close. For example, consider the curves labelled A, B, D, C, and E in Figure 55. Suppose that the curve labelled E is the true but unknown (Newtonian) solution. Curve B satisfies neither criterion as (1) its peak value is outside the specified (shaded) band width, and (2) the computed  $c$ -value would be too large. The failure of the latter criterion is demonstrated when the force  $P(t_1)$  (obtained by convolution)

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<sup>12</sup>Local, as used here refers to dimensions of the size of a typical laboratory specimen.

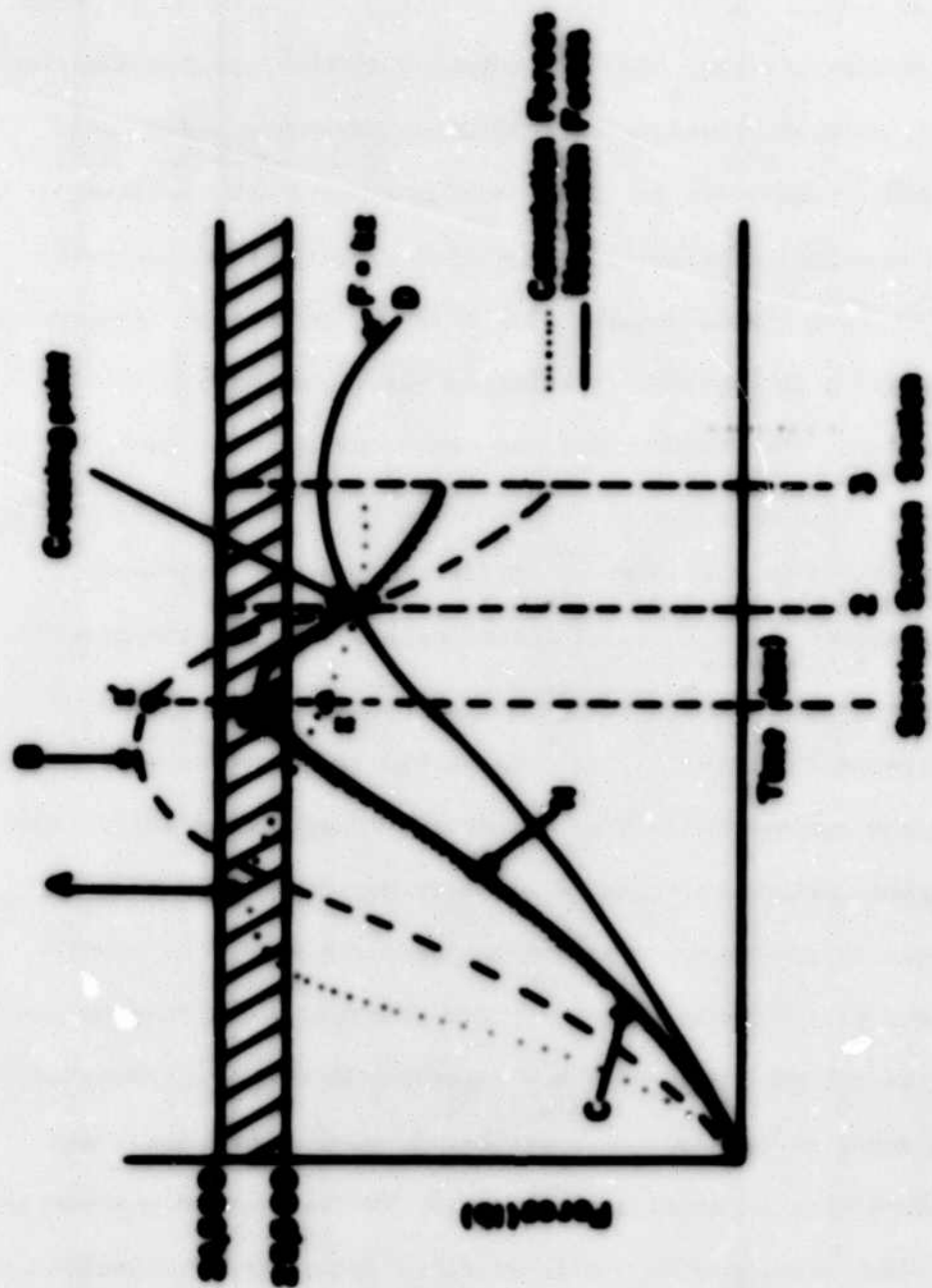


Figure 10. Graph showing the concept of the Strain Rate in Polymer Degradation

of  $X'$  (Figure 36) is used instead of  $R$  to calculate the  $c$  parameter at the point of inflection (section (1), Figure 36), using equation (17a). Curve A satisfies the 500-pound criterion but does not satisfy the  $c$ -parameter criterion, since the value of the force  $X$  at the point of inflection is less than  $R$ . Substitution of  $X$  for  $F(t)$  in equation (17a) would yield a value of  $c$  which would be less than the desired value. Curve C would satisfy both criteria. For this curve the convolution and Newtonian solutions are essentially the same. The fact that the two solutions are the same ensures that a standard point of convergence is used for all calculations. It does not mean that the  $h$ ,  $c$ , and  $n$  parameters are absolute values since as previously cited, the parameters are average values, and are influenced by the approximation  $[F(t)]$  to reality inherent in the hypothesized model.

Since measurements could not be made exactly at the edge of the tire print, it was necessary to calculate the signature (the deflection at the edge of the tire print) using the characteristics of the lateral dynamic deflection profile. It was assumed, and subsequently verified (Figures 35 and 36), that the deflections under the wheel and at its edge are essentially equal. In calculating the signature the three parameters  $A_{peak}$ ,  $\delta_{peak}$ , and  $\tau_{peak}$  were used to provide a scaling of the lateral attenuation of the peak deflections with time. Figure 36 shows a comparison of a typical measured and calculated signature. The signature (curve A) was measured as the F-4 passed over a gage embedded in the pavement. The other embedded gages measured points on the deflection basin which provided the inputs to the calculations. The closest gage was 18 inches from the center of the load wheel. The difference between the maximum calculated curve (B)



and measured deflections is about 3 percent. Since all field measurements analyzed in this work were made with the LVDT beam at distances closer than 18 inches from the edge of the tire, the correspondence between the calculated and the measured signatures in Figure 36 indicates the upper bound of the differences between calculated and measured signature. Using linear interpolation, the dotted curve (C) in Figure 36 corresponds more closely to typical calculated signatures used in the data analyzed herein since the LVDT beam permitted measurements to be made as close as 3 inches from the edge of the tire print.

### 7.2.2 Parameters of the Maximum Lateral Deflection Profile

Pavement deflection has been used as an indicator of the support condition of a pavement-subgrade system for some time. Methods of evaluation have been developed that are based on (a) magnitude of deflection (Reference 62), (b) bending index (Reference 63), (c) radius of curvature (Reference 23), and (d) the "slope of deflection" (Reference 64). These methods in general have used static or quasi-static loading. For the reasons discussed previously in paragraph 7.1, these deflection measurements are not true indicators of the dynamic response of a pavement-subgrade system subject to vehicular loads.

The dynamic lateral deflection profile defined by equation 2 has three parameters  $\Delta_{peak}$ ,  $\delta_{peak}$ , and  $r_{peak}$  which together account for both the magnitude and the curvature of the lateral deflection basin. Since the deflection measurements were made during a nonstop passage of the F-4 load cart in front of the LVDT beam, the three parameters are representative of the actual maximum dynamic lateral deflection basin due to prototype loads.

**Figure 26. Comparison of Signatures**



The results presented in paragraph 6.2.1 showed some variation in the parameters  $\Delta_{\text{peak}}$ ,  $\delta_{\text{peak}}$ ,  $\tau_{\text{peak}}$  at each site, and there were distinct differences between Sites 1 and 2. In order to better characterize the two sites and give due consideration to the parameter variability at the sites, plots of cumulative percent smaller versus each parameter were prepared from the results in paragraph 6.2.1. Figures 57 through 59 show these plots. The distinct differences between the two sites are displayed as a shift of the individual site characterization plots.

The U. S. Air Force in recognition of the structural inadequacy of Site 1<sup>13</sup> uses the area as a parking area. Site 2 on the other hand is an in-service taxiway. If the lower 10 percent of the Site 2 parameters is arbitrarily selected as the line denoting failure, criterion based on the correlation of parameters with performance is established. This is shown in Figures 57 through 59. The lower 10 percent as used here means that 10 percent of the values do not meet the criterion. Thus, in Figure 59, the line denoting failure intersects the Site 2 cumulative percent smaller curve at the 10 percent smaller value whereas in Figures 57 and 58, the 90 percent smaller value of the cumulative percent smaller plot is intersected by the criterion line.

### 7.2.3 Parameters of the Transfer Function

The results given in paragraph 6.2.2 showed that there is some variation in the parameters  $k$ ,  $c$ , and  $n$  of the transfer function over

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<sup>13</sup>See Appendix B, Figure B-1(a)

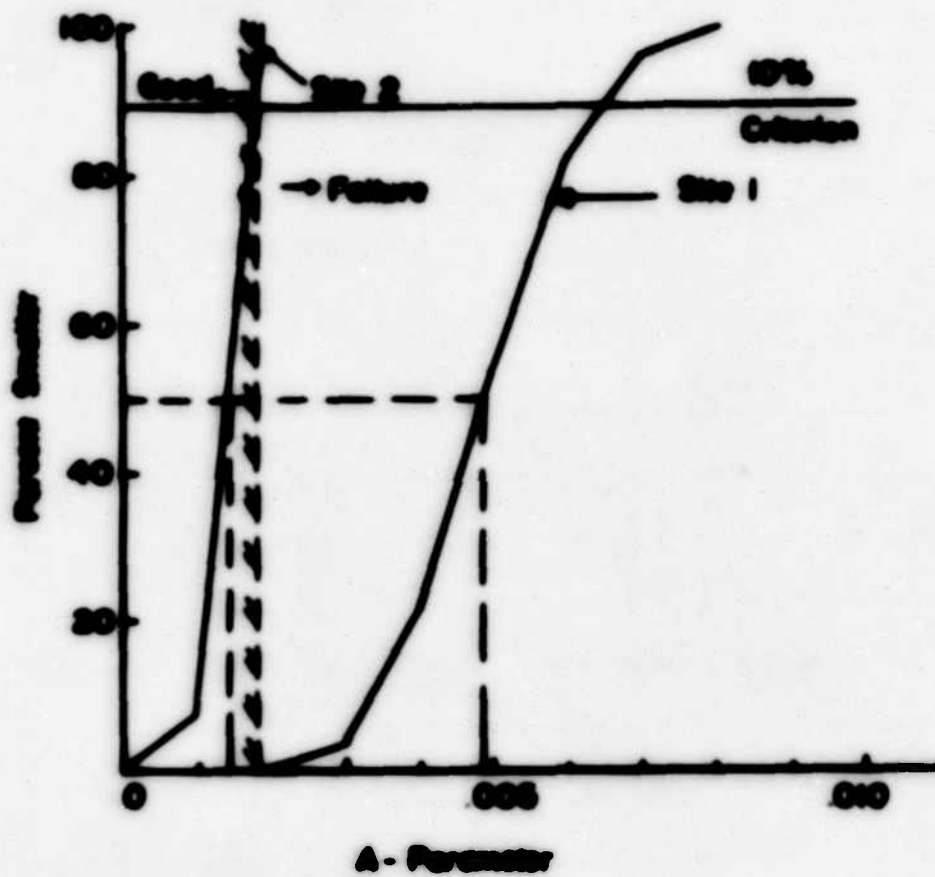


Figure 57. Comparison of A Parameters: Eglin AFB March 1976

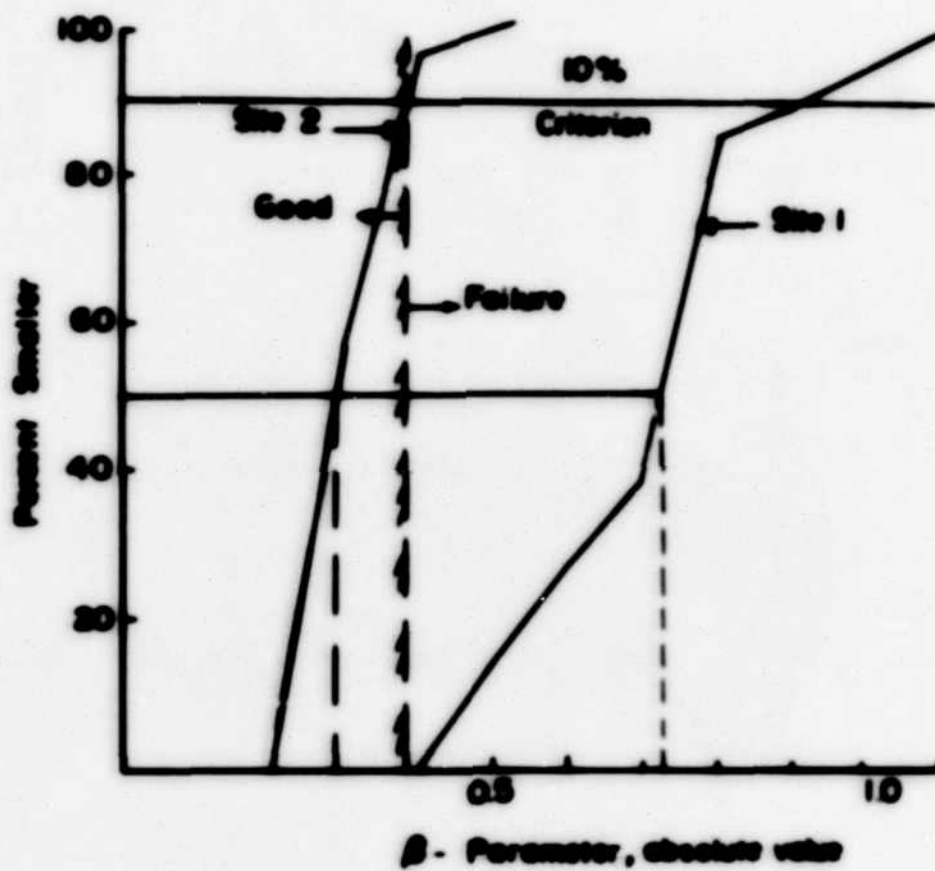


Figure 56. Comparison of the  $\beta$ -Parameters: Eglin AFB, March 1976

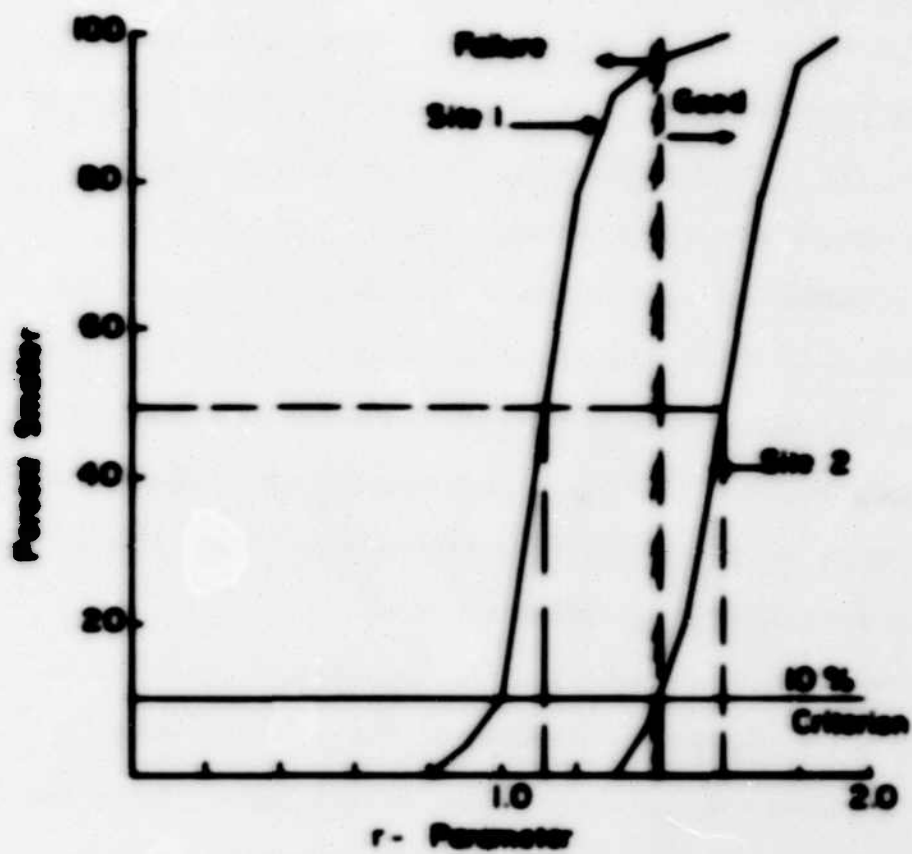


Figure 39. Comparison of r Parameters: Eglin AFB March 1976

each of the two sites. Plots of cumulative percent smaller versus each parameter have been prepared for each site. Figures 60 through 62 show these plots. It can be seen that Site 1 exhibits more uniformity and considerably smaller values of all three parameters than Site 2. With reference to Figure 60 the fact that the entire curve of "cumulative percent smaller" is shifted towards higher stiffnesses for Site 2 indicates that the stiffnesses determined in the evaluation procedure are not local hard spots, but represent the variability in the stiffness characteristics of the area tested.

If the arbitrary 10 percent criterion shown in Figures 57 through 59, is applied to each of the parameters  $k$ ,  $c$ , and  $n$  of the transfer function, a criterion based on performance can be had. The line denoting failure is shown on Figures 60 through 62. The performance based criteria shown in Figures 60 through 62 can then be used in the same manner as was presented in the discussion of the parameters of the various lateral dynamic deflection basin.

It is interesting to compare the  $k$  parameters with stiffness as determined in a 1973 evaluation (Reference 20) by the Air Force, in which an F-4 aircraft was used as the load vehicle and the Buchelman beam was used to measure rebound deflections. Figure 63 shows the locations where relative stiffnesses were determined. Figure 64 shows a histogram on the relative stiffnesses calculated by their procedure. Figure 64 also shows the sum  $k$  parameters for Sites 1 and 2 as calculated by the procedures developed in this research effort. Site 1 is shown to have a smaller sum stiffness than all the sections evaluated, while Site 2 is in the range that occurs with about 9

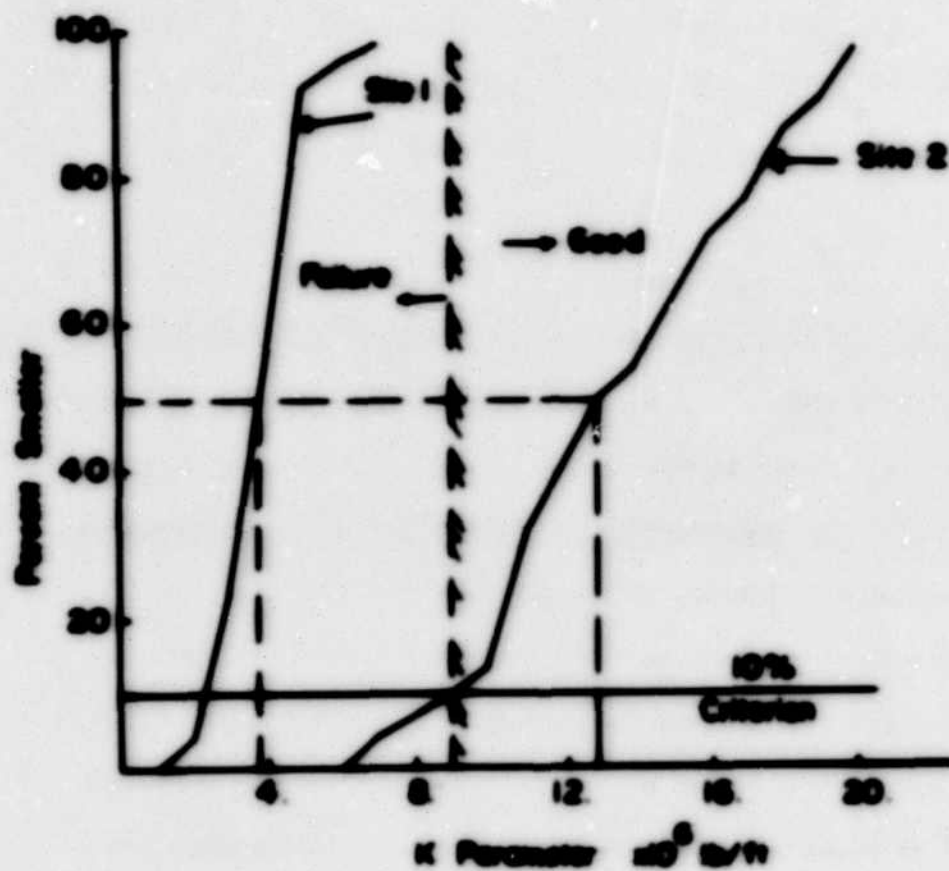


Figure 60. Comparison of Equivalent k Parameters: Eglin AFB  
March 1976

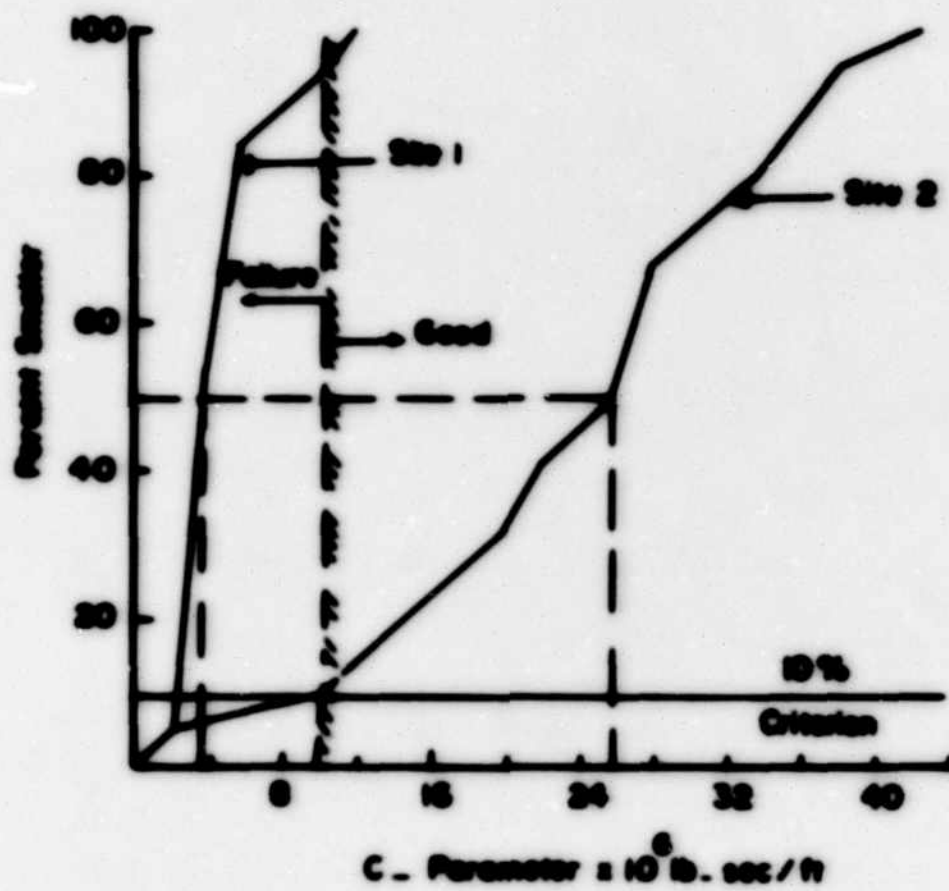


Figure 61. Comparison of Equivalent c Parameters: Eglin AFB  
March 1976

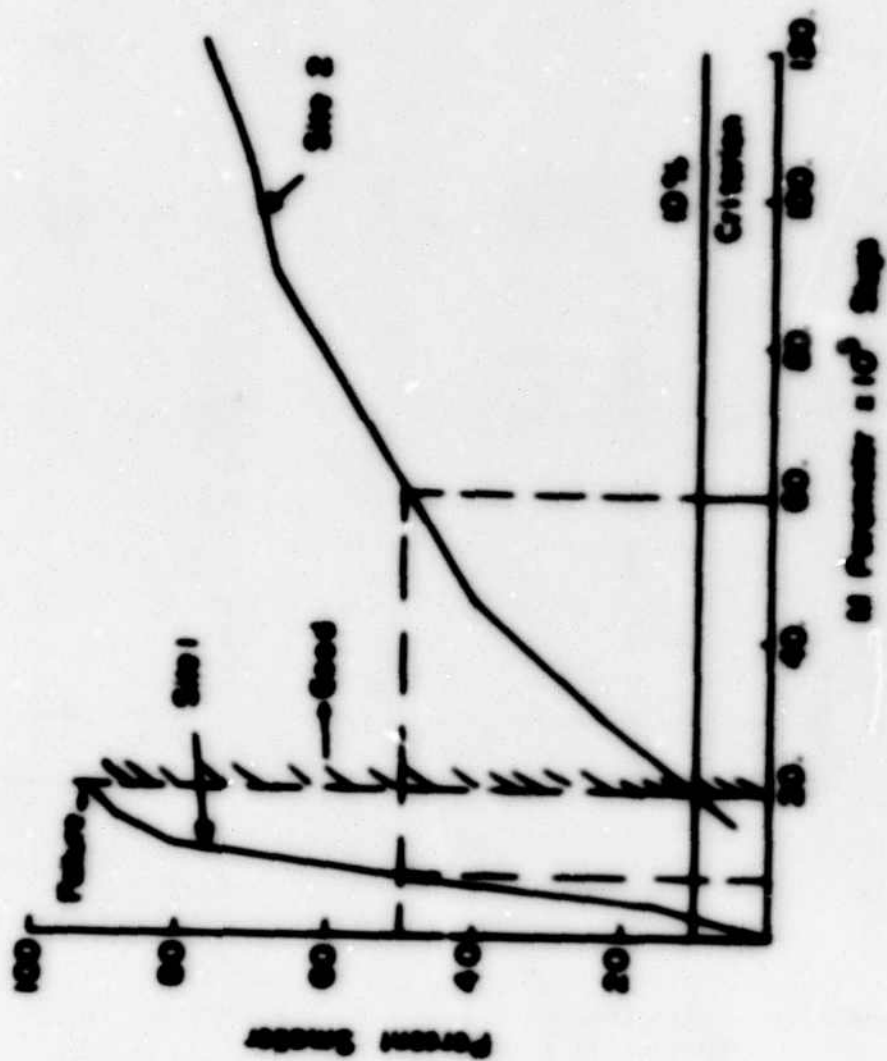


Figure 6.2. Comparison of the Equivalent n Parameters: Right AFV, March 1976





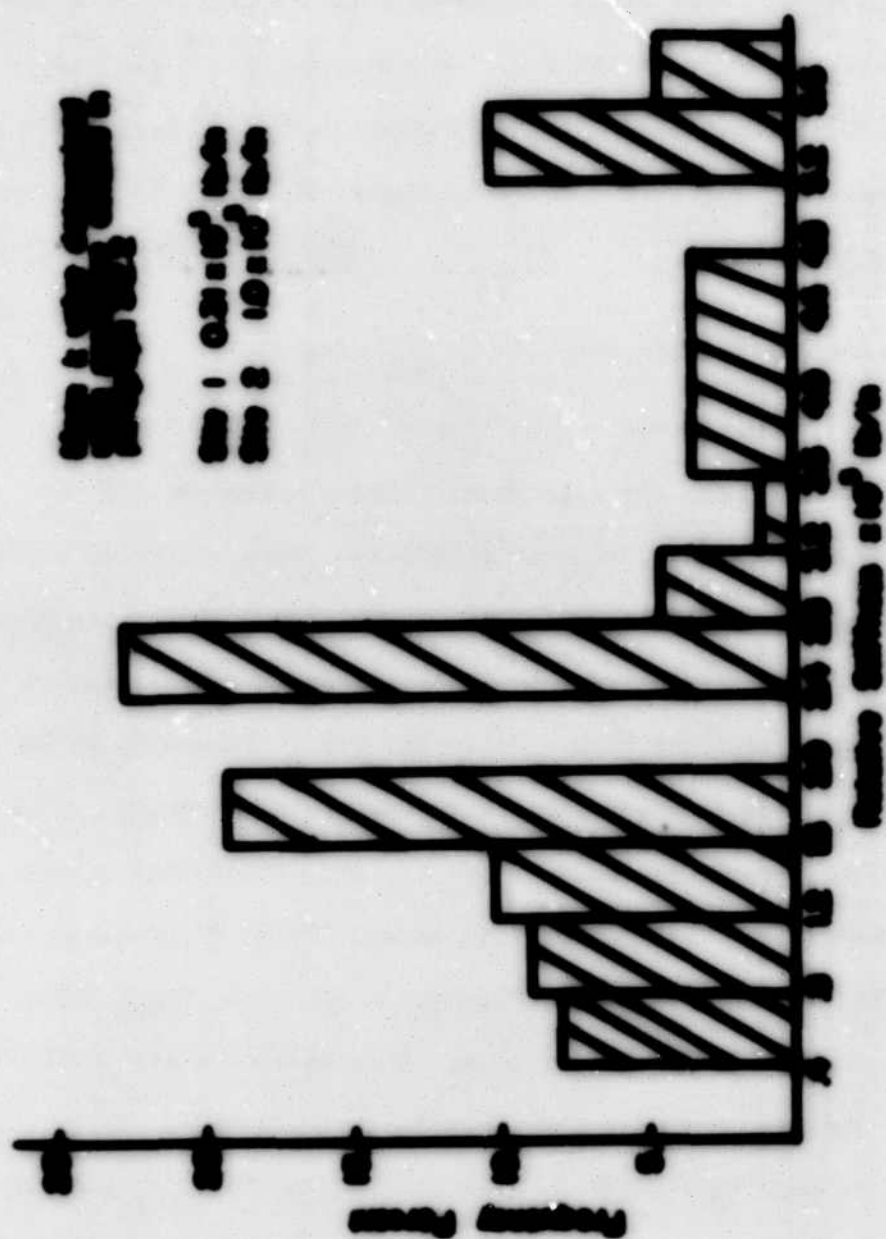


Figure 64. Histogram of Relative Stiffness (Based on AFSC Report)

percent frequency.

It appears then that field performance and comparison of stiffness both substantiate the lower limit of the  $k$  parameter. A reasonable lower bound of an acceptable  $k$  value of about  $9.0 \times 10^6$  lb/ft (750 kips/in) is suggested by the Site 2 curve in Figure 60. This is the lower 10 percent value.

#### 7.2.4 Relationship between the $k$ and $A_{\text{peak}}$ parameters

The  $A_{\text{peak}}$  parameter defined in this study is basically the maximum deflection under the load wheel. The  $k$  parameter, on the other hand, represents an equivalent stiffness. This stiffness reflects the complicated unknown interaction of all the materials in the zone of influence of the wheel load. The  $k$  parameter is thus a measure of the stiffness resulting from this interaction. Figure 65 shows a plot of the  $A_{\text{peak}}$  and corresponding  $k$  parameters from the two sites as given in the results in Tables 5 and 6. The dashed line represents a limiting envelope. There appears to be two linear sections to this envelope. If the straight line portions are extended, the  $A$  and  $k$  parameters corresponding to their point of intersection are 0.0026 ft (0.0312 in) and  $6 \times 10^6$  lb/ft (500 kips/in) respectively. It is interesting to note that the Site 2 (active taxiway) ( $k$ ,  $A$ ) parameters fall below the line PQ (0.0312 in) and the Site 1 (parking area) ( $k$ ,  $A$ ) parameters lie above the PQ line. It is also interesting to note where the  $k$  coordinate of this point (P) line, if plotted on Figure 66. The curves in Figure 66 were developed by the Corps of Engineers using vibratory techniques and correlations with actual

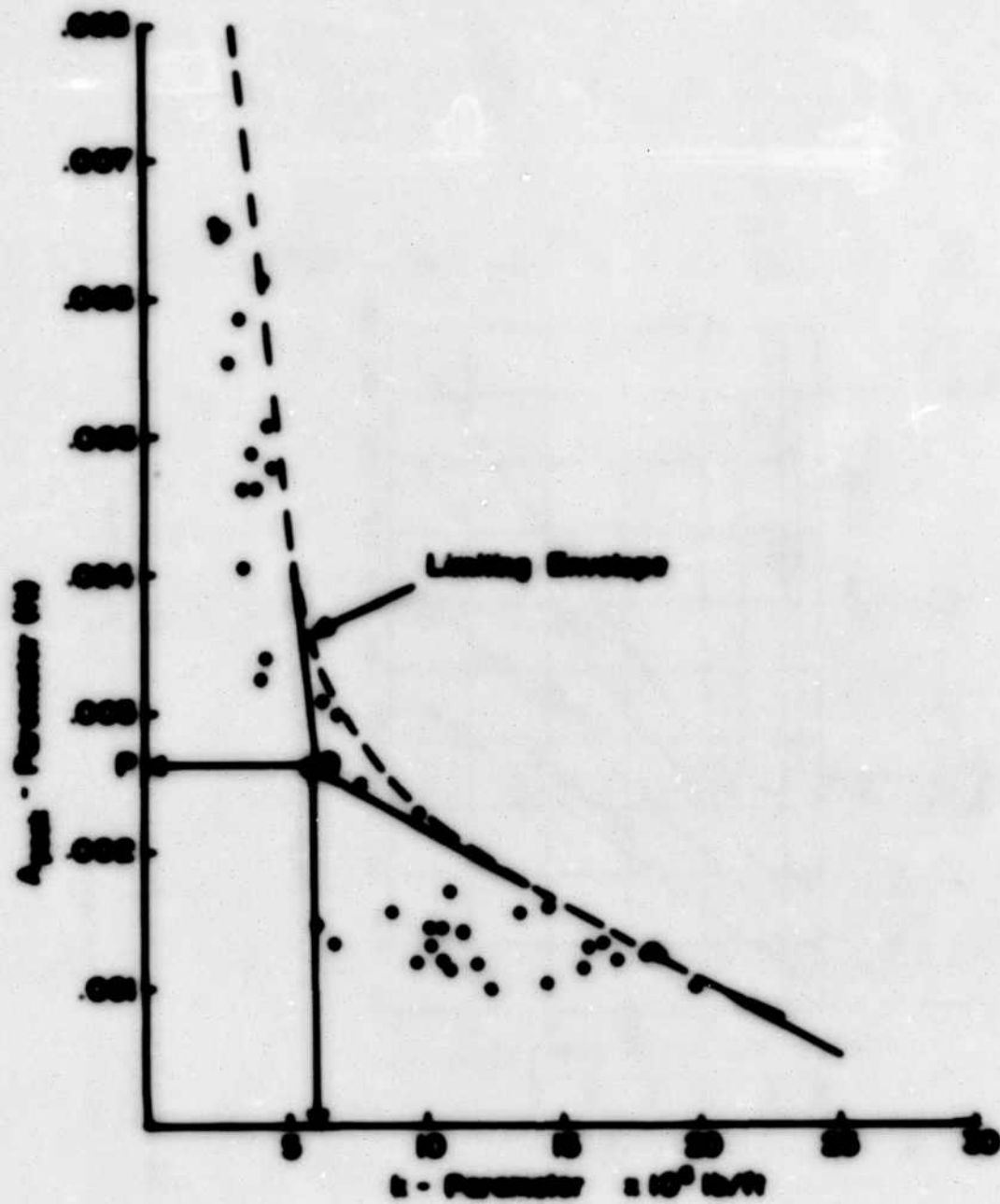


Figure 65. Relationship Between  $A_{peak}$  and  $k$  Parameters

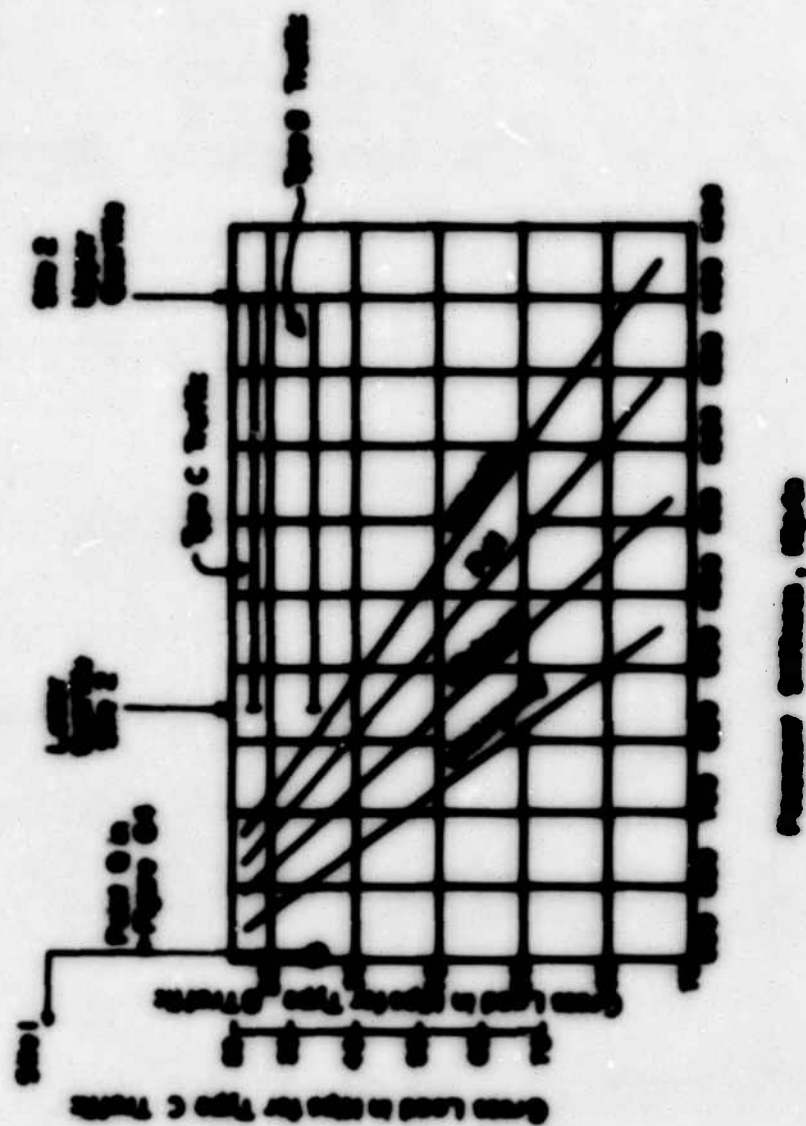


Figure 66. Representative Evaluation Curves for Flexible  
 Footings. Single Wheel Load, 100 lb. after  
 1000 (Reference 10)

aircraft loads. Since the F-4 aircraft gear is a single wheel of contact area 108 in.<sup>2</sup> loaded to about 25 kips (Reference 24), the  $h$  value of the point  $q$  (Figure 63) can be plotted directly on Figure 66 for C type or B type traffic. Figure 66 also shows  $h$ -parameters corresponding to the lower and upper quartile values at Site 2 (active runway). Site 2 lies above the capacity line and Site 1 lies below the emergency line. This estimation appears to confirm the known status of Sites 1 and 2.

The limiting envelope in Figure 63, therefore, appears to provide an additional evaluation tool. Since deflections alone are measured, the limiting  $h$  values can be estimated from Figure 63, and compared with available correlations as shown, to estimate load rating.

### 7.2.3 Comments Related to Estimating $h$ , $c$ and $a$ for F-4 Landing

Figure 30 shows the typical relationship between the input force  $P(t)$  and the output  $s(t)$ . Figure 67 shows the frequency characteristics of  $P(t)$  normalized by the maximum recorded wheel load (25 kips) at three sections corresponding to sections 1, 2 and 3 of Figure 7. Sixty data sets were used to develop the frequency curves.

With reference to Figure 67, at the point of inflection (section 1), the normalized force ratio has a mean value of approximately 0.9. This suggests that the maximum applied force occurs at a time close to maximum pavement velocity. Similarly at maximum deflection (section 3), 0.5 of the maximum force is the mean value of normalized force ratio. This indicates that at the time the measured deflection is a minimum the wheel has already passed the point under consideration. At the



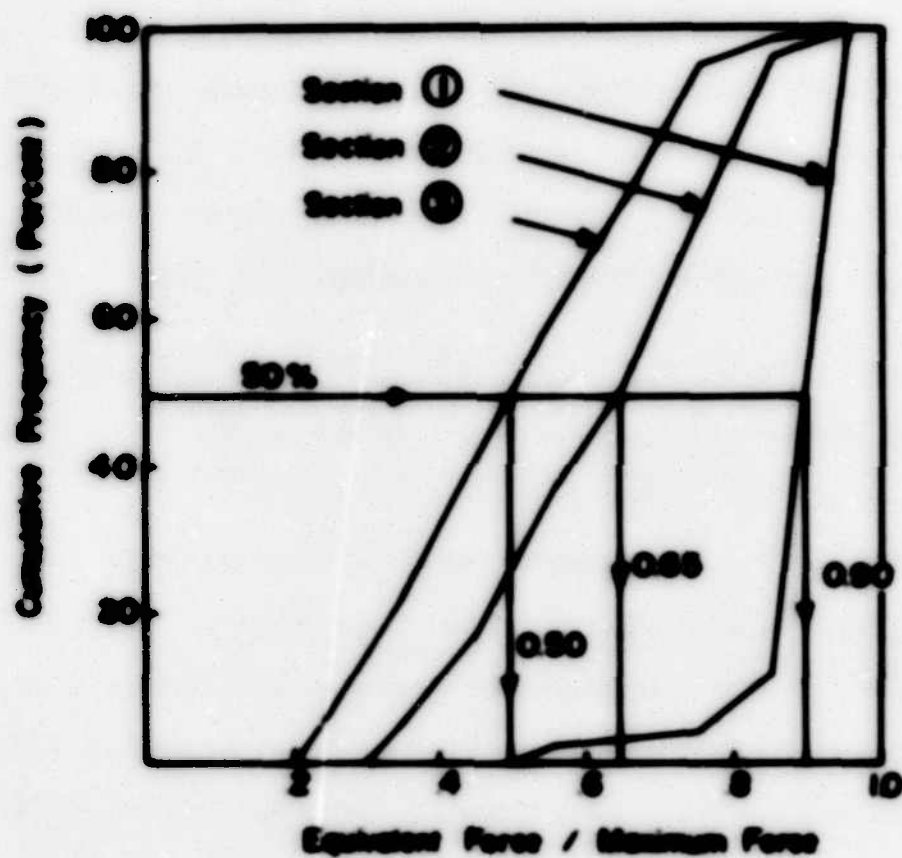


Figure 67. Frequency Characteristics of Forces at the Point of Inflection, Crossing Point and Maximum Deflection

crossing point (section 2). approximately 0.65 of the maximum load is the mean value of the force ratio.

Figure 66 shows the frequency characteristic of the time normalized by the time to peak deflection corresponding to the point of inflection (section 1) and the crossing point (section 2) respectively. At the 30 percent level the normalized time ratio is seen to be 0.72 and 0.90 for the point of inflection (section 1) and the crossing point (section 2) respectively.

Figures 67 and 68 suggest a simplified approximate method for determining the transfer function parameters from the deflection-time history of one pass of a vehicle. In order to determine  $k$  from the signature  $s(t)$ , the deflection  $s(t_2)$ <sup>14</sup> is found at  $0.9 T_p$ , where  $T_p$  is the time to the peak deflection (Figure 66). The force  $F(t_2)$  applied at the time  $(t_2)$  is approximately  $0.65 P_{max}$  (Figure 67) where  $P_{max}$  is 25 kips for the F-4 landing. As was noted in paragraph 3.2.2 at the crossing point.

$$F(t_2) = k \cdot s(t_2)$$

hence, using the approximate values,

$$k = \frac{F(t_2)}{s(t_2)} = \frac{(0.65)(25000)}{s_{0.9 T_p}}$$

<sup>14</sup> For the sake of clarity, the subscript of "t", such as in  $t_2$ , will be retained to describe the corresponding section in Figures 67 and 68.



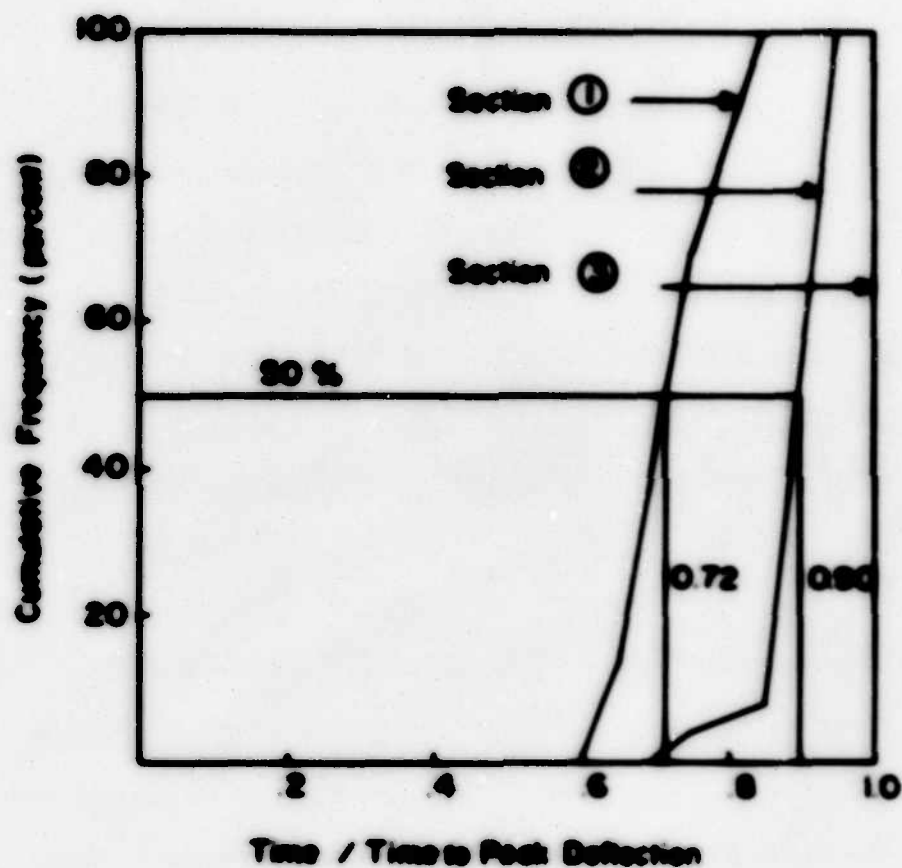


Figure 68. Frequency Characteristics of Time at the Point of Inflection, Crossing Point and Maximum Deflection

Since  $k$  is known, the  $c$  parameter can be obtained by applying the same reasoning to the point of inflection (section 1, Figure 67); namely,

$$c = [V(t_1) - ks(t_1)]/\dot{s}(t_1)$$

where  $V(t_1)$  is  $0.9 P_{max}$  (Figure 67) and  $s(t_1)$  and  $\dot{s}(t_1)$  are the deflection and numerical approximation of the velocity, respectively, at the time corresponding to  $0.72 T_p$  (Figure 68).

The parameter  $n$  can then be estimated using the equation for conditions at the crossing point, where

$$n = - \frac{c \pm \dot{s}(t_2)}{\ddot{s}(t_2)}$$

and  $\dot{s}(t_2)$  and  $\ddot{s}(t_2)$  are the numerical values for the velocity and acceleration at the time  $0.9 T_p$ .

The developed approximate procedure for estimating  $k$ ,  $c$  and  $n$  was examined with respect to 38 data sets from both Sites 1 and 2 at Eglin AFB<sup>15</sup>. The normalized forces at the crossing point and the point of inflection were taken to be 0.65 and 0.85<sup>16</sup>, respectively. The normalized times at the crossing point and the point of inflection were taken to be 0.72 and 0.9, respectively. The  $k$ ,  $c$  and  $n$  parameters obtained using the simplified procedure were then compared with their computer solutions. Correlation coefficients of 0.93, 0.93 and 0.90

<sup>15</sup> See Appendix B

<sup>16</sup> 0.9 was tried initially but 0.85 yielded  $c$  values which correlated more closely with the computer solutions.

were obtained from the linear least squares correlation study for the  $k$ ,  $c$  and  $m$  parameters, respectively. The advantage of the simplified procedure is that it allows reasonably reliable estimates to be made of parameters without the need of a digital computer.

#### 7.2.6 Estimating Reaction Parameters

The modulus of subgrade reaction ( $\bar{k}$ ) and CBR of the subgrade can be estimated from the  $A_{\text{peak}}$  parameter of the peak deflection profile.

Using the assumption of a Halpin model, Pieter and William (Reference 26) developed the following relation between the subgrade deflection  $W(x)$ , pressure on the subgrade ( $p$ ), modulus of subgrade reaction ( $\bar{k}$ ) and a shear stiffness parameter ( $CH$ ) as the distance from the edge of the loaded area ( $x$ ):

$$W(x) = -\frac{p}{2\bar{k}} \exp(-x/CH)$$

This expression is similar in form to equation (2),

$$z_{\text{max},j} = A_{\text{peak}} \exp(\beta_{\text{peak}} z_j^{r_{\text{peak}}})$$

which was found to describe the maximum lateral dynamic deflection profile. If it is assumed that the two relations correspond at their maximum values (for  $x = 0$ ), it follows that

$$A_{\text{peak}} = -\frac{p}{2\bar{k}}$$

Hence, this suggests that the modulus of subgrade reaction can be obtained as,

$$\bar{E} = \frac{P_{\text{max}}}{A_{\text{peak}}} \quad (23a)$$

Using a 1:1 simplifying assumption [cf. Veder (Reference 56)] to calculate the attenuation of the wheel load,  $P_{\text{max}}$ , through the pavement section of thickness  $D$ , the contact pressure,  $p$ , equals  $P_{\text{max}} / (3.64 + D)^2$ ; where 3.64 is the radius of the equivalent circular contact area due to the F-4 aircraft with tire pressure 250 psi and a  $P_{\text{max}}$  of 25,000 pounds. Substituting in equation (23a) gives

$$\bar{E} = \frac{P_{\text{max}}}{2.0(3.64 + D)^2 A_{\text{peak}}} \quad (23b)$$

CBR values can then be estimated using established correlations (Reference 65) between  $\bar{E}$  and CBR. One such correlation given by the Portland Cement Association (Reference 65) is shown in Figure 69.

Using equation (23b) and the maximum, median and minimum values of  $A_{\text{peak}}$  calculated at site 2, and a  $D$  of 17 inches,  $\bar{E}$  values of 323, 462 and 646 pounds per cubic inch were obtained. The same calculation for site 1 (with  $D = 9$  in) gave  $\bar{E}$  values of 237, 316 and 315. The correlation chart shown in Figure 69 gave the range of CBR values for site 2 from 28 to 73, and for site 1 from 18 to 32.

Moduli of subgrade reaction were not determined under asphaltic concrete pavement sections at Eglin Air Force Base by the Air Force Civil Engineering Center during the 1974 Survey (Reference 21): subgrade CBRs were obtained for these sections and these only at a few locations (about 10 in number). In the area of site 2, a CBR

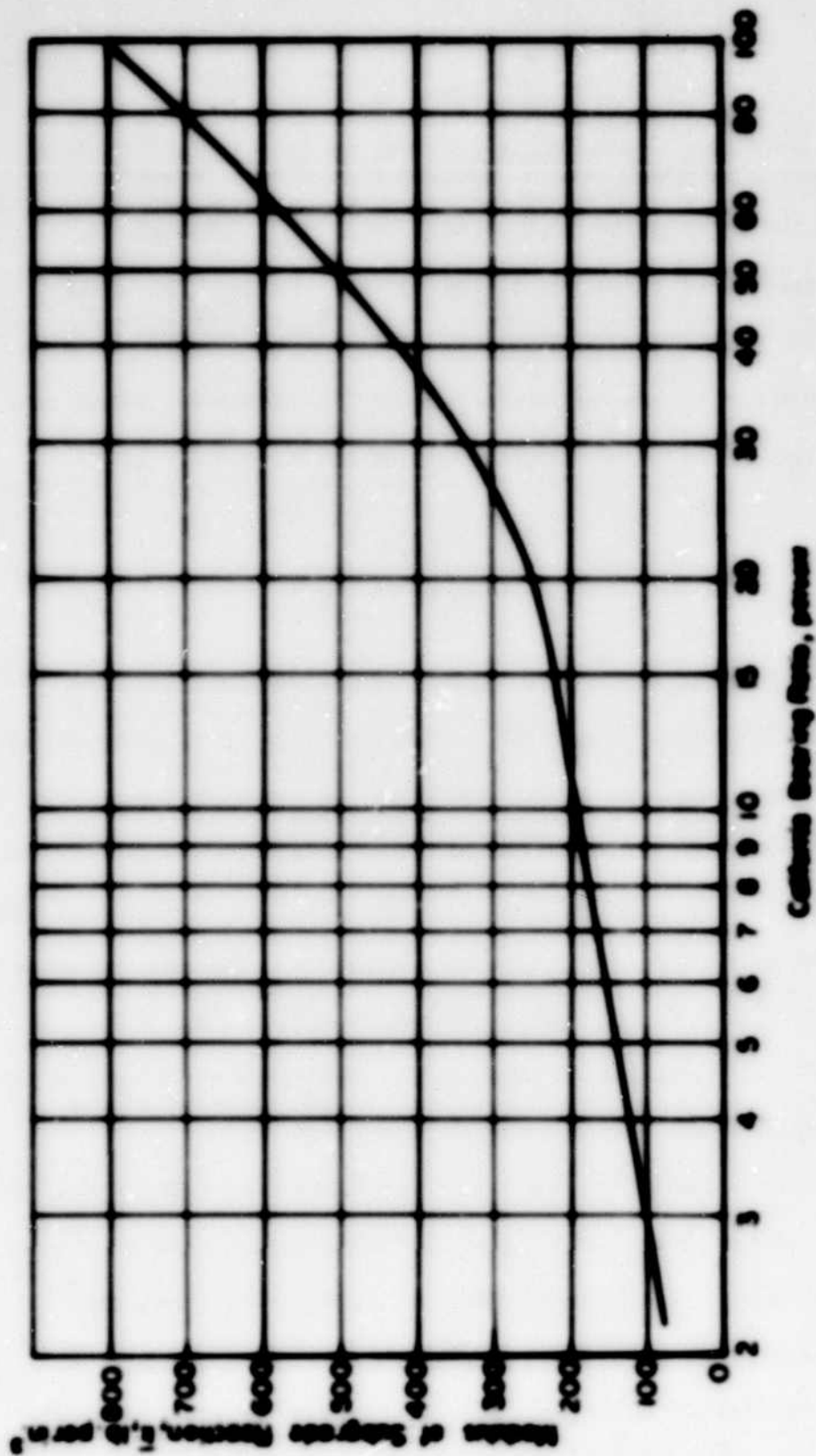


Figure 69. Relationship Between California Bearing Ratio and Modulus of Subgrade Reaction (after PCA [Reference 63])

value of 75 was reported. As noted above, this corresponds quite closely to the minimum calculated value of 73. The range of subgrade CBRs throughout the pavement sections varied from 10 to 85 percent. Reported  $\bar{k}$  values, under the Portland Cement concrete sections, ranged from 220 to 320 psi.

It is interesting to note that the lower value of the range of CBRs for site 1 was about 10 while the low value for all the results was 10. Even though no CBR values were available in the vicinity of site 1, a comparison of its corresponding CBR and  $\bar{k}$  values with those at site 2 indicate it to be an inferior pavement. This had been recognized by the Air Force as it is used only as a parking area; whereas, site 2 is an in-service taxiway.

In summary, the recommended procedure for estimating the  $\bar{k}$  and CBR values from prototype F-4 landings is as follows:

1. Estimate  $A_{\text{peak}}$  from an arithmetic plot of distance ( $x_j$ ) from edge of the tire print versus peak deflections at each gage ( $s_j$ ).  $A_{\text{peak}}$  is the intercept at  $x = 0$ .
2. Use equation (23b) to estimate  $\bar{k}$ , the modulus of subgrade reaction, and, if desired,
3. Find CBR value from established correlation charts such as Figure 69.

A worked example is shown in Appendix E.

### 7.3 Prediction

The prediction methodology consisted of (1) determining the relationship between the inputs of two vehicles at a standard site,

and (2) using this relationship to predict the response of one of the vehicles at another site, if only the response of that site to the other vehicle is measured.

#### 7.3.1 Validity of the Concept of the "Equivalency Function"

The concept of the equivalency function has been used in many areas of engineering. In foundation engineering it has many names, some of which are "shape factor", "depth factor", and "inclination factor". In highway and airfield work it is known as "the equivalent single wheel load" or the "equivalent single axle load" or "layer equivalency factor". The basic underlying concept of "equivalency" is that two different entities can be related by a multiplier. In this work, the multiplier is a function of time - the equivalency function - and not a number.

The question arises as to whether the equivalency function defined at one site is applicable at another site where another set of conditions prevails. The results, Figure 12, showed that the equivalency function is indeed applicable under sets of conditions different from those under which it was first determined.

The equivalency function as defined in equation 21 is essentially a linear ratio of inputs of two vehicles at the same site. In reality the relationship between inputs is probably not linear; however, three factors seem to combine to make the effects of nonlinearity negligible.

First, consider the strain induced in the system due to prototype loading. Measured peak deflections are of the order of 0.05 inch,



whereas the depth of influence of the wheel load is of the order of 12 feet or 144 inches (Reference 60). Small strains, in general of about 0.0003, are thus induced in the system as a result of prototype loading. The linear approximation is valid because strains are small.

The linear approximation to actual nonlinear material behavior at small strains has been used in mechanics for years. Hertz (Reference 66) has shown that if the functional relationship ( $F_1$ ) between stress ( $\sigma$ ) and strain ( $\epsilon_x, \epsilon_y, \epsilon_z, \dots, \gamma_{xy}$ ), given by the equation

$$\sigma_x = F_1(\epsilon_x, \epsilon_y, \epsilon_z, \gamma_{yz}, \gamma_{zx}, \gamma_{xy})$$

is expanded in Maclaurin series, the equation

$$\sigma_x = (F_1)_0 + \left(\frac{\partial F_1}{\partial \epsilon_x}\right)_0 \epsilon_x + \left(\frac{\partial F_1}{\partial \epsilon_y}\right)_0 \epsilon_y + \dots + \left(\frac{\partial F_1}{\partial \gamma_{xy}}\right)_0 \gamma_{xy}$$

results, if the higher order terms in the Maclaurin series are eliminated.

The zero subscripts denote the value of the function  $F_1$  relationship and its derivatives at zero strain. From this relation it can be seen that if strains are small a linear relationship exists between  $\sigma_x$  and  $\epsilon_x, \epsilon_y, \epsilon_z$ , etc. Applying this same reasoning to the equivalency functions, the linear approximation between equivalent inputs works, because of the strains induced in pavement-subgrade systems due to prototype loads are, in general, small at all sites. The equivalency function at one site is thus the same equivalency function at another site where strains are small and of the same order of magnitude.

The second factor, which contributes to the validity of the



linear equivalency function, is inherent in the flexible pavement design procedures, that have evolved, and supports the "small strain" concept previously cited.

Pavements are designed, basically, to limit subgrade deflections. This can be inferred from the fact that conventionally, thick sections are constructed over weak subgrades, while on the other hand, thinner sections are built over strong subgrades. The net effect is that deflections and thus strains are forced to stay within the same order of magnitude of small strains by the design procedures. Since pavement sections are generally designed using conventional procedures, the "small strain" concept previously discussed should be valid for most pavements. Thus, the equivalency function between two such sites would be valid if strains at the two sites are of the same order of magnitude and small.

The third and final factor concerns the time the maximum load is actually applied at a point on the pavements. The time period that the wheel load is over a point is very small. Authors (References 40 and 47) have used Dirac Delta (impulse) functions to represent vehicular loads. Since the time is small, factors such as settlement, which normally are amplified in static cases, are of minimal importance in the dynamic mode.

### **7.3.2 Effects of Gear Configuration**

The C-135, C-131 and C-130 aircraft have different gear configurations as shown in Figures 24 through 26. The prediction methodology permitted a vehicle having a single-twin gear configuration

(C-131) to be used as a standard vehicle to predict the response of a twin-tandem gear (C-132) and a single tandem gear (C-133). This implies that any vehicle in the inventory can be used as a standard vehicle. The combination of evaluation and prediction can then be performed simultaneously by the selected vehicle. Thus, at each site evaluated, the response of all vehicles in the inventory can be predicted as a part of the evaluation.

### 7.3.3 Relative Effects of $k$ , $c$ and $n$ Parameters

Figure 42 showed a typical plot of the calculated equivalent total force and of its force components with respect to the parameters  $k$ ,  $c$  and  $n$ . The maximum resisting force due to the  $k$  parameter is seen to be about twice that of the resisting force due to the  $c$  parameter, and about 7 times greater than that of the  $n$  parameter. If design procedures could be directed toward greater utilization of the  $k$  parameter it appears that a more logical basis for design could be had.

## SECTION VIII

### EFFECTS OF DISTRIBUTION OF PASSES ON RUNWAY PERFORMANCE

It is generally accepted by personnel concerned with airfield pavements that the response of the pavement-subgrade system is a function of the number of wheels on an aircraft gear, its gross load, tire pressures, width of tire print, ambient conditions and the lateral distribution of passes (References 1, 2, 3 and 4).

A method for quantifying the cumulative effect of the lateral distribution of passes, type of aircraft and ambient conditions in the context of pavement evaluation is presented. This method expands the concept of cumulative total pavement deflection presented by Nighter and Herr (Reference 12). They found that a pavement could only accommodate a certain number of feet of cumulative total deflection prior to the onset of distress. Their data base consisted of AASHTO Road Test data, data collected from Pease and Castle Air Force Bases and from prototype testing on specially designed test sections at Kirtland Air Force Base. Analysis of the data showed that a threshold cumulative total peak pavement deflection, at which severe distress occurs in asphaltic airfield pavements, was about 2000 feet. For asphaltic highway pavements the threshold, was about 1200 feet.

#### 8.1 Pass to Coverage (p/c) Ratio Based on Tire-Contact Area Width

The pass to coverage (p/c) ratio, in concept, relates the number of passes made by a vehicle across a pavement-section to the number of passes over a selected point on the pavement. This ratio has been

related conventionally to the number of wheels on an aircraft landing gear, the width of the tire print and the lateral distribution of the aircraft wheel paths.

Two procedures (References 1 and 57) have been used to define the p/c ratio. Both of these procedures use as principal parameters the width of the tire print and the lateral distribution characteristics of the passes over a particular pavement section. The FAA procedure (Reference 1) defines p/c using the relationship

$$c = \frac{0.75 D N W}{12T} \quad (24)$$

where

c = coverage

N = Number of wheels of gear of aircraft

T = Traffic width in feet (generally, 7.5)

W = Width of tire contact area of one tire in inches, and

D = Cycles of operation (one cycle consists of one landing and one takeoff)

The constant, 0.75, is based on the assumption that the lateral distribution of aircraft can be approximated by a uniform distribution as shown in Figure 70(a). In concept, one cycle of operation is essentially two passes. Hence using  $D = p/2$ , equation (24) becomes,

$$c = \frac{(p/2) (0.75 N W)}{12T}$$

$$= \frac{0.75 p N W}{24T}$$

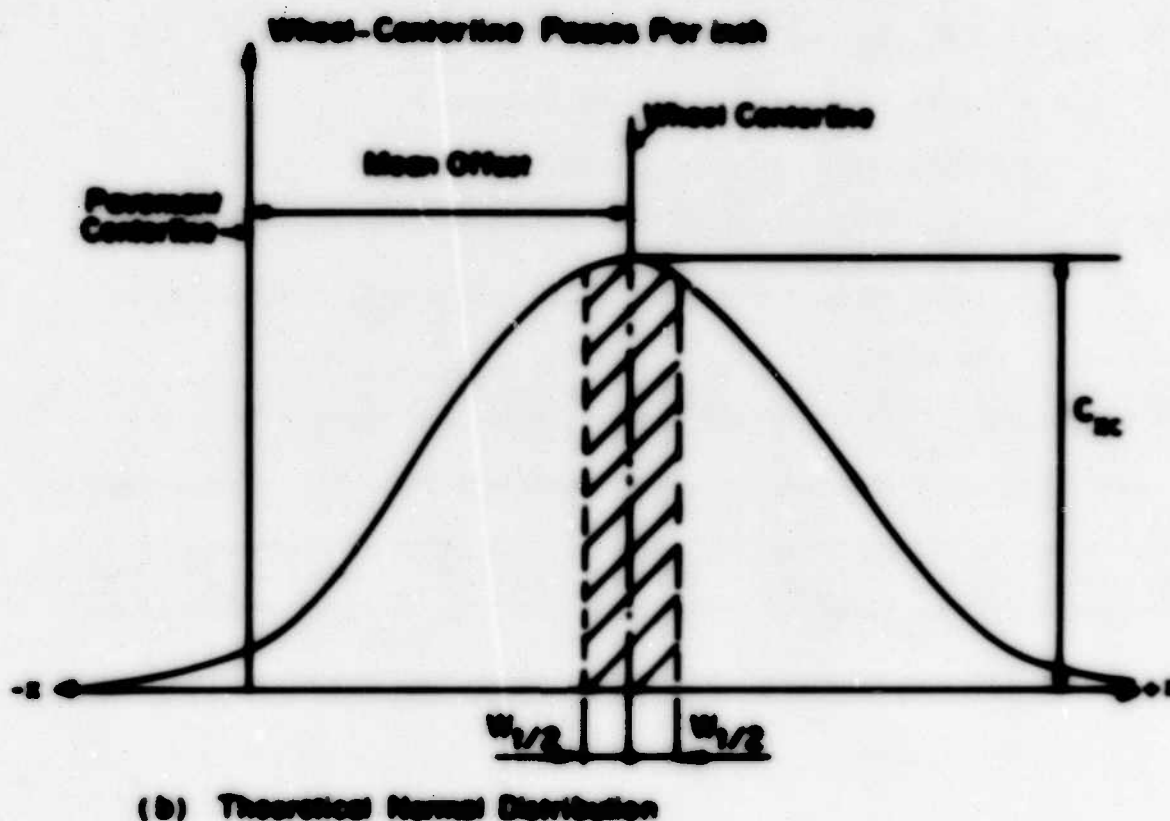
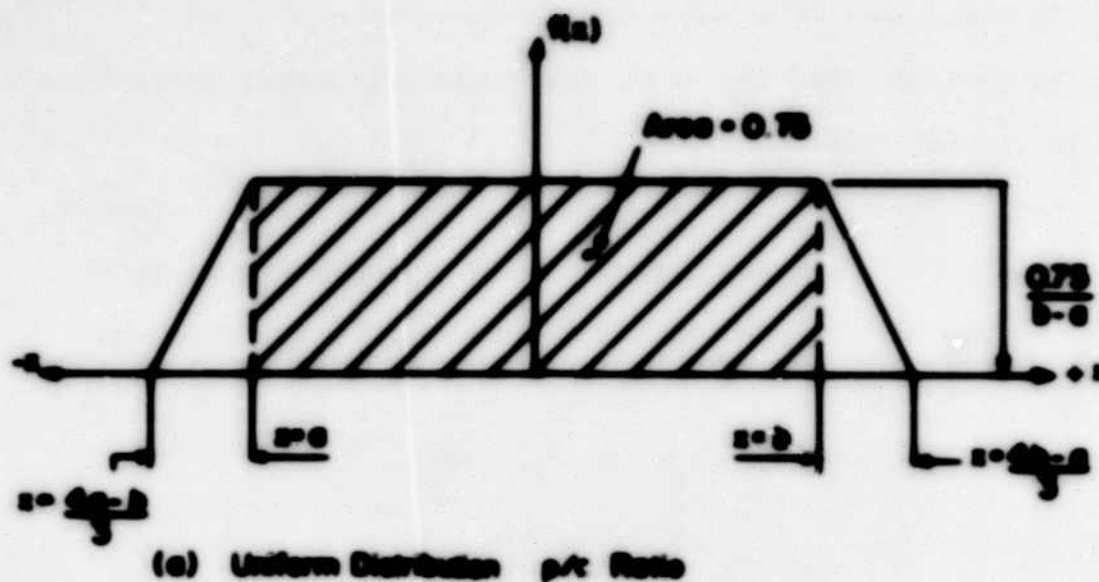


Figure 70. Lateral Distribution of Aircraft Used in Design of Airfield Pavement (after Hoang [Reference 57])

Thus

$$\frac{R}{c} = \frac{127}{WV}$$

Based on measurements of the lateral distribution of aircraft on various runways and taxiways, Hsiao (Reference 57), proposed the use of a normal distribution instead of the uniform distribution, to describe the lateral distribution of aircraft. He gave the following expression for the p/c ratio:

$$p/c = \frac{1}{C_{mc} W_t}$$

where  $W_t$  is the width of the tire contact area, " $C_{mc}$  represents the number of wheel-centerline passes per inch of width, per aircraft pass, which accumulates at the point where maximum accumulation occurs". Coverage  $c$  is defined as the maximum number of wheel passes at the point of maximum accumulation. Figure 70(b) illustrates the p/c ratio concept as applied to a single wheel. In concept, with reference to Figure 70(b), only the effects of tire prints or partial tire prints applied to the surface within the width  $W_t$  are considered in this method.

The current FAA procedure and Hsiao's proposed method both use the tire print (contact area width) as a key parameter in the definition of the p/c ratio. The method developed here uses the measured dynamic lateral deflection profile, due to the prototype load, to define pass to coverage; and relates this ratio to performance extending the peak cumulative deflection concept introduced by Righter

and Harr (Reference 12).

## 8.2 Deflection-Based p/c Ratio

The fundamental concept underlying the deflection-based p/c ratio is founded on the following reasoning. The level of significance of a loaded wheel during one pass over a pavement section is indicated by the measured lateral dynamic deflection basin. As the lateral distance from the load wheel increases, the work done by the load decreases. Hence, immediately under the wheel the influence is greatest; whereas, at a point where the measured deflection is zero, the influence is negligible.

As one pass, in effect, produces deflections from a maximum under the wheel to zero at some distance from the wheel; for a p/c ratio to be meaningful, it should account not only for the induced energy level corresponding to the maximum deflection but for all the levels in the range. The principal reasoning here is that the pavement-subgrade system "remembers" not only the maximum deflection but all load induced deflections. Hence, in general, large load induced deflections at a point result in greater work done and remembrances of it, than do smaller load induced deflections.

With reference to Figure 71, each of the curves labelled P, Q, R, S represents a series of peak lateral deflections. If one pass of a load wheel is applied at a point corresponding to  $x = 0$ , the maximum deflection (at  $x = 0$ ) would be  $A = \Delta_0$ . If the same load had been applied at  $x = 1$ , a maximum deflection of  $\Delta_1$  would have been measured at  $x = 0$ . If the load had been applied at  $x = 2$ , then  $\Delta_2$

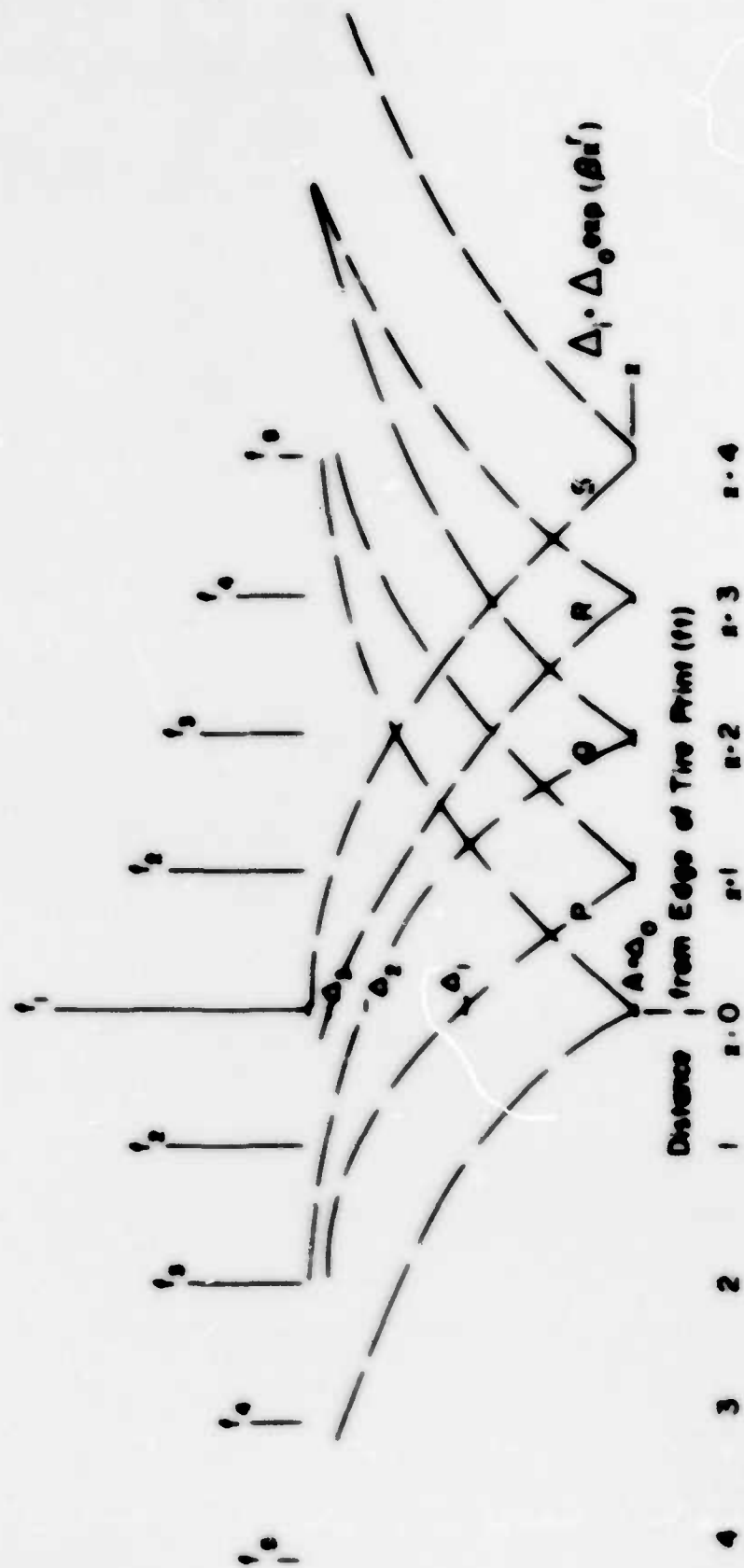


Figure 71. Overview of the Concept Used in the Deflection Based p/c Ratio Calculations



would have been measured at  $x = 0$ ; similarly for a load at  $x = 3$ , etc.

One coverage then, in concept, is the cumulative peak deflection at the point in question that corresponds to maximum deflection  $\Delta$  under the wheel. For example, if one pass of a load wheel is made at  $x = 0$ , then one coverage results at that point. On the other hand, one pass made at  $x = 3$  corresponds to the fractional coverage  $\Delta_y/\Delta$  at  $x = 0$ .

Suppose that  $f_0$  through  $f_n$  are the discrete frequencies at  $x = 0, 1, 2, 3, \dots, n$ , of the distribution of passes of aircraft laterally about  $x = 0$ . Then the cumulative peak deflection at  $x = 0$  due to this frequency distribution becomes

$$\text{Cumulative Peak Deflection} = N_p \sum_{i=0}^n \Delta_i f_i$$

where  $N_p$  is the number of passes and  $\Delta_i$  are the peak deflections corresponding to the points in question. The coverages  $N_c$  due to the  $N_p$  passes is then,

$$N_c = \frac{\text{Cumulative Peak Deflection}}{\text{Maximum Deflection under the Wheel}}$$

$$= N_p \sum_{i=0}^n \Delta_i f_i / \Delta_0$$

Therefore,

$$\frac{N_p}{N_c} = \frac{\Delta_0}{\sum_{i=0}^n \Delta_i f_i}$$

Equation (24) is seen to have the same form as the expression for the equivalent permeability of a layered system (Reference 67)

$$k_y = \frac{d}{\sum_{n=1}^N d_n/k_n} \quad (25)$$

where  $k_y$  is the equivalent vertical permeability,  $d_n$  and  $k_n$  are the thickness and coefficient of permeability respectively of layer  $n$ , and  $d$  is the sum of all the thicknesses.

### 6.3 Effects of Lateral Distribution

The effects of the frequency and of the lateral distributions of aircraft on the cumulative peak deflection and the deflection-based p/c ratio were studied.

Equation (2) in the form,

$$\Delta_j = \Delta_0 \exp(-\beta x_j^r)$$

was used to calculate the lateral dynamic deflection profile, where  $\Delta_j$  and  $x_j$  are the deflections and distances from the edge of the tire print at measurement points  $j$  in a direction perpendicular to the direction of motion of the wheel.  $\Delta_0$ ,  $\beta$ , and  $r$  are the parameters describing the maximum dynamic lateral deflection basin as discussed in paragraph 3.2.1. The numerical values, shown in Table 7, will be used to illustrate the procedure. These values were obtained from data collected at Site 1, Eglin AFB, in March 1976.

Table 7

$\Delta_o = 0.00479$ $\delta = -0.801$ $r = 1.021$	
$x_j$ (ft)	$\Delta_j$ (ft)
0	0.00479
1	0.00215
2	0.00094
3	0.00041
4	0.00018

Four discrete distributions are shown in Figure 72 for an assumed single wheel load. Figure 73 shows the effect of the four assumed lateral distributions (keyed by number to Figure 72) on the cumulative deflection. Figure 74 shows the effect of the scatter of the frequency distribution, as given by its standard deviation based p/c ratio. These results show that,

1. the assumption of a uniform distribution of passes (distribution ① on Figure 72) yields the least cumulative peak deflection per pass and,
2. as would be expected, the distribution with the smallest scatter yields the greatest cumulative peak deflections.

#### 8.4 Discussion

The results showed the dependence of cumulative peak deflection

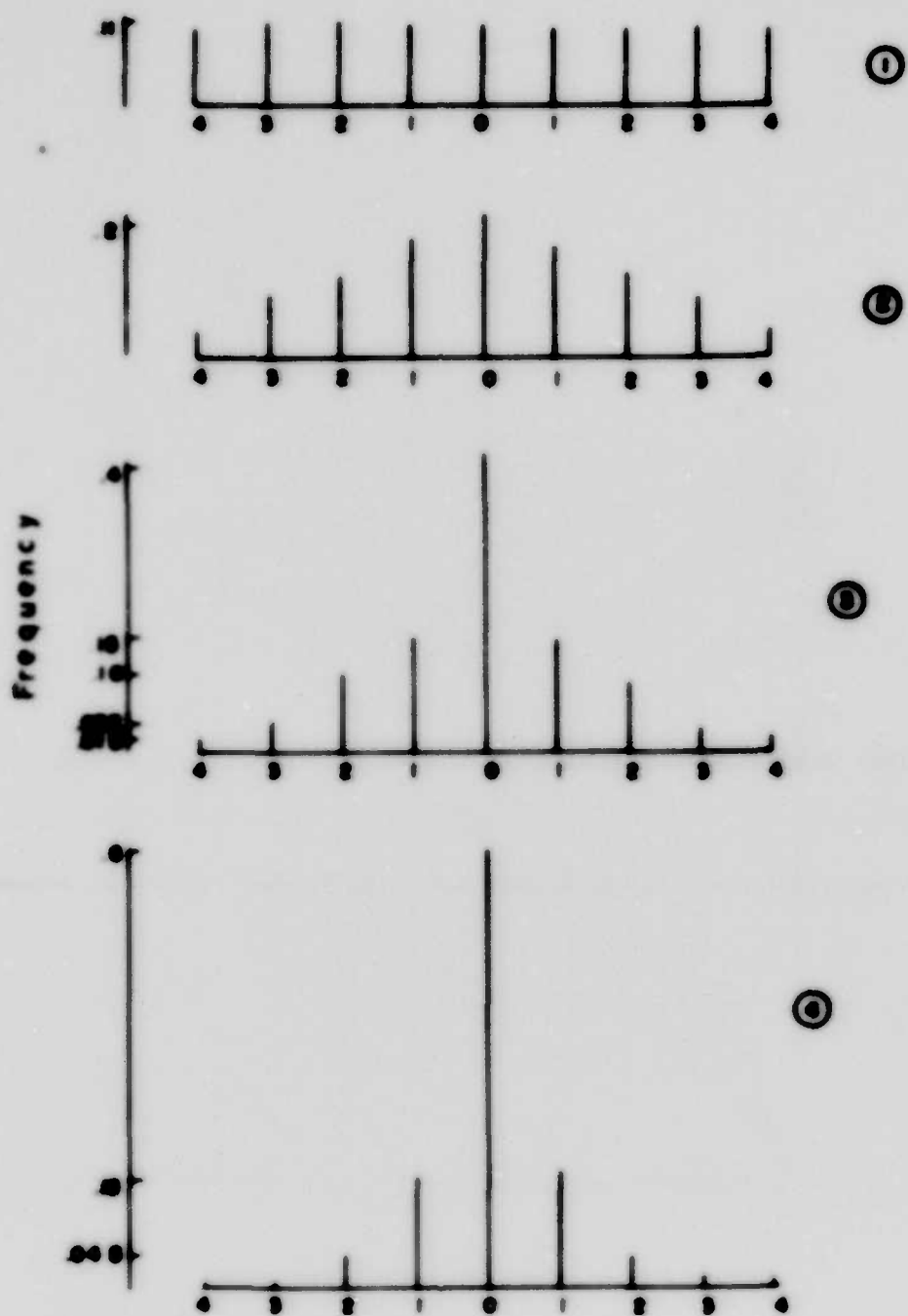


Figure 72. Discrete Distributions Used in Study

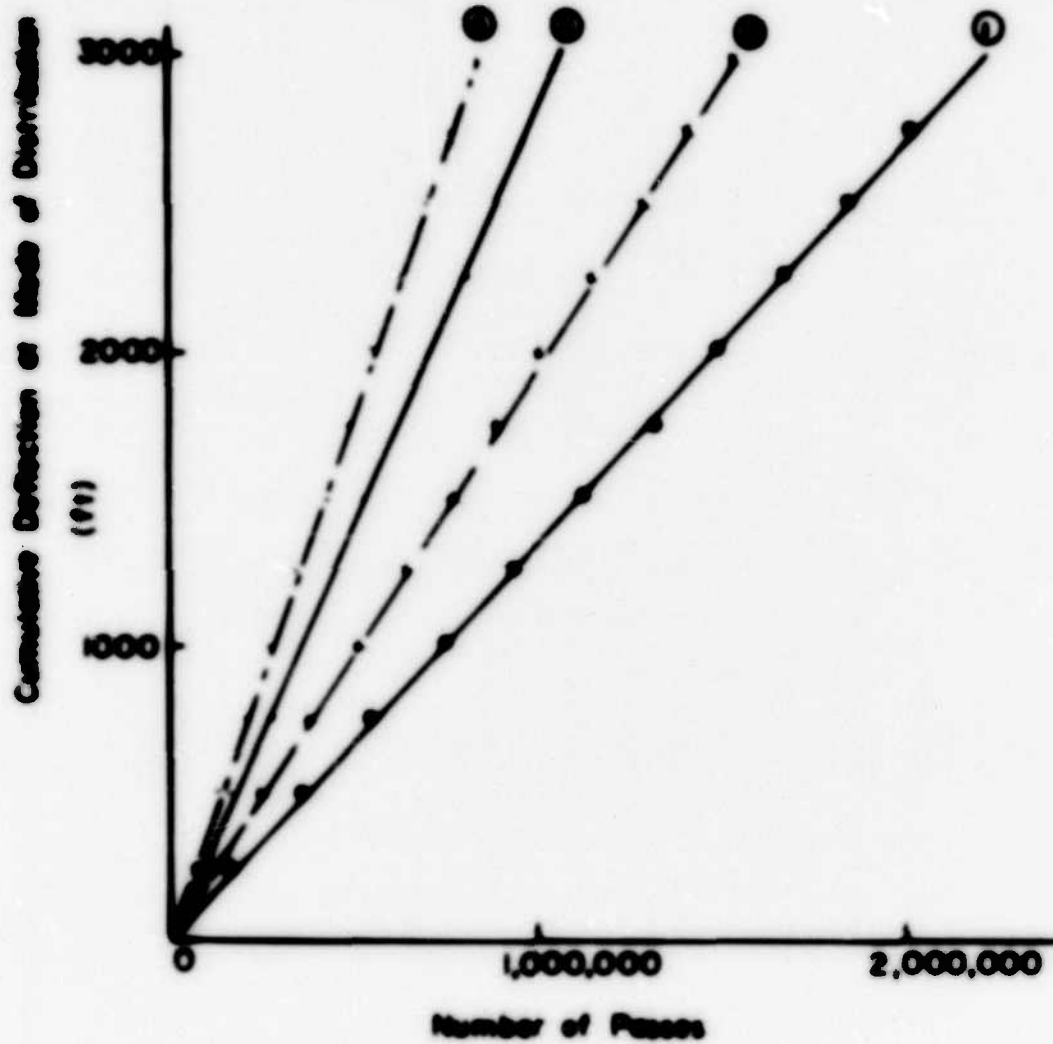


Figure 73. Cumulative Deflection vs. Passes for Four Discrete Distributions of Passes

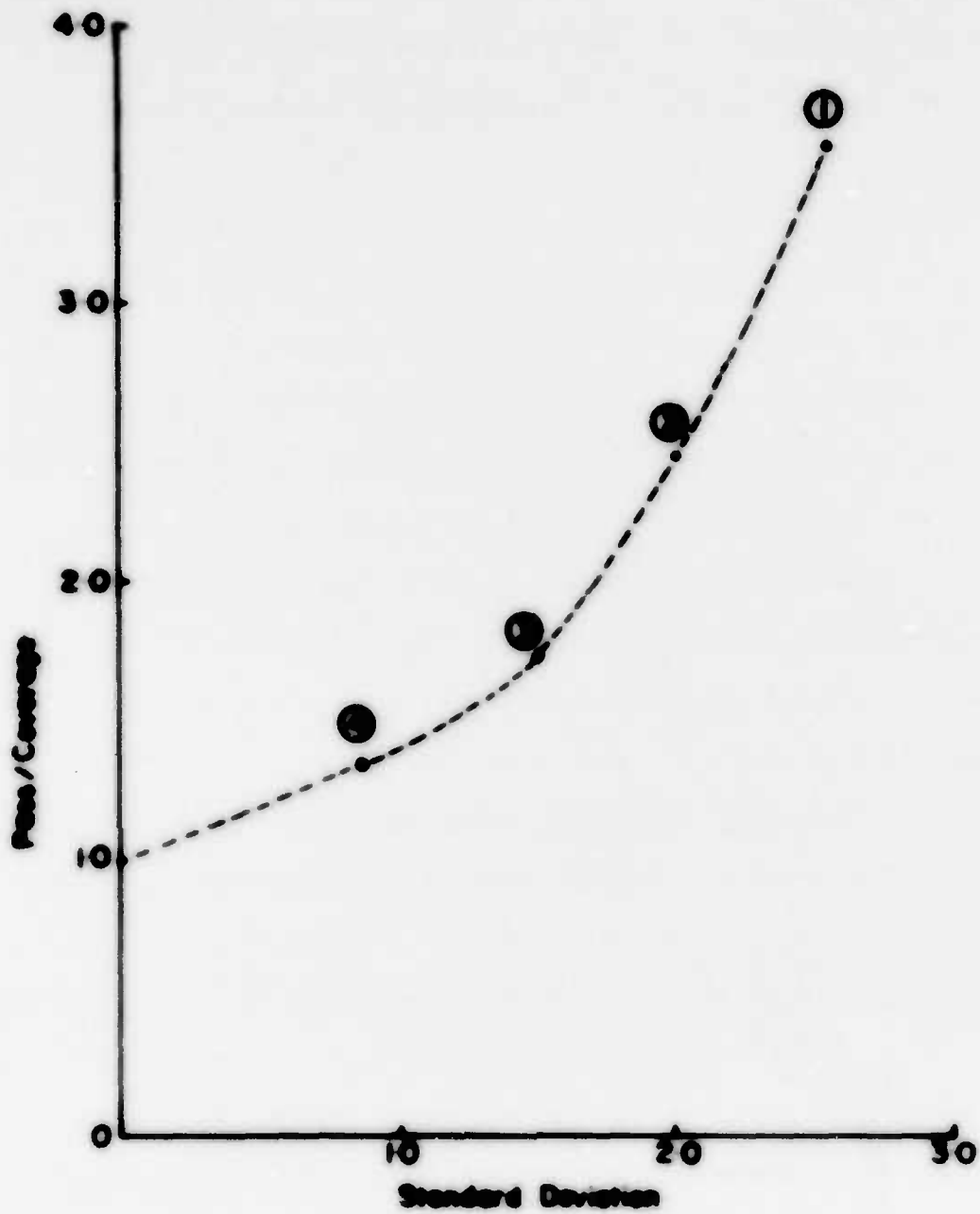


Figure 74. Effects of Standard Deviation on Deflection-Based p/c Ratio

on the lateral distribution of passes and the peak deflection profile. The p/c ratio thus provides a means of quantifying the variability of the input (aircraft loads) characteristics and pavement-subgrade system response (output).

With reference to Figure 75, input variables consist of aircraft loads and lateral distribution characteristics of loads. These can include wind effects, surface condition, type of aircraft, and quantity of fuel aboard. The main output variable is the peak pavement deflection profile. Inherent in this measurement are temperature effects and other ambient conditions. Figure 75 shows how the p/c ratio can be utilized to estimate the amount of energy imparted to a pavement-subgrade system due to variable inputs and also how to estimate the number of passes required to induce a certain energy input as given by the total cumulative peak deflections.

For example, assuming that the lateral distribution of passes has a standard deviation of 2.0 (distribution ② in Figure 73), the number of passes required to reach the threshold<sup>13</sup> total cumulative peak deflection value of 2200 feet is 1,160,000 passes or 580,000 cycles of operation.

On the other hand, if the assumed lateral distribution of passes has a standard deviation of 2.66, then 580,000 cycles of operation would yield a cumulative peak deflection value of about 1500 feet, which is well below the threshold<sup>13</sup> value for that distribution. For this case 850,000 cycles of operation could be tolerated before severe

<sup>13</sup>The threshold value of 2200 feet was given by Hightner (Reference 12) without due regard to the lateral positioning of traffic. Lacking additional information at this time the same value was used in the present study.

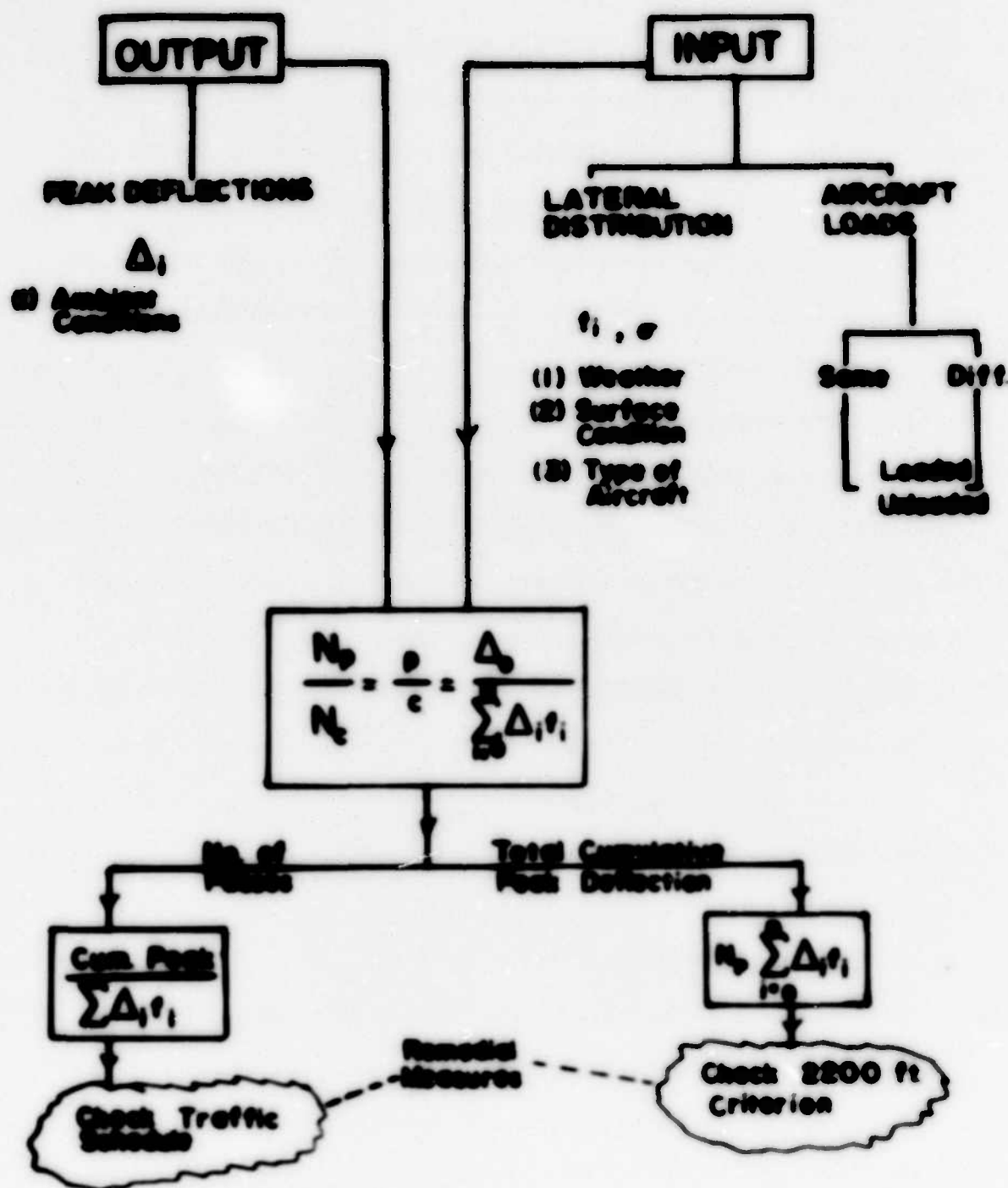


Figure 75. Overview of Evaluation Scheme Using Deflection Frequency Relationship



distress might be expected.

As another example, suppose that due to overlay or resurfacing of pavement, parameters and peak deflections change to those given in Table 8 after 290,000 cycles of operation, then 700,000 cycles of operations (rather than 290,000) would now be required to attain the threshold<sup>14</sup> value of 2200 feet. This assumes that the section "remembers" the loading prior to resurfacing. If resurfacing had not taken place, only 290,000 cycles of operation would have been required to show effects of distress.

The above examples have attempted to show that actual measured distribution data such as that provided by HoSang (Reference 57), and actual measured deflections (which account for ambient seasonal effects) can be combined to estimate the cumulative damage effects due to prototype loads. Once a standard site and standard vehicle have been selected, the damage effects of various magnitudes of loads

Table 8

$\Delta_0 = 0.0012$ $\bar{S} = -0.2256$ $r = 1.7770$	
$x_j$ (ft)	$\Delta_j$ (ft)
0	0.00120
1	0.00096
2	0.00055
3	0.00024
4	0.00085

<sup>14</sup> See Footnote 13.

and gear configurations and their distributions can be estimated. By monitoring the effects of specific pavement sections, the direction which remedial measures should take could be established (see Hightor and Harr (Reference 12)).

## SECTION IX

### SUMMARY

The findings of the present research effort can be summarized under three basic categories, namely:

1. nondestructive pavement testing equipment development,
2. nondestructive pavement evaluation and behavior prediction, and
3. extension of cumulative peak deflection-damage-energy related concepts.

Two equipment systems for use in the nondestructive evaluation of flexible pavements have been developed. They are the LED system and the LVDT system. The feasibility of rapidly measuring pavement deflections caused by moving loads using the developed equipment has been investigated. Field testing of the developed systems using prototype loads was conducted.

A nondestructive pavement evaluation methodology using transfer function theory has been developed. Parameters of the transfer function which reflect site characteristics have been isolated and related to performance of two sites. Parameters of the lateral peak deflection profiles have been investigated. Simplified procedures for estimating the parameters of the transfer function and parameters (CBR, etc.) used in design have been suggested.

A methodology has been presented for predicting the deflection if the response at a standard site to a standard load vehicle and another vehicle, and the response of the other sites to the standard vehicle are known. The same transfer function parameters that are used in the

evaluation phase are used in the prediction scheme.

A method of accounting for the lateral distribution of aircraft on a pavement, and variability of input and output to the pavement-subgrade system has been presented. The interrelationship among the components of NDT pavement evaluation-response prediction-cumulative damage prediction based on deflections caused by prototype loading has been discussed. The deflection based pass to coverage ratio was shown to be a vital link in the scheme.

## SECTION X

### CONCLUSIONS

This research effort has attempted to cover a spectrum of activities that comprise nondestructive testing and evaluation of flexible airfield pavements. The following conclusions have been reached as a result of this study.

1. Rapid nondestructive measurements of pavement deflections due to moving prototype loads can be obtained in the field using the LED system "breadboarded" in this research effort and the companion LVDT system.
2. The parameters of both the transfer function and the peak lateral deflection profile reflect characteristics of the pavement-subgrade systems and can be used as the basis of a nondestructive pavement evaluation scheme. Some common parameters such as CBR and modulus of subgrade reaction can be obtained from those defined in this study.
3. The developed methodology, using the same parameters of the transfer function that are used to evaluate a pavement system, can be used to predict the deflection response function of a site to different magnitudes and configurations of loadings.
4. The concept of cumulative peak deflection (Reference 12) as it relates to energy induced in a pavement-subgrade-system due to load repetition, was extended to account for the lateral distribution of aircraft. The frequency characteristics and the number of passes of aircraft are shown to

effect, significantly, the amount of distress a pavement  
might evidence in time.

## SECTION XI

### RECOMMENDATIONS

This work has afforded the opportunity to consider in some depth a significant portion of the current state of the art of nondestructive testing theory and methods used on airfield pavements. Based on the findings of this work the following recommendations are forwarded:

1. The use of prototype loadings in evaluation should be encouraged.
2. The development of a scheme, based on the use of nondestructively measured pavement deflections due to prototype loads, similar to that briefly discussed in paragraph 8.4 of this work should be pursued.
3. The prototype of noncontact measuring equipment shown to be feasible in this investigation should be developed. This development should take advantage of the current state of the art in optical design.
4. A thorough study of the lateral distribution of aircraft has recently been made (Reference 57). A similar information gathering study should be initiated to collect data on numbers and types of aircraft using specified pavements at both commercial and military installations. Pavement deflections should be obtained regularly at the sections being monitored. This data base is necessary if the concepts and the preliminary conclusions reached at this time are to be validated and generalized.
5. The speedy development of a prototype device to move over the

pavement sections and simultaneously measure its own dynamic deflection basin without significantly interrupting traffic would greatly facilitate the information gathering phase. This would simultaneously provide a common denominator or standard vehicle.

6. Research should be directed towards determining the influences of the components of a pavement-subgrade system on the  $k$ ,  $c$ , and  $a$  parameters. The success of this endeavor would be a step towards optimizing design procedures and the use of paving materials.



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APPENDIX A  
RESEARCH AND DEVELOPMENT  
OF  
MEASUREMENT SYSTEMS

The breadboard model of the LED system was subcontracted by Purdue University to Science Applications Incorporated (SAI), New Mexico, during the period May, 1974 to December, 1975. The contents of Section a of this Appendix is based principally on SAI's Final Report (Reference 56).

During the period January 1975 to June 1976, the breadboard model electronics was upgraded at Purdue University and work was done to convert the static measurement system in order to make it more compatible with a moving beam-moving load concept. Section b of this Appendix presents a summary of this work.

Section c of this Appendix presents some details of the Linear Variable Differential Transformer System (LVDT) developed at Purdue University by G. Baladi (Reference 52) for a study sponsored by the FIRMA.

a. The LED System

Several optical systems were considered during the development of the LED system. These include:

1. A retroreflector module whose motion is detected by a laser beam.
2. A limited version of the global Moire method.
3. Focal point shift detection.
4. Triangulation of a light spot on a surface.



As the triangulation method was finally selected for development, only the summary details concerning this method are presented herein.

The breadboard model employing the triangulation method is shown in Figure A-1. This arrangement has an image shift  $\delta_2$  (Figure A-2) perpendicular to the line of view which is related to the pavement deformation by the equation,

$$\delta_2 = m \frac{\sin(\gamma + \beta)}{\sin \gamma} \cdot \frac{\delta}{\tan(90 - \gamma)}$$

where  $m$  is the magnification of the deformation. Other symbols are designated in Figure A-2. The pavement "roughness" function is represented by  $f(x)$ .

The straight line of the input center ray is given by

$$y = (x-b) \tan(90 - \gamma)$$

or

$$y = x \tan(90 - \gamma) + a$$

The intersection of the input ray with  $f(x)$  is at  $x_0$ , giving

$$f(x_0) = x_0 \tan(90 - \gamma) + a$$

and the intersection with the displaced  $f(x)$  is at  $x_1$ , giving

$$\delta + f(x_1) = x_1 \tan(90 - \gamma) + a$$

Using a Taylor expansion near  $x_0$  to get  $f(x_1)$  and dropping higher orders gives

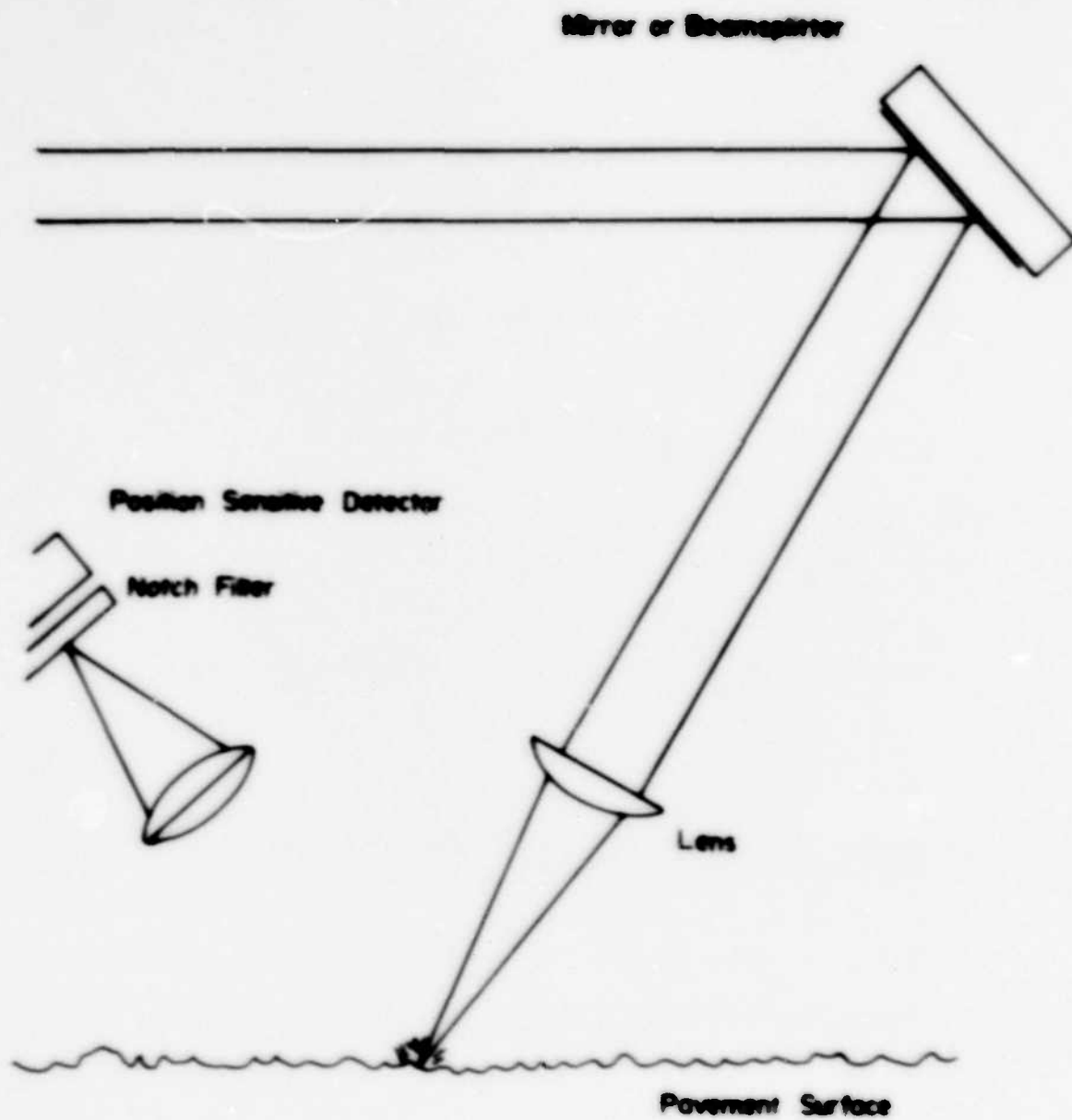


Figure A-1. Triangulation Arrangement

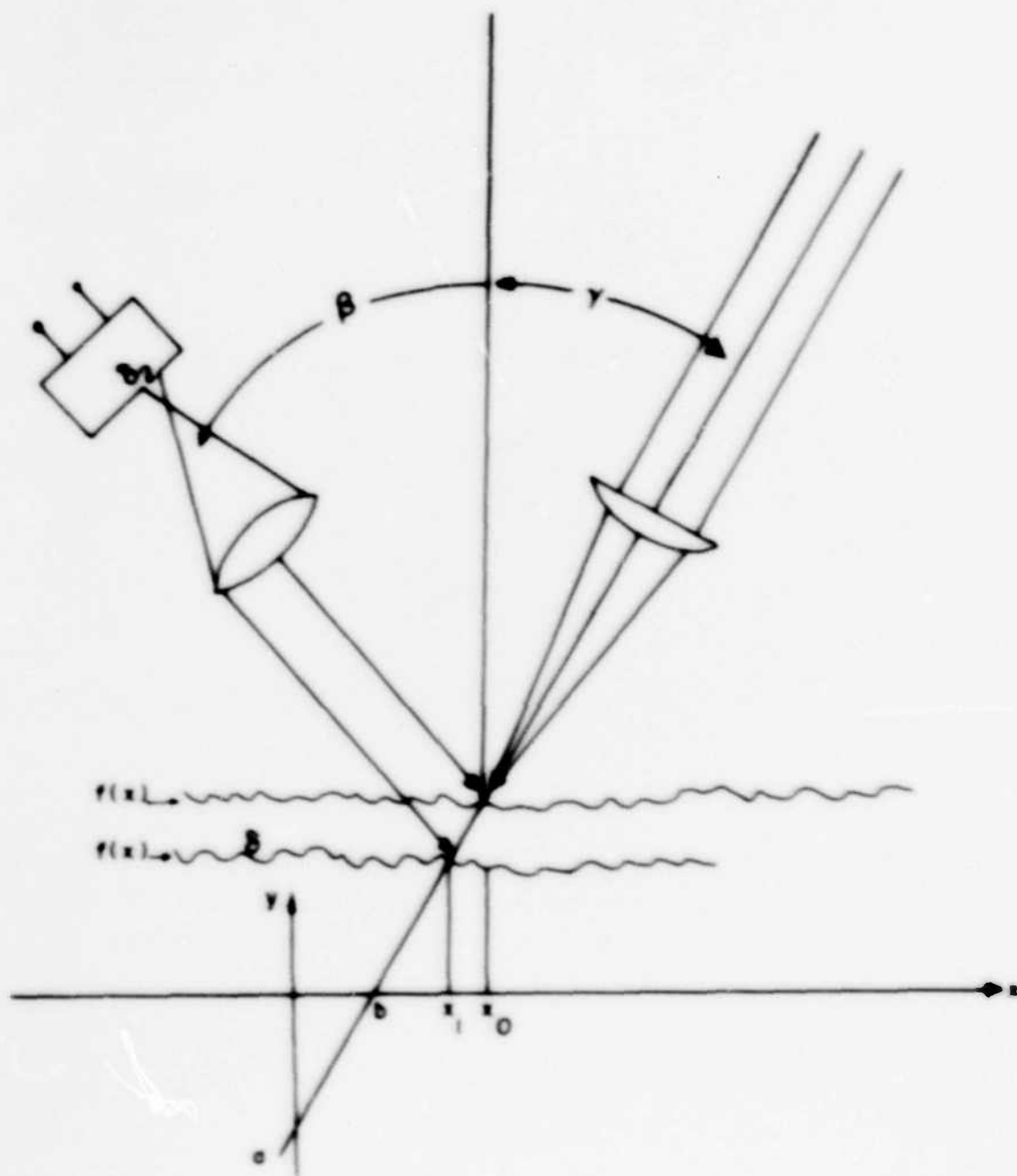


Figure A-2. Triangulation Parameters

$$f(x_1) = f(x_0) + \frac{f'(x_0)}{1} (x_1 - x_0) + \frac{f''(x_0)}{2} (x_1 - x_0)^2$$

Substitute this into the second intersection equation and subtracting the two gives

$$(x_1 - x_0) \tan(\theta - \gamma) - \delta = f'(x_0)(x_1 - x_0) + \frac{f''(x_0)}{2} (x_1 - x_0)^2$$

which is solved to obtain,

$$(x_1 - x_0) = \frac{2\delta}{[f'(x_0) - \tan(\theta - \gamma)] \pm [f'(x_0) - \tan(\theta - \gamma)]^2 - 2f''(x_0)\delta}$$

The image point is shifted by the component  $\delta_2$  normal to the axis of the imaging lens where,

$$\delta_2 = n \frac{\sin(\gamma + \delta)}{\sin \gamma} \cdot (x_1 - x_0)$$

The image motion can then be obtained as a function of the arrangement parameter ( $\gamma$ ), the surface  $f(x_0)$  and the surface displacement, ( $\delta_1$ ) by the equation

$$\delta_2 = n \delta_1 \left[ \frac{\sin(\gamma + \delta)}{\sin \gamma} - \frac{2}{\left[ \frac{\cos \gamma}{\sin \gamma} - f'(x_0) \right] \pm \left[ \frac{\cos \gamma}{\sin \gamma} - f'(x_0) \right]^2 - 2f''(x_0)\delta} \right]$$

However, the pavement is rough on the scale of the focused spot on the runway. To eliminate the dependency on surface roughness, there are two alternatives. First, make the focused spot a focused line long enough that the effects of roughness are averaged to zero and second, reduce the angle between the pavement normal and input ray,  $\gamma$ , to zero. The image motion equation when  $\gamma = 0$  reduces to

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NONCONTACT NONDESTRUCTIVE DETERMINATION OF PAVEMENT  
DEFLECTION UNDER MOVING LOADS(U) PURDUE RESEARCH  
FOUNDATION LAFAYETTE IN M E HARR ET AL AUG 77

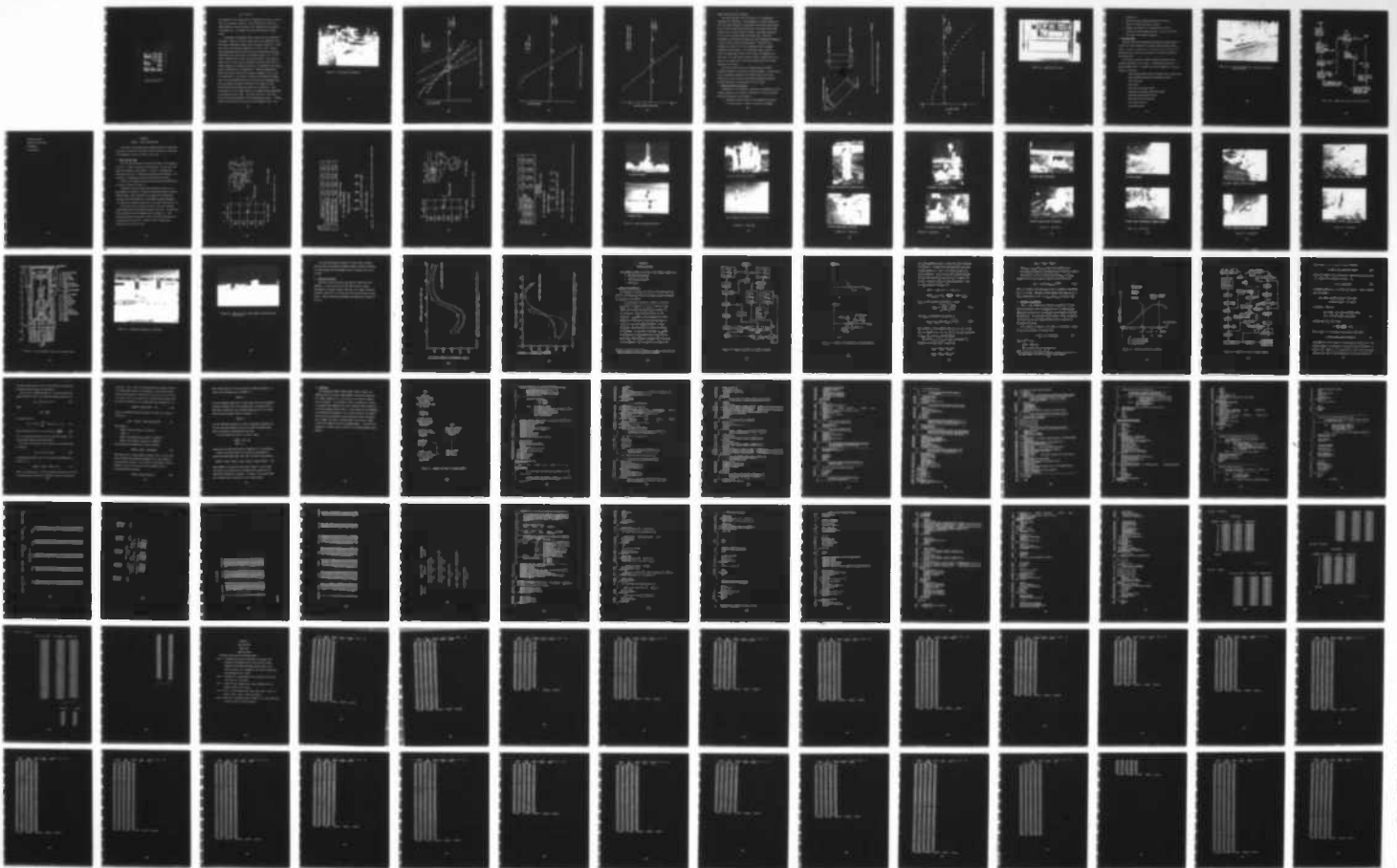
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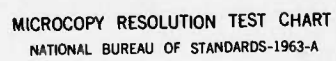
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MICROCOPY RESOLUTION TEST CHART  
NATIONAL BUREAU OF STANDARDS-1963-A

$$\delta_2 = m \delta \sin \beta$$

The sensitivity of the image motion is maximized when  $\beta$  goes to  $90^\circ$  but that is not physically possible. Also the collection of light for imaging depends on the solid angle of the imaging lens with respect to the pavement spot. The larger  $\beta$  forces the solid angle to smaller values.

A triangulation arrangement using a laser input was breadboarded and tested. Figure A-3 shows the laser setup in the laboratory at SAI. Some typical displacement signal curves are given in Figure A-4. These data are for four different samples and  $\gamma = 23^\circ$ ,  $\beta = 45^\circ$ . Several other arrangements and the theory given above demonstrated that these calibration curves become smooth and repeatable when  $\gamma = 0^\circ$ ,  $\beta = 45^\circ$  using a cylinder lens to focus a line on the surface. Also shown in Figure A-5 is a curve which was obtained by using the sum of the two position signals as a normalization factor. An extension of the linear range is obtained with the normalization. Using the normalization method also yields a further more important advantage, that is, that the reflectivity of the surface is removed from affecting the signal. Figure A-6 shows normalized data for concrete and gray sandpaper which have the maximum and minimum reflectance of the sample set used. Their reflectance difference was greater than a factor of 2. The differences in the two signals appear in the regions where normalization has extended the linear range. The major contributor to this error was the inaccurate measurement of the normalization constant. If higher precision electronics had been used in this breadboard, most of the

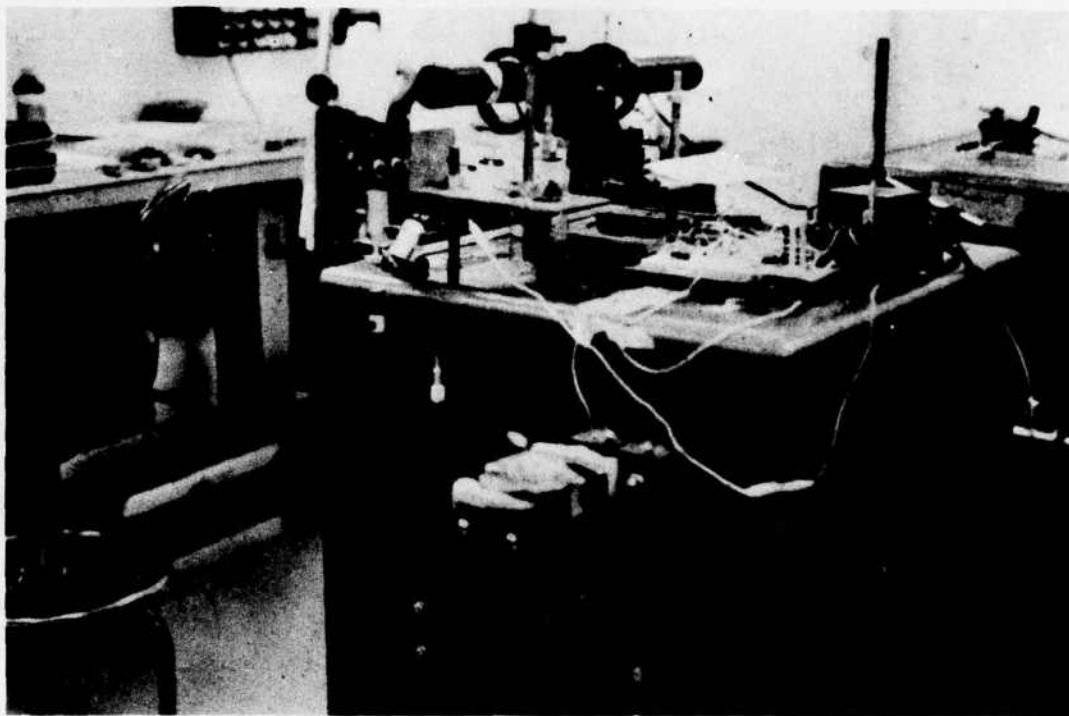


Figure A-3. Laser Setup in Laboratory



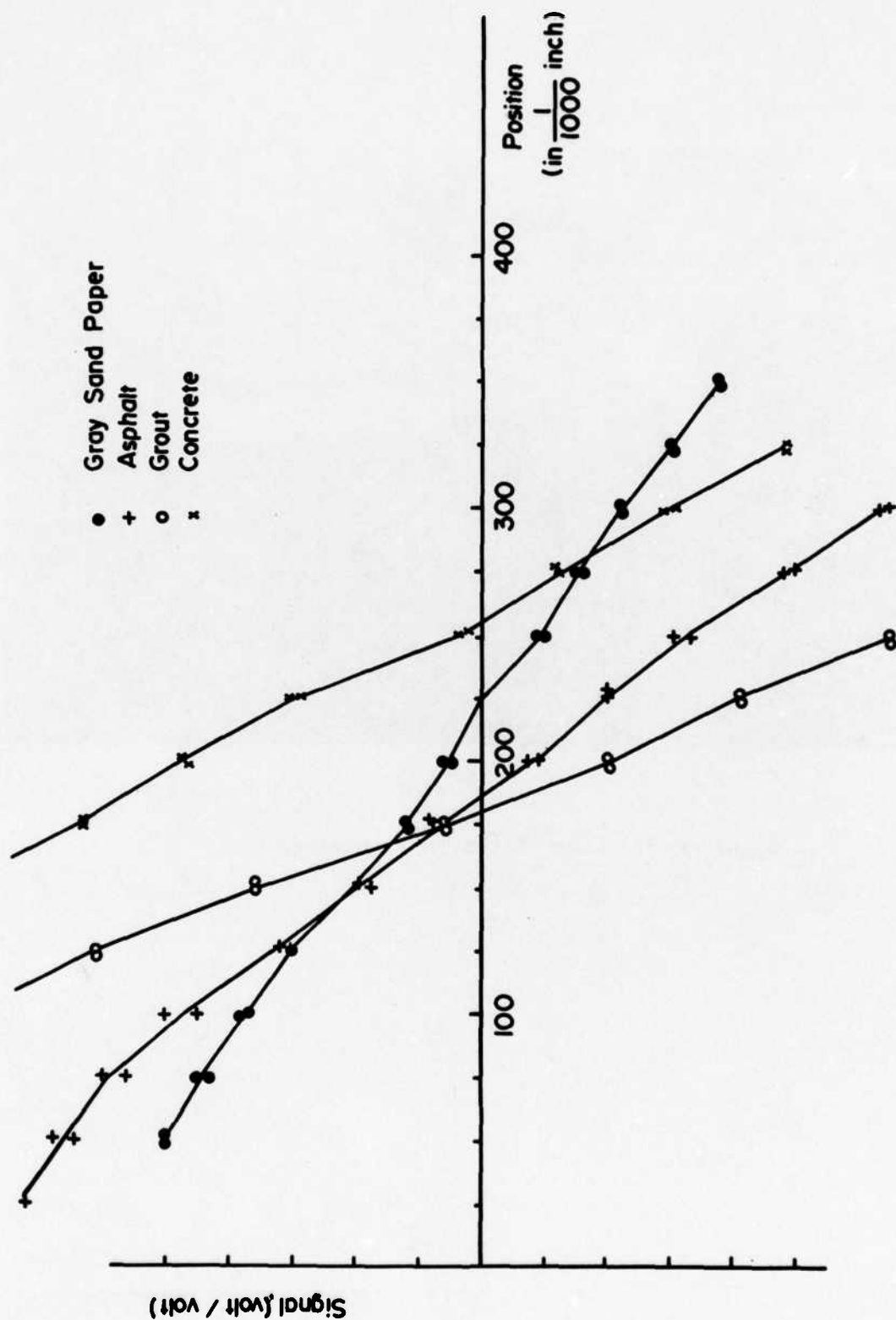


Figure A-4. Typical Triangulation Displacement Curves

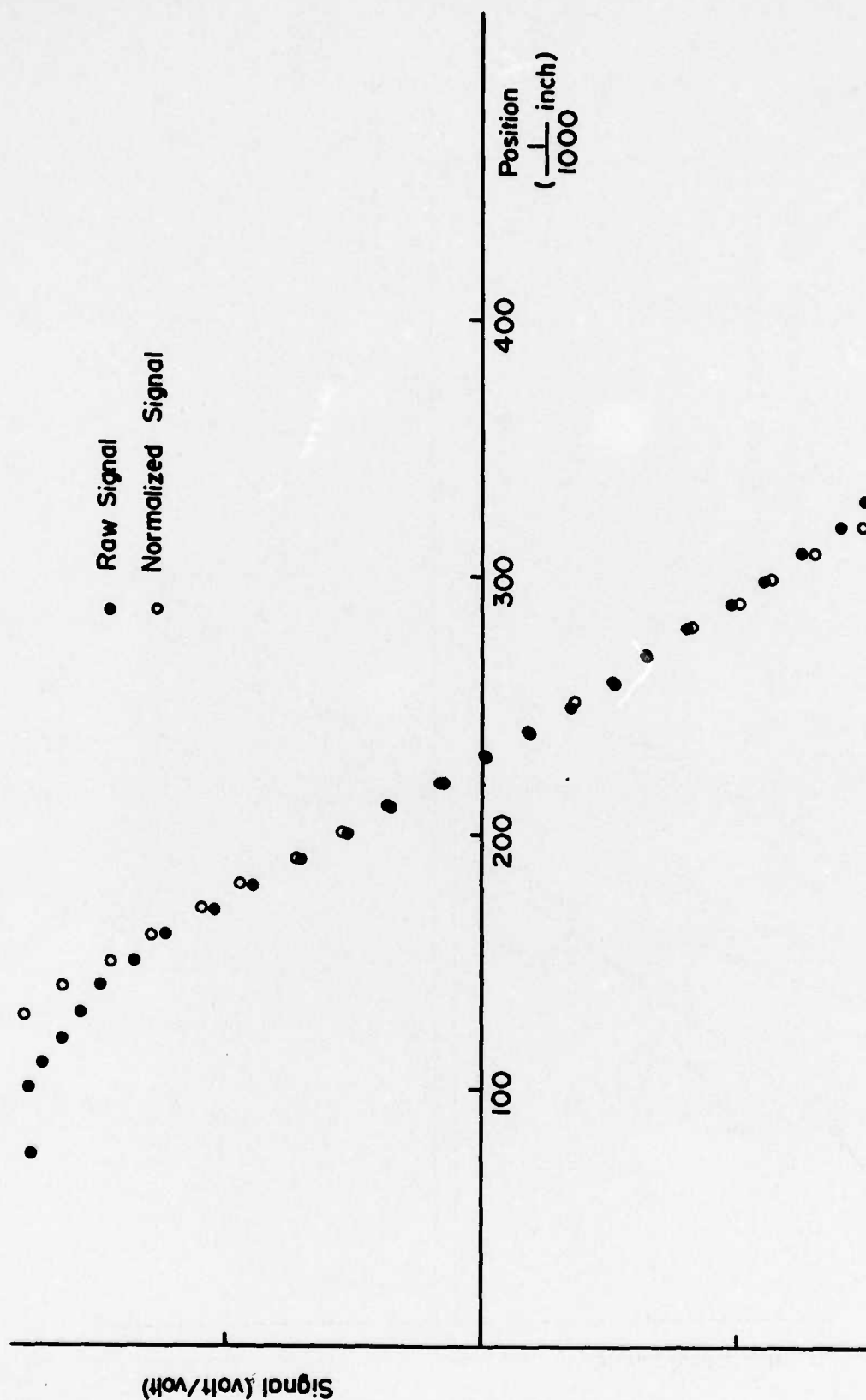


Figure A-5. Normal Incidence Displacement Curve

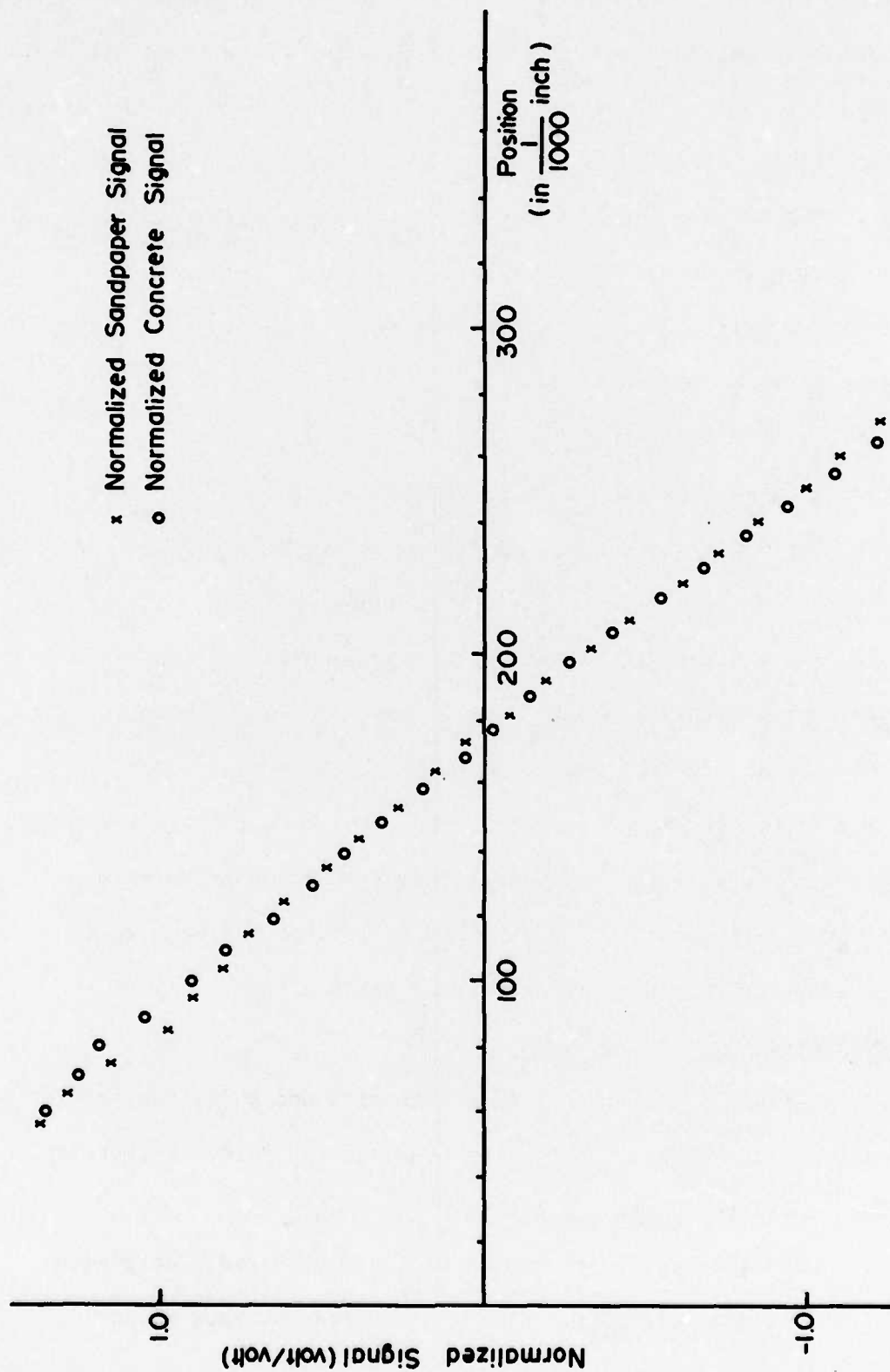


Figure A-6. Normalized Deflection Curves

signal differences would disappear.

The choice was made to use LED sources in a triangulation arrangement to deflections. This arrangement is shown in Figure A-7 and is the same triangulation arrangement as was tested before except that the light emitting diode replaces the input laser beam and the cylinder lens has been modified by adding a convex-plano spherical lens to form a composite spherical-cylinder lens. This lens arrangement was developed by mapping the three dimensional distribution of energy using an aperture and photodiode. The peak of the intensity was found for each lens arrangement until an optimum arrangement was determined. The displacement signal, shown in Figure A-8 demonstrates effects of the change in sharpness of the focal zone. The curve shows a change in slope in either side of the central focus region that is due to the larger area for the "line" focussed on the surface.

The basic optical principle as described herein remained unchanged throughout the course of system development. The electronics and the mechanical attachments were however modified to be more consistent with the concepts of the moving load-moving beam which evolved subsequent to the conclusions of SAI's effort.

b. Additional Work on LED System

Repackaging of the breadboard electronics and modification of the software supplied by SAI was done by personnel at Purdue University. This work consisted of the following:

1. Converting the basic wiring of the breadboard electronics to printed circuits. Figure A-9 shows the repackaged

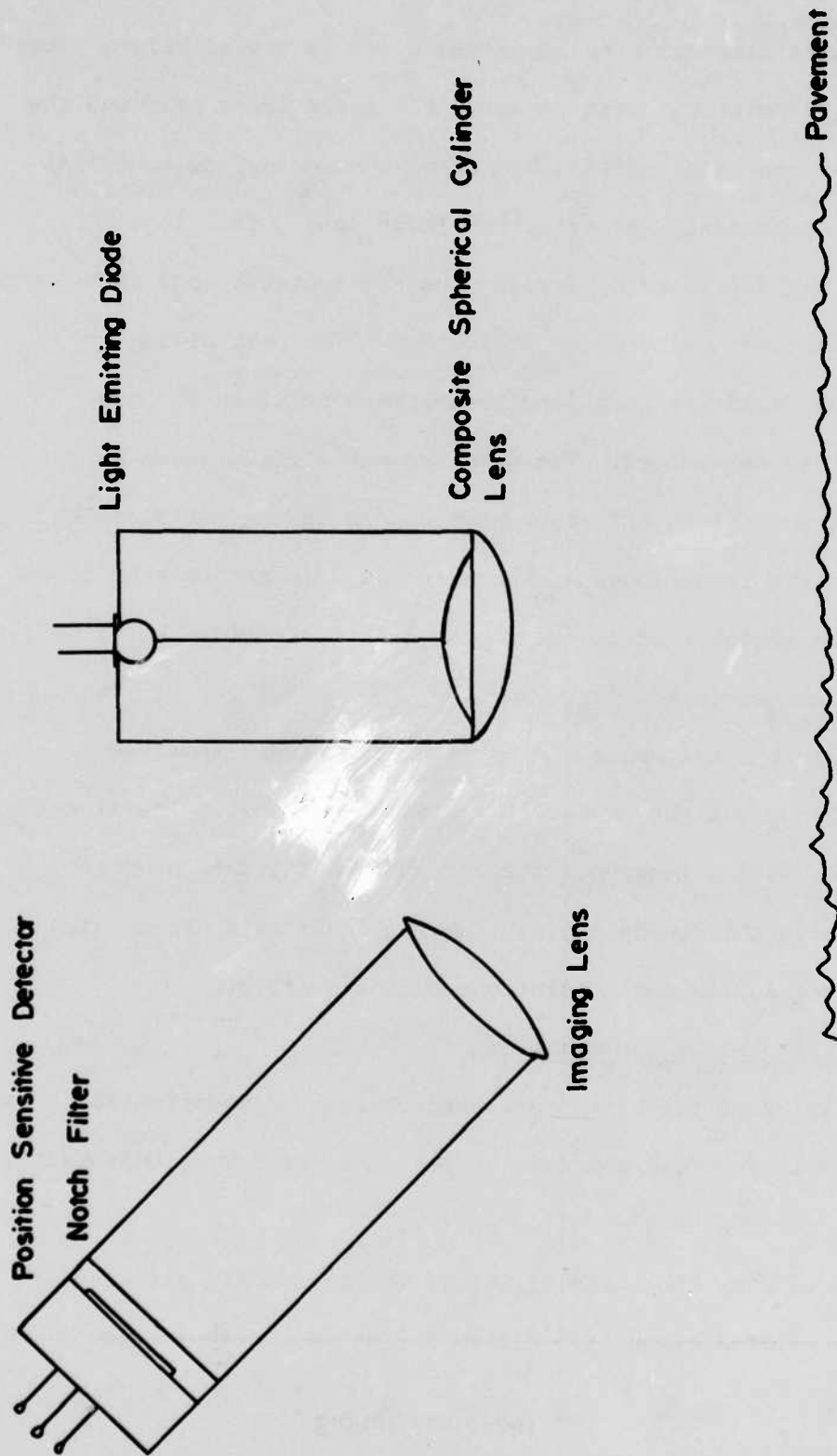


Figure A-7. Light Emitting Diode Triangulation Arrangement

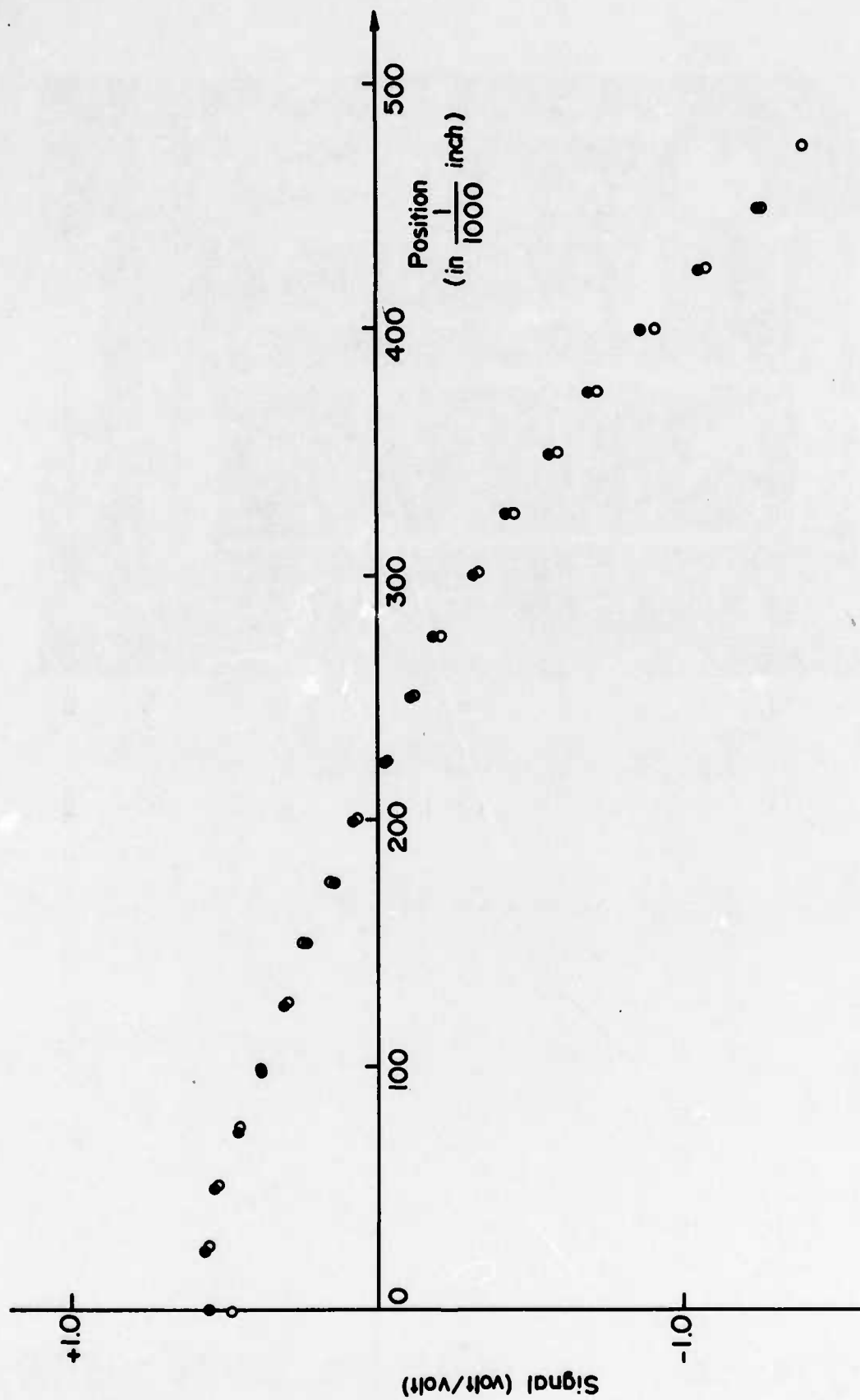
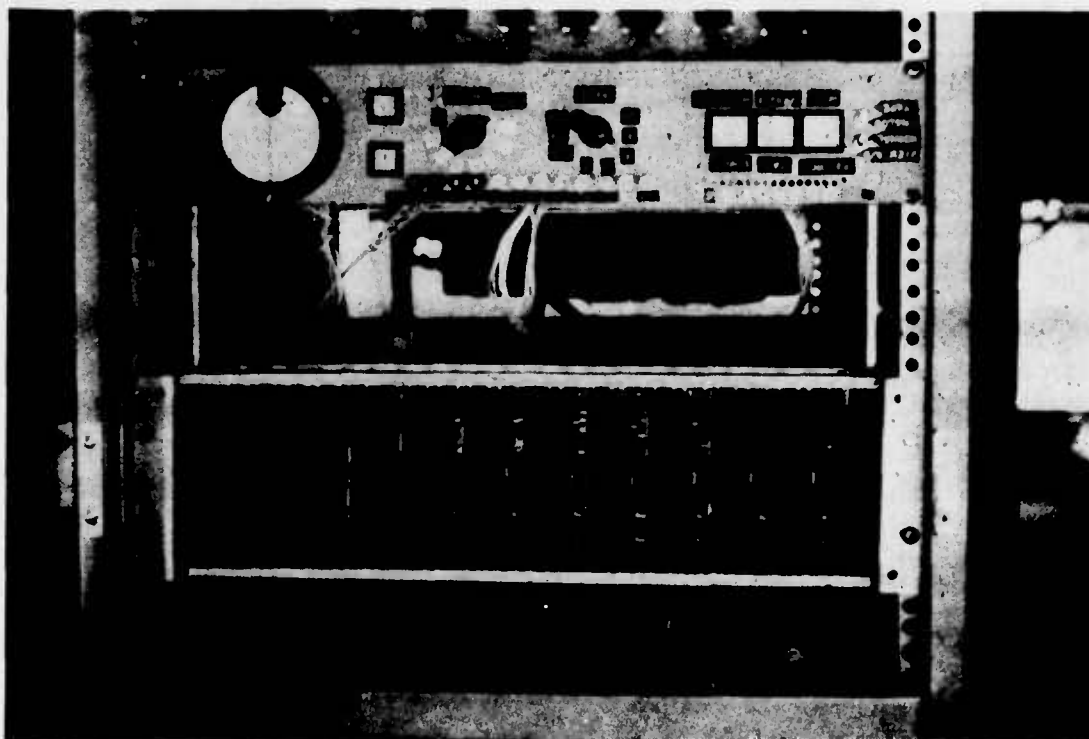


Figure A-8. Light Emitting Diode Displacement Curve



**Figure A-9. Repackaged Electronics**

electronics.

2. Testing the basic moving beam-moving load concept.

Figure A-10 shows the basic test setup.

3. Changing the software to be compatible with the new concept of a moving beam-moving load. Figure A-11 shows a flow chart of the modified software.

c. The LVDT System

The LVDT system was designed and fabricated at Purdue University as part of a study sponsored by the Federal Highway Administration (FHWA). Because an overview of the system has already been presented previously in this report only the details of the system components are present here.

The use of the system to measure response functions has been discussed previously in this report. For additional details see Baladi (Reference 52). A listing of the basic components of the LVDT system is as follows:

- Light Weight Aluminum I-beam, 80 inches long, 12 inches wide
- Linear Variable Differential Transformers (LVDTs)
- 2 Way Screw Jack
- Pipe (pivot)
- Small Screw Jacks under LVDTs
- 6-Channel Oscilloscope Light Beam Recorder
- Kodak-2022-light Sensitive Paper
- Sears Electric Power Generator
- AC-DC Power Converter
- Micrometer-Caliper





Figure A-10. Test Setup Moving Beam - Moving Load Operation:  
Purdue University

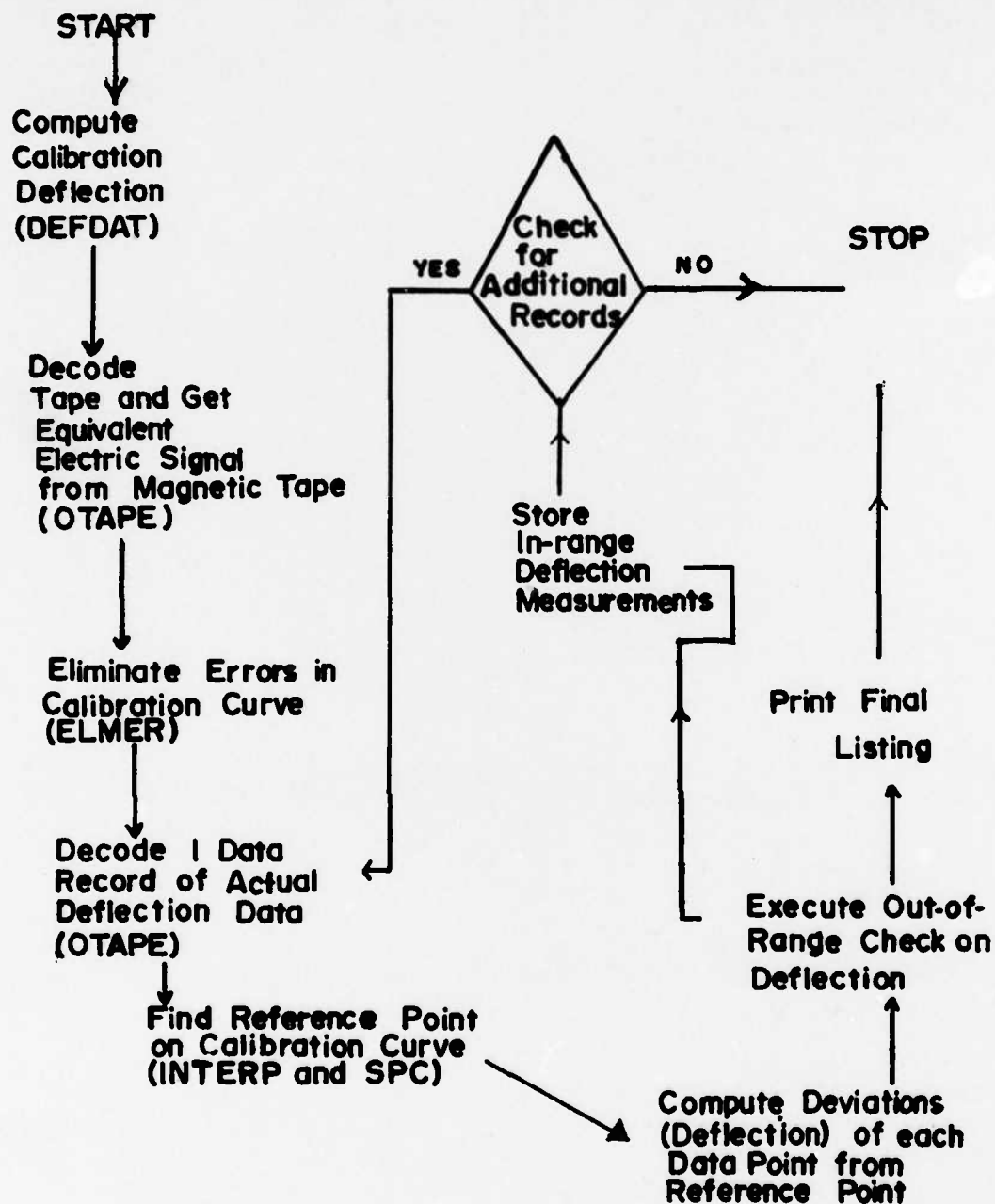


Figure A-11. Summary Flow Chart of LED System Software

- Hydraulic Scales
- Heavy Duty Silver Tape
- Thermometer
- Miscellaneous

## APPENDIX B

### SERIES A: FIELD INVESTIGATIONS

The Series A field investigation program consisted of conducting field tests at Eglin Air Force Base, Florida and Pease Air Force Base in New Hampshire during the period of this study.

#### a. Eglin Air Force Base

Two sites were selected at Eglin Air Force Base. The location of the sites is shown in Figures B-1(a) and B-3(a). At each site, LVDT gages were embedded in the pavement. At Site 1, five gages were installed and at site 2, four gages were placed in the pavement. The locations of the gages are shown in Figures B-1(b) and B-3(b).

Details of the boring locations and site profile characteristics are shown in Figures B-2 and B-4.

A summary of the gage installation procedure is shown in the photosequence in Figure B-5. Figure B-6 shows the details of typical installed gage. After installation, the gages were calibrated as discussed in Boyer (Reference 11), and pavement response functions were obtained as discussed previously in this report (see section 5.1).

Grids were laid out as shown in Figures B-1(b) and B-3(b) and response functions were determined using the LVDT beam. The gages were first calibrated using the equipment shown in Figure B-7. Then response functions were obtained at each of the grid locations shown in Figures B-1(b) and B-3(b). Figure B-8 shows a typical pass being made by the P-2 fire truck.

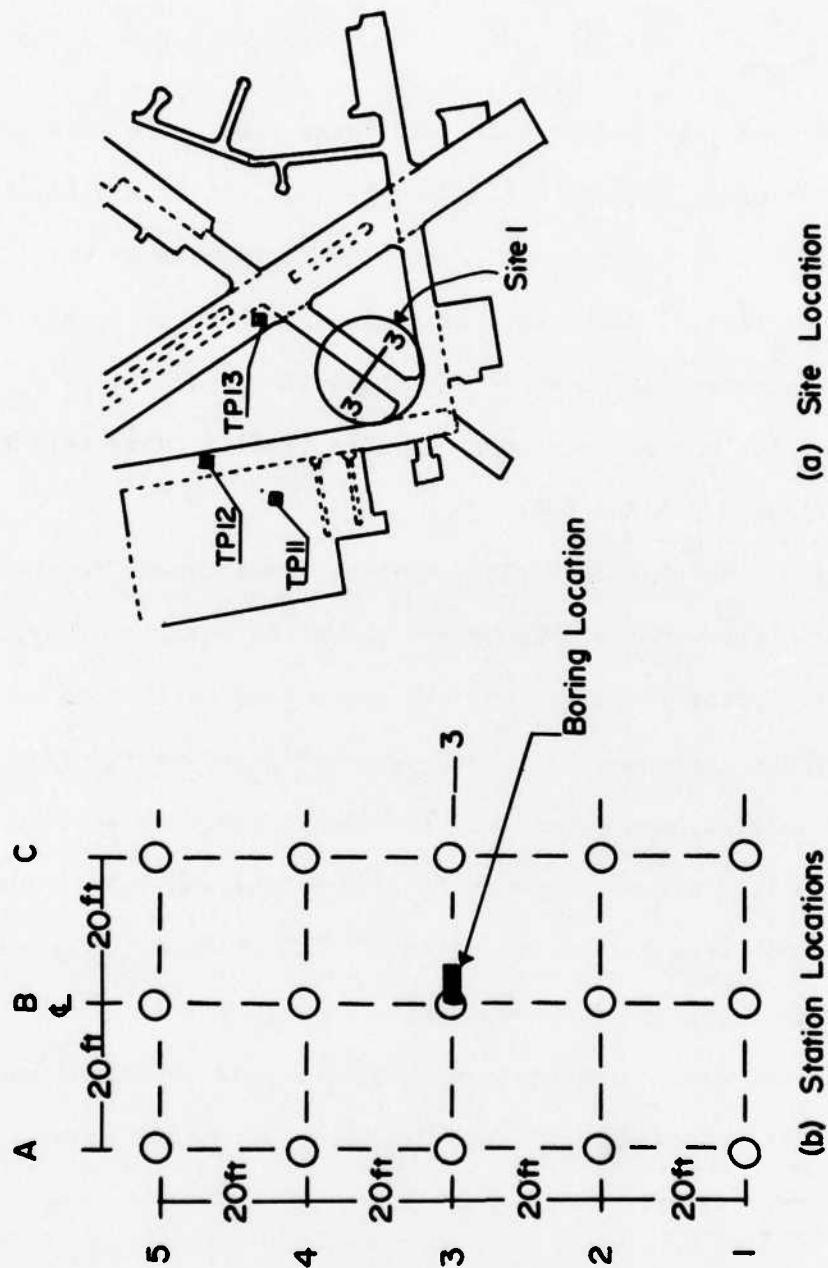
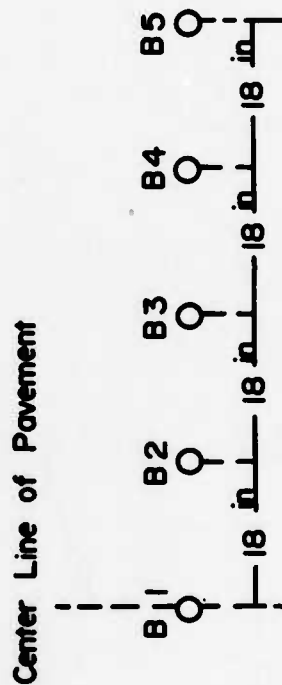


Figure B-1. Eglin Air Force Base: Site 1

Layer	Boring Number								
	A	B	C	B 1	B 2	B 3	B 4	B 5	
A				2.25 +	2.0	2.0	1.35	2.0	
				7.0	7.5	7.0	7.0	7.0	
				168	168	168	168	168	

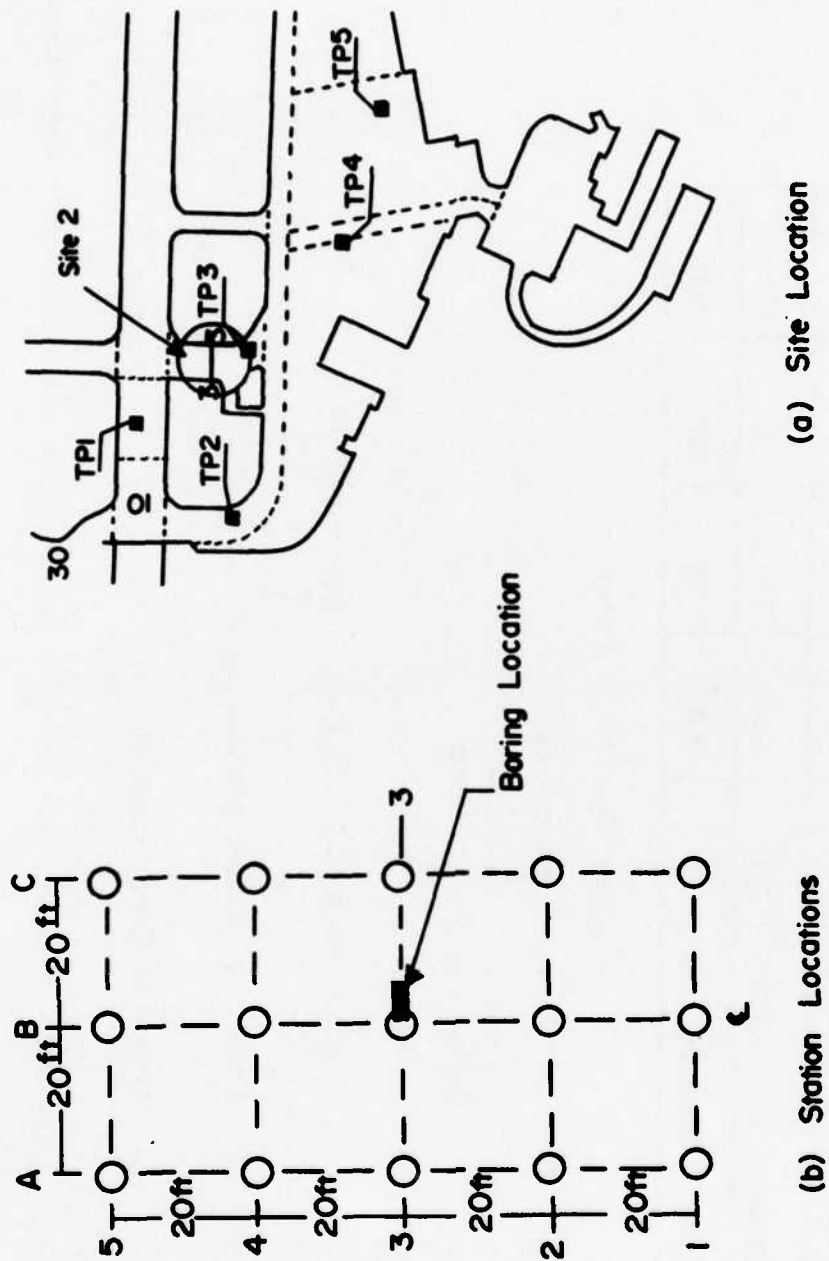
+ Layer Thickness in Inches

(a) Site Profile Characteristics



(b) Details of Boring Location

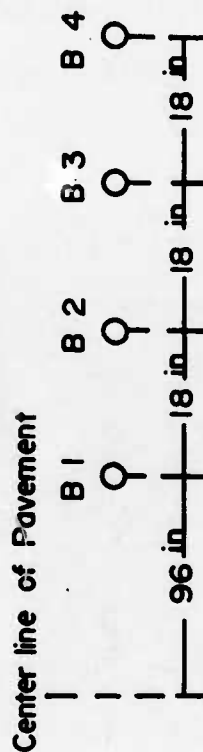
Figure B-2. Eglin AFB - Site 1: Details of Boring Location and Site Profile Characteristics



Layer	Boring Number				
A	Layer A - Asphalt Concrete <sup>1</sup>				
B	Layer B - Asphalt Concrete <sup>2</sup>				
C	Layer C - Sand Asphalt				
D	Layer D - Medium Sand				
E	Layer E - Silty Sand				
	B 1	B 2	B 3	B 4	
	1.25 <sup>+</sup>	1.125	1.25	1.25	
	3	3	3	3	
	14	13.5	11.5	12.0	
	132	132	132	132	
	48	48	48	48	

1 Resurfacing  
2 Old Surface  
+ Layer Thickness in inches

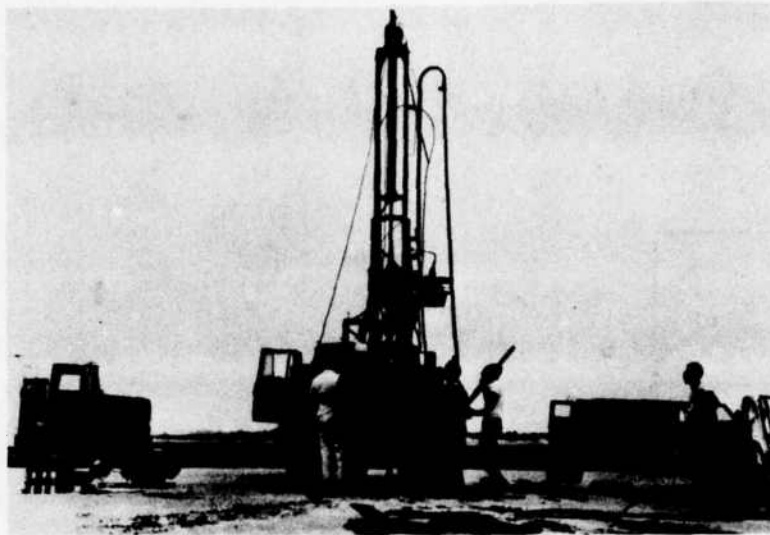
(a) Site Profile Characteristics



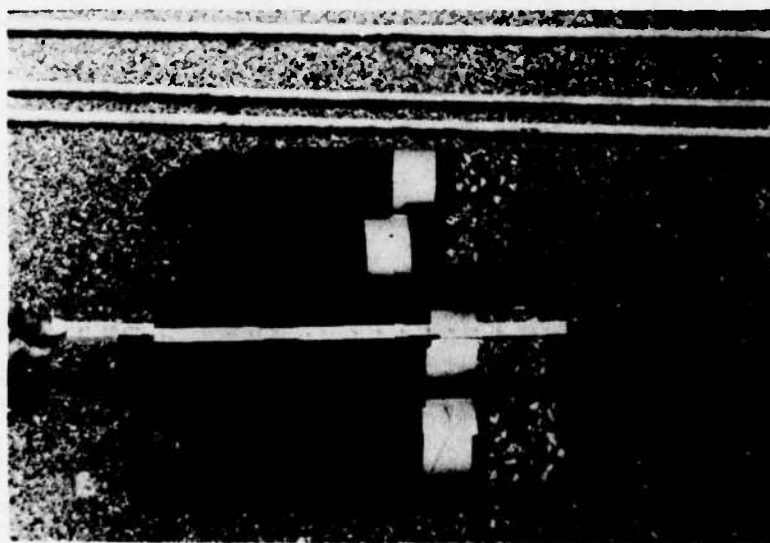
(b) Details of Boring Location

Figure B-4. Eglin - Site 2: Details of Boring Location and Site Profile Characteristics



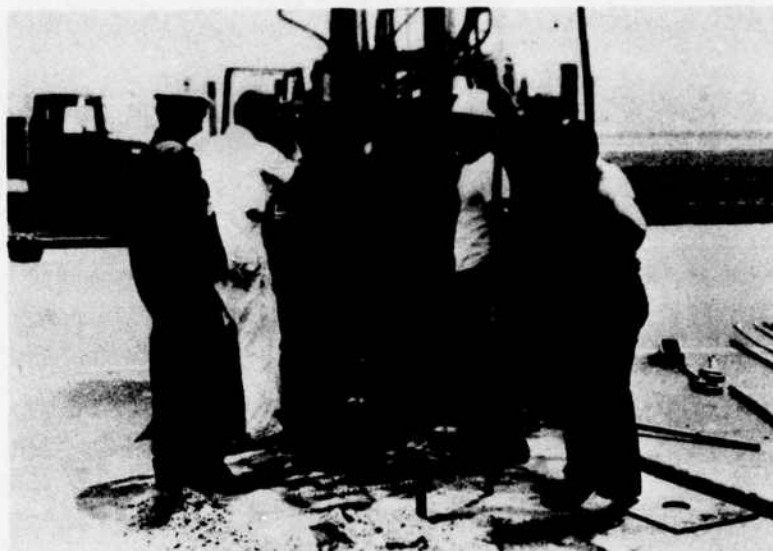


**(a) Coring Pavement**

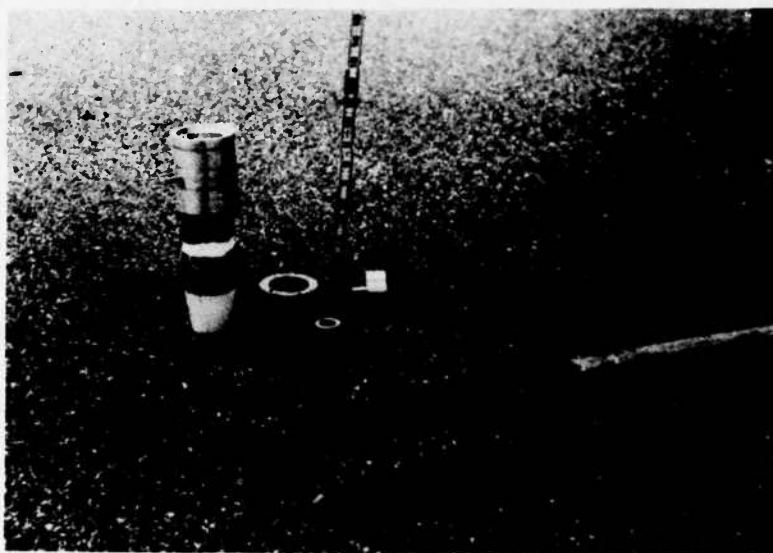


**(b) Extract Cores**

**Figure B-5. Gage Installation Procedure**



**(c)** Drill Hole to about 14 feet

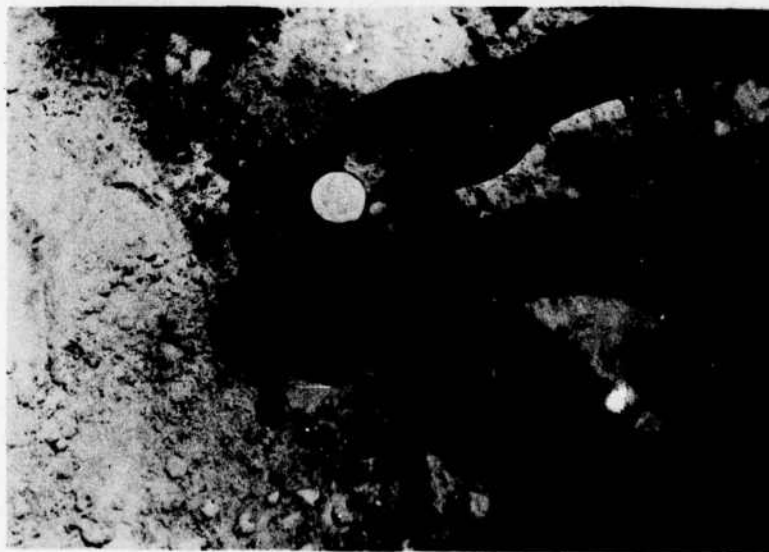


**(d)** Paraphernalia Ready for Installation in Hole

**Figure B-5. (Continued)**



**(e) Lower Rod, Anchor and Casing into Hole**

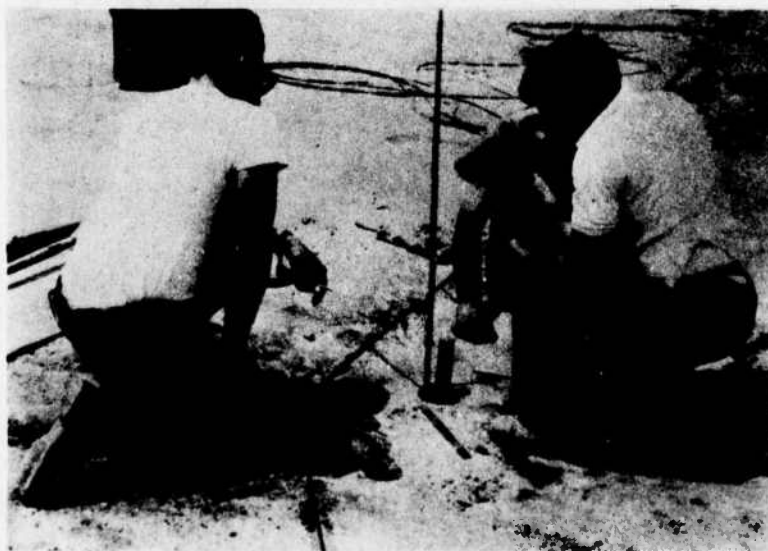


**(f) Screw Impact Head to Inner Rod**

**Figure B-5. (Continued)**



(g) Backfill with Sand and Compact



(h) Drive out Anchor Prongs

Figure B-5. (Continued)



(i) Position Upper Paraphernalia

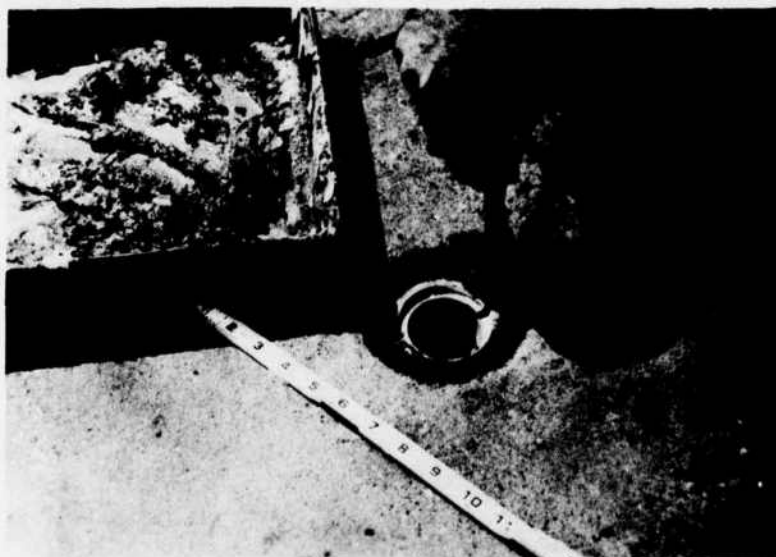


(j) Backfill Around Upper Paraphernalia

Figure B-5. (Continued)



(k) Groove Pavement



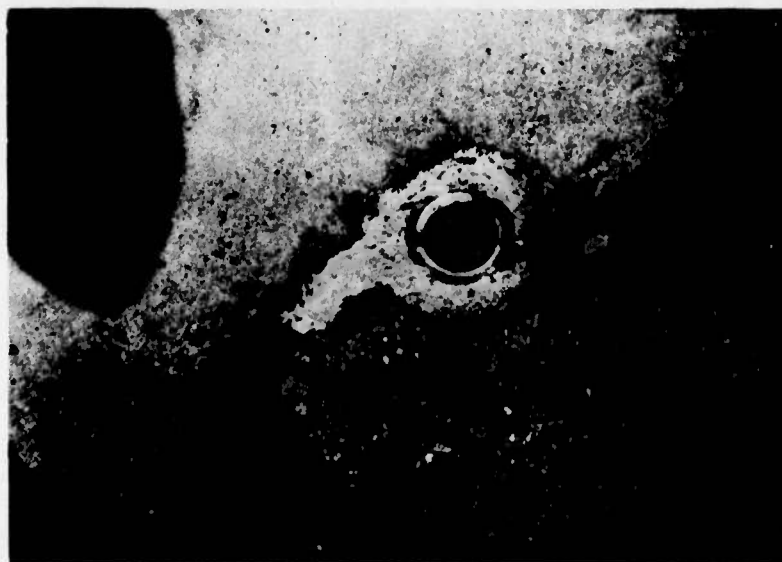
(l) Epoxy Upper Paraphernalia to Asphaltic Concrete

Figure B-5. (Continued)





(m) Epoxy Cables for LVDT into Groove



(n) Typical Installation-Partially Epoxied Cables

Figure B-5. (Continued)



(o) Epoxy Cable in Groove to Edge of Pavement



(p) Gages Ready for Element (Sensor) Installation

Figure B-5. (Concluded)



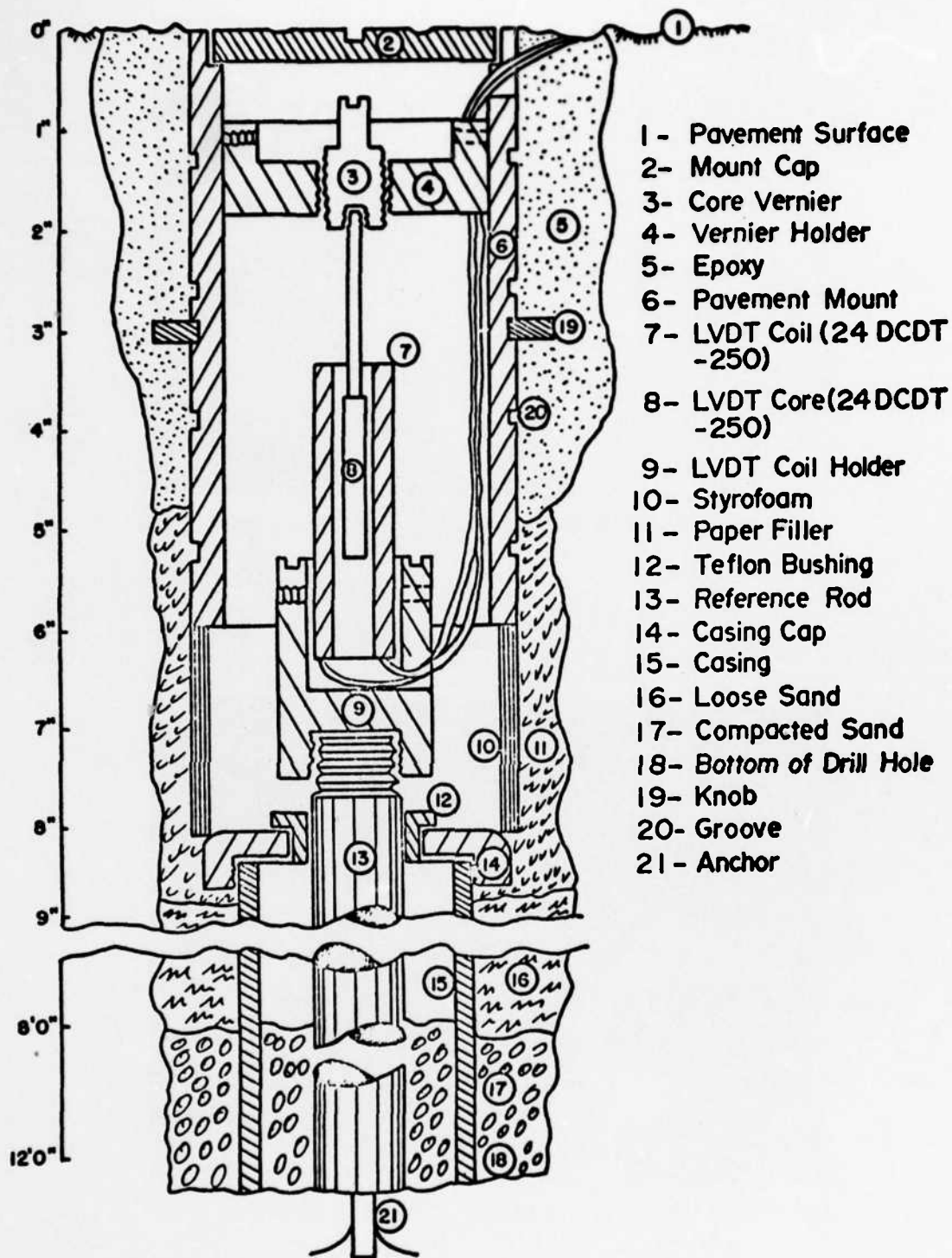
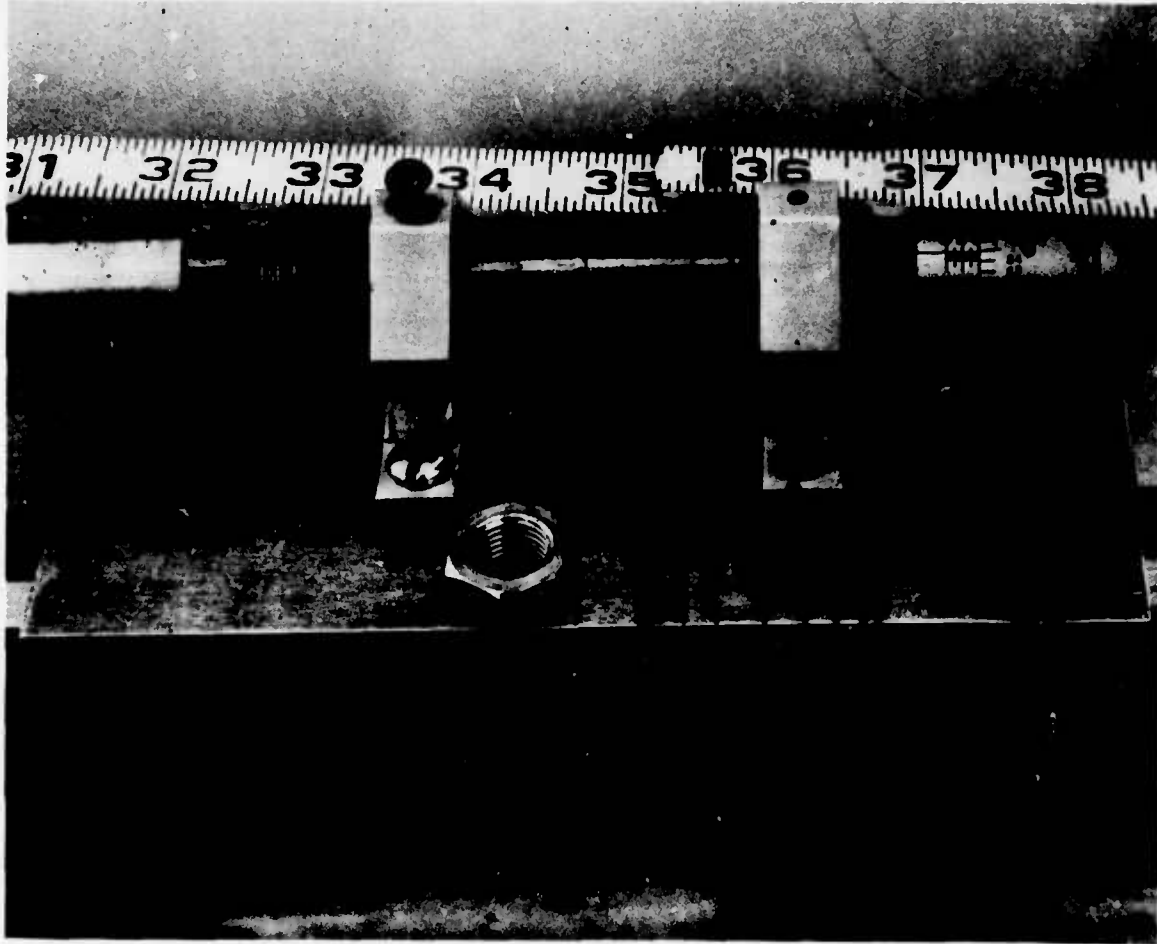
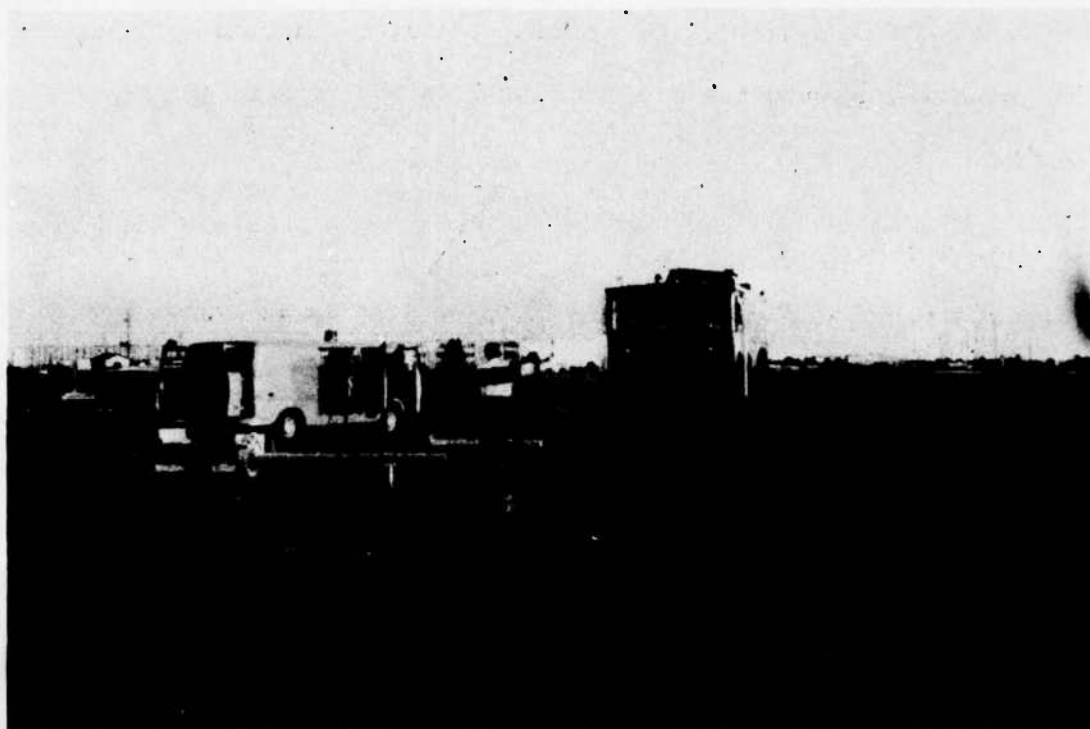


Figure B-6. Gage Installation (after Boyer [Reference 12])



**Figure B-7. Calibration Equipment for LVDT Gages**



**Figure B-8. Photo of P-2 Fire Truck Making a Pass During LVDT Beam Testing**

At the locations shown in Figure B-1(b) and B-3(b), attempts were also made to estimate the pavement transfer function by dropping a 60 pound weight onto the pavement close to the gage at the tip of the beam.

b. Pease Air Force Base

One site, on the main runway, was tested at Pease AFB in New Hampshire. At this site only the LVDT beam was used to obtain measurements of pavement response functions in the manner previously described, using the P-2 fire truck and the KC-135A aircraft as prime movers. Typical deflection measurements are presented in Figures B-9 and B-10.

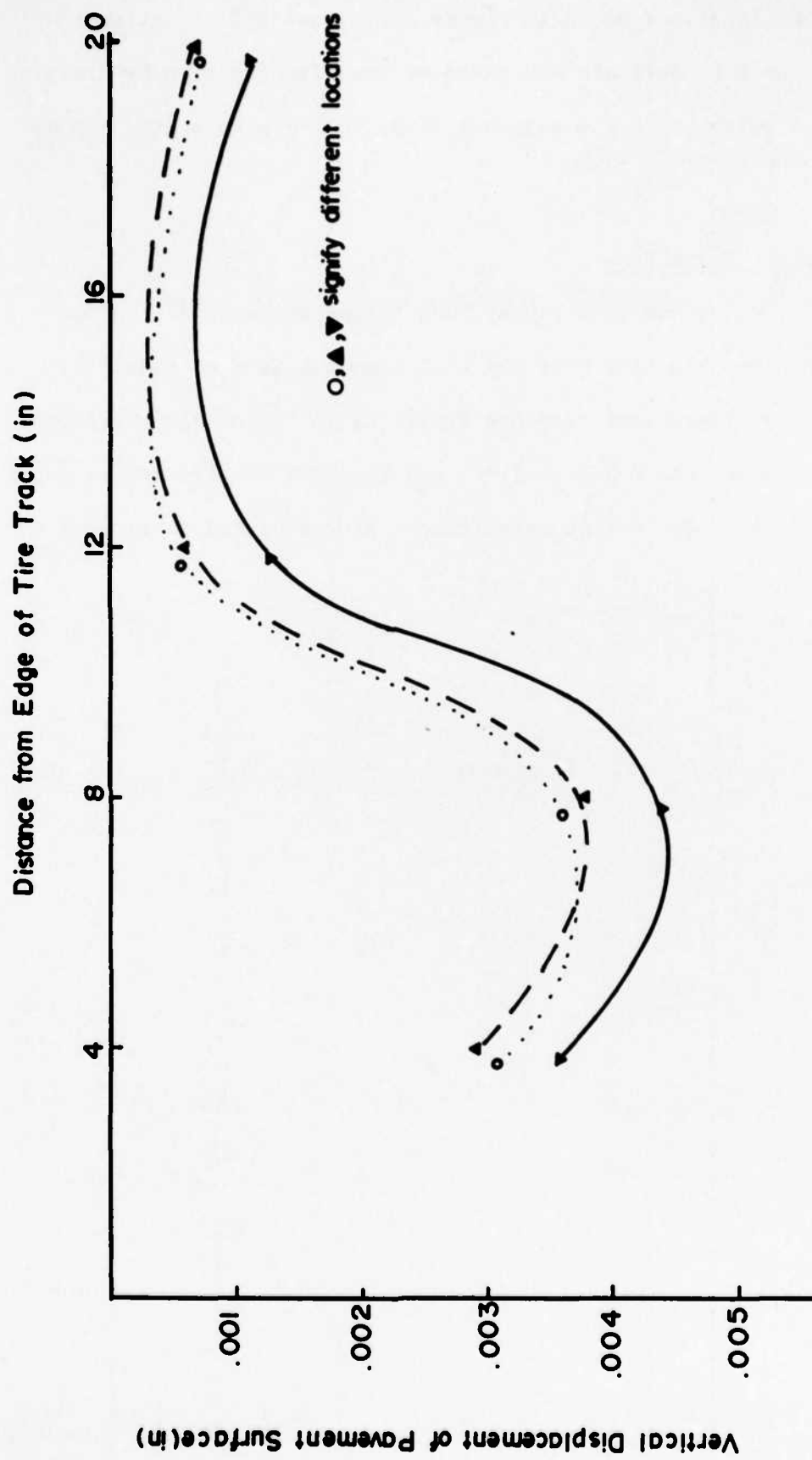


Figure B-9. Variability of Maximum Vertical Displacement of Pavement with Distance from Edge of Track of Tire Closest to Gage : KC-135 A

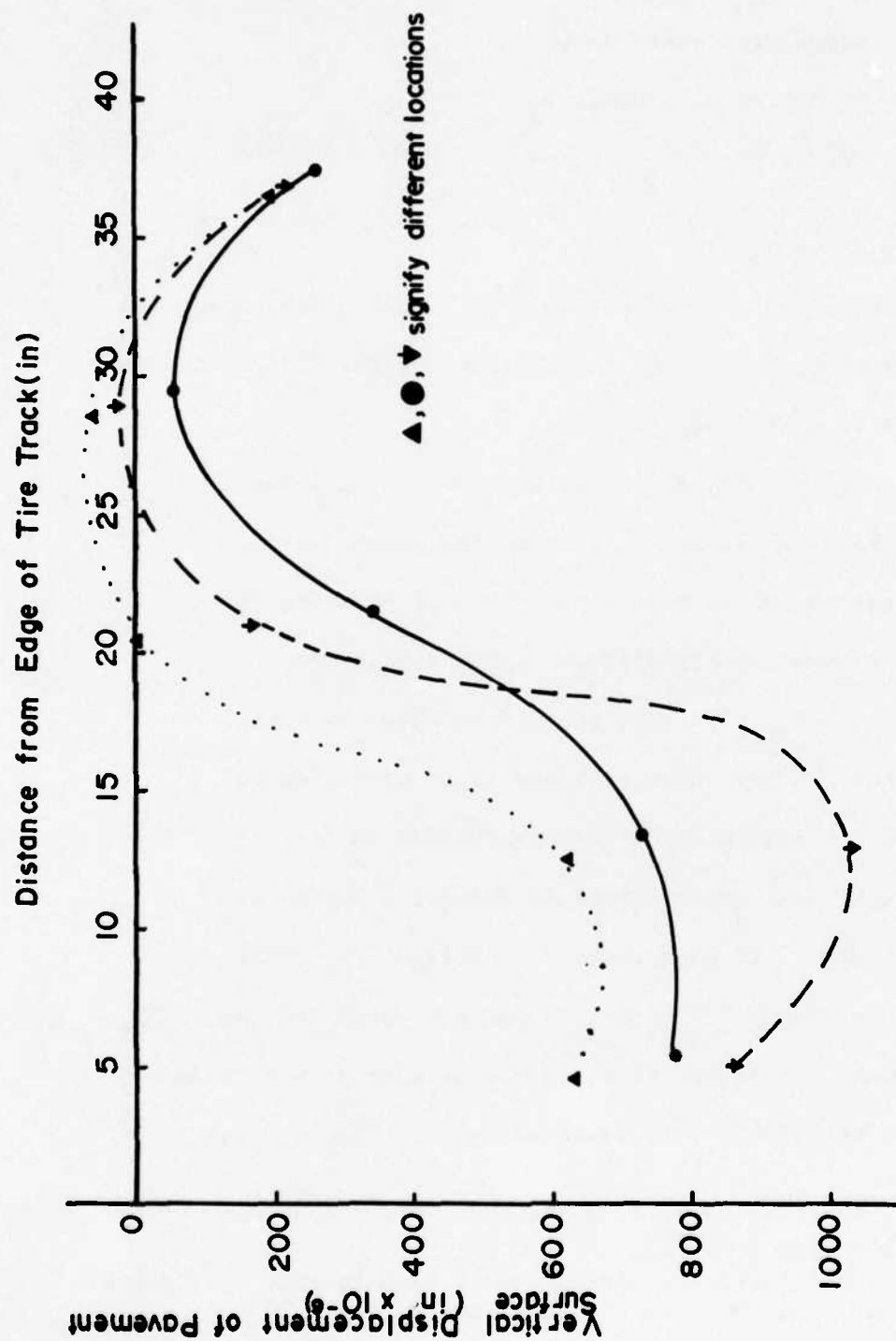


Figure B-10. Variability of Maximum Vertical Displacement of Pavement with Distance from Edge of Track of Tire Closest to Gage: P2 Fire Truck

APPENDIX C  
COMPUTER PROGRAMS

This Appendix contains the details of the computer program for,

1. Signature determination
2. Parameter determination
3. Prediction

a. Signature Determination

The signature as defined in the text is calculated using the equations (3) through (10) and the subroutines EXACFIT and SIGNTR.

The procedure is as follows:

With reference to Figures C-1 and C-2, a value of  $r_{\text{peak}}(\text{FXP})^{17}$  is assumed (0.2) then the left hand side (FLHS) and the right hand side (FRHS) of equation 5a are calculated. Their difference TVAL(1) is then calculated.  $r_{\text{peak}}(\text{FXP})$  is then incremented by 0.0125 (DFXP) and the left hand side and right hand side of equation 5a, and their difference TVAL(2) is again calculated. The ratio (FDIF) of TVAL(2) and TVAL(1) is calculated. If this ratio is positive,  $r_{\text{peak}}(\text{FXP})$  is incremented by 0.0125 (DFXP) and the ratio FDIF is again found. This procedure is repeated until the ratio is first negative. This is shown as S in Figure C-2a;

---

<sup>17</sup> Symbols in capital letters correspond to symbols used in the subroutine EXACFIT which performs the calculations.

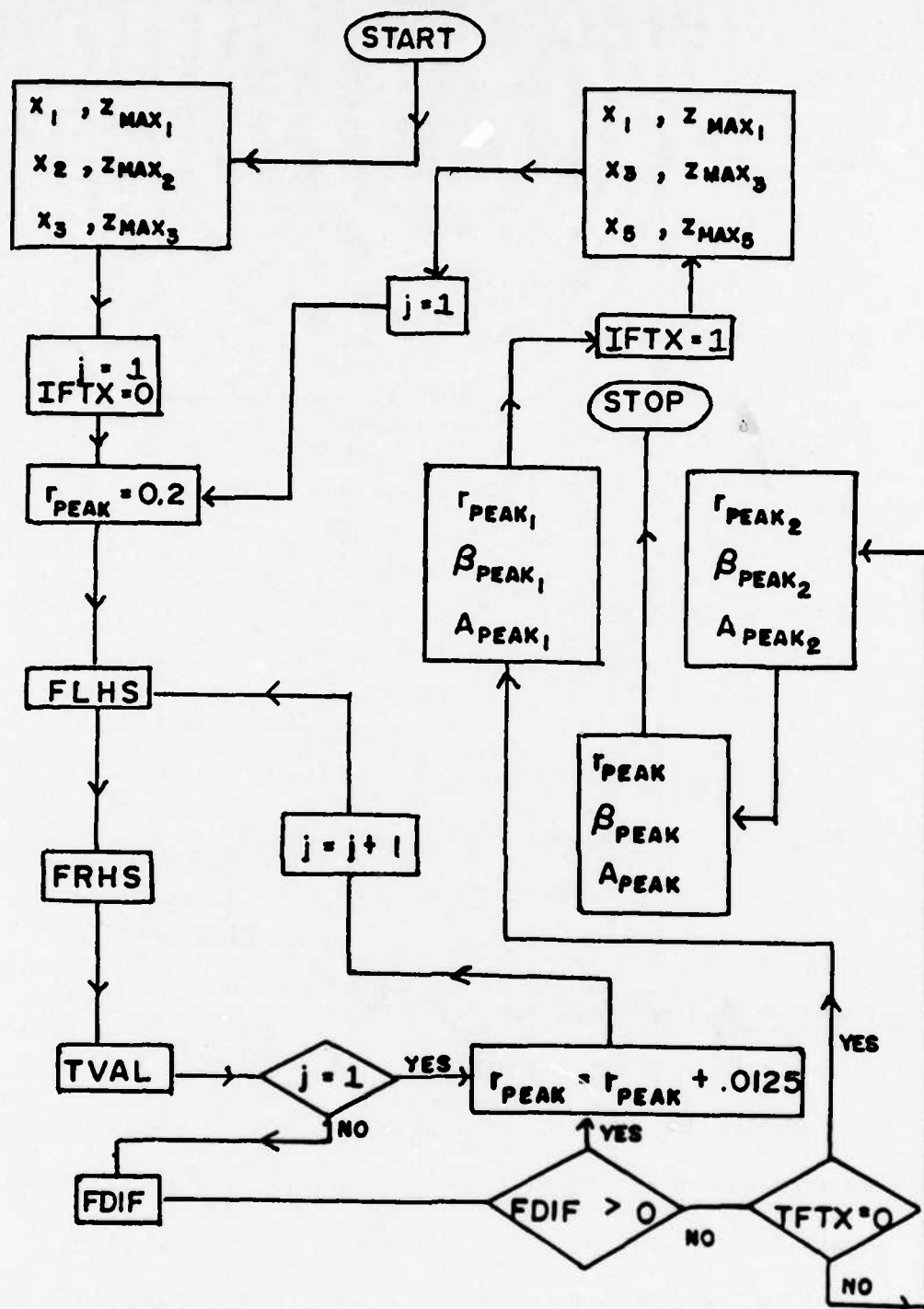
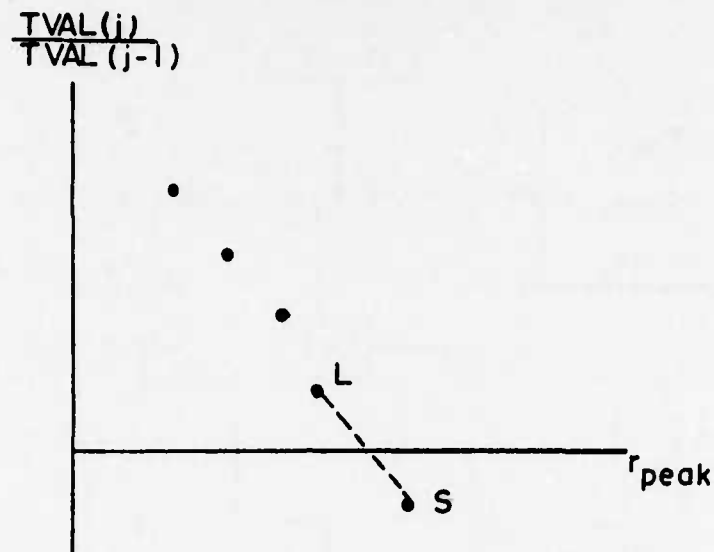
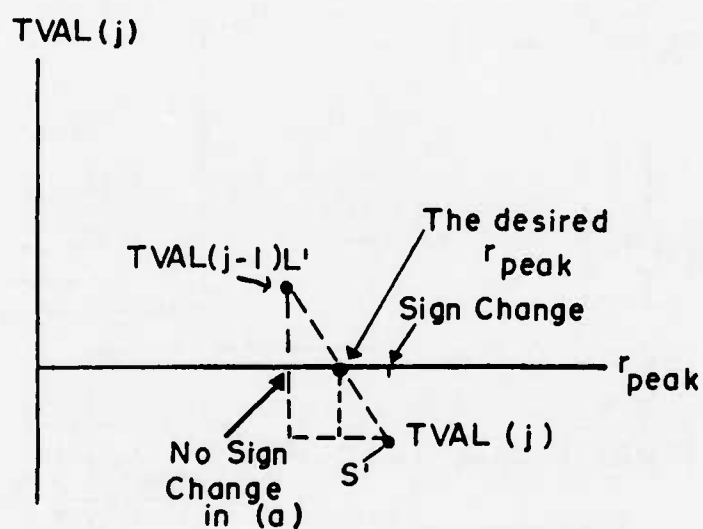


Figure C-1. Summary Flow Chart of Subroutine EXACFIT





(a)



(b)

Figure C-2. Details of Interpolation in Subgrade EXACFIT

the point immediately before, at which the ratio is positive is labelled L. In Figure C-2b, the point before the ratio becomes negative is L' and S' is the point at which the ratio is negative. The point where the difference between the left hand side and the right hand side of equation 5a is zero is found by linearly interpolating between L' and S'. With reference to Figure C-2b

$$TFDIF = | TVAL (J-1) | + | TVAL (J) |$$

$$FFXP_{\text{required}} = FXP_j - \frac{TVAL(J)}{TFDIF} \cdot DFXP = r'_{\text{peak}}$$

$\beta'_{\text{peak}}$  is then calculated from equation 5 where

$$\beta'_{\text{peak}} = \frac{\ln z_{\text{max}_1} - \ln z_{\text{max}_3}}{\frac{r'_{\text{peak}}}{x_1} - \frac{r'_{\text{peak}}}{x_2}} \quad (5a)$$

and,  $A'_{\text{peak}}$  is calculated from equation 3a

$$A'_{\text{peak}} = z_{\text{max}_1} / [\exp (\beta'_{\text{peak}} x_1^{r'_{\text{peak}}})] \quad (3a)$$

This procedure is then repeated using  $(x_1, z_1)$ ,  $(x_3, z_3)$  and  $(x_5, z_5)$  instead of  $(x_1, z_1)$ ,  $(x_2, z_2)$  and  $(x_3, z_3)$ , and values of  $r''_{\text{peak}}$ ,  $\beta''_{\text{peak}}$  and  $A_{\text{peak}}$  are calculated.

The desired  $r_{\text{peak}}$ ,  $\beta_{\text{peak}}$  and  $A_{\text{peak}}$  are found as the average of the values using the equations,

$$r_{\text{peak}} = (r'_{\text{peak}} + r''_{\text{peak}})/2$$

$$\beta_{\text{peak}} = (\beta'_{\text{peak}} + \beta''_{\text{peak}})/2$$

$$A_{\text{peak}} = (A'_{\text{peak}} + A''_{\text{peak}})/2$$

The  $A_{\text{peak}}$ ,  $r_{\text{peak}}$ , and  $\beta_{\text{peak}}$  values thus calculated are the parameters describing the maximum lateral deflection profile.

The signature is then calculated using the  $r_{\text{peak}}$ , and  $\beta_{\text{peak}}$  parameter and the basic equation, equation 2a but in the form

$$A(t) = z(t)/\exp(\beta_{\text{peak}} x_1^{r_{\text{peak}}}) \quad (10)$$

where  $z(t)$  refers to the deflection at gate 1 (closest to the wheel), and  $t$  is the time. Subroutine SIGNTR performs these computations by direct substitution of  $z(t)$ ,  $x_1$ ,  $r_{\text{peak}}$  and  $\beta_{\text{peak}}$  in equation (10).

#### b. Parameter Determination

The  $k$ ,  $c$  and  $m$  parameters as defined by equation (1) in the text are calculated using the methodology, concepts and equations presented in Section III in the paragraph with subheading "Parameter Determination". The subroutines EXACT1, NWCONV, SIGNTR, and EXACFIT are called from the main program FNDPRM in order to perform the necessary computations.

With reference to Figure C-3 and Figure C-4, initially, a value of the spring constant  $k$  is assumed where

$$k = EQKA = AAI \times PMAX/DMAX \quad (29)$$

where  $AAI^{18} = 0.05$

$PMAX = 25000$ , and

$DMAX = \text{Maximum value of the signature.}$

---

<sup>18</sup> For convenience, the symbols in capitol letters in section (4) are the same symbols used in the computer program FNDPRM.

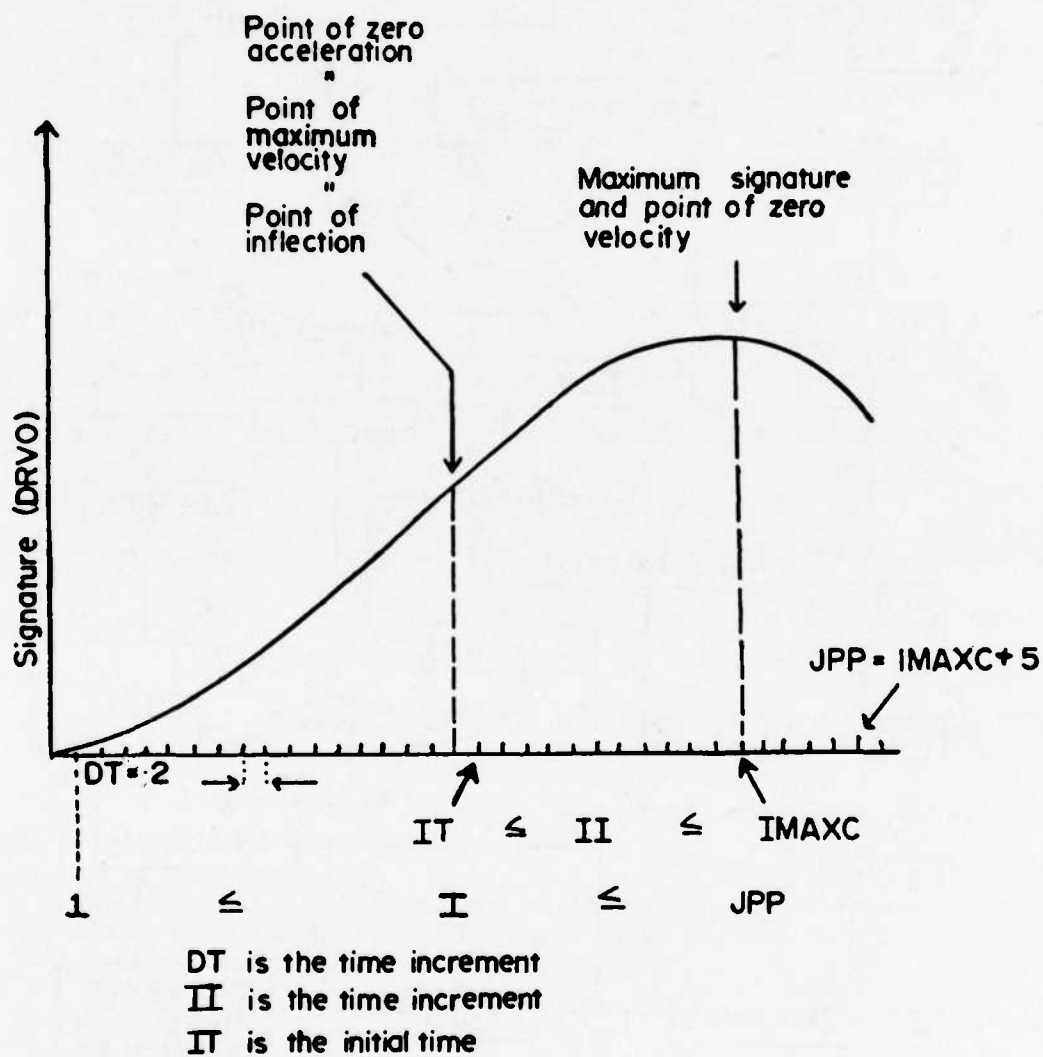


Figure C-3. Definition Sketch for Signature

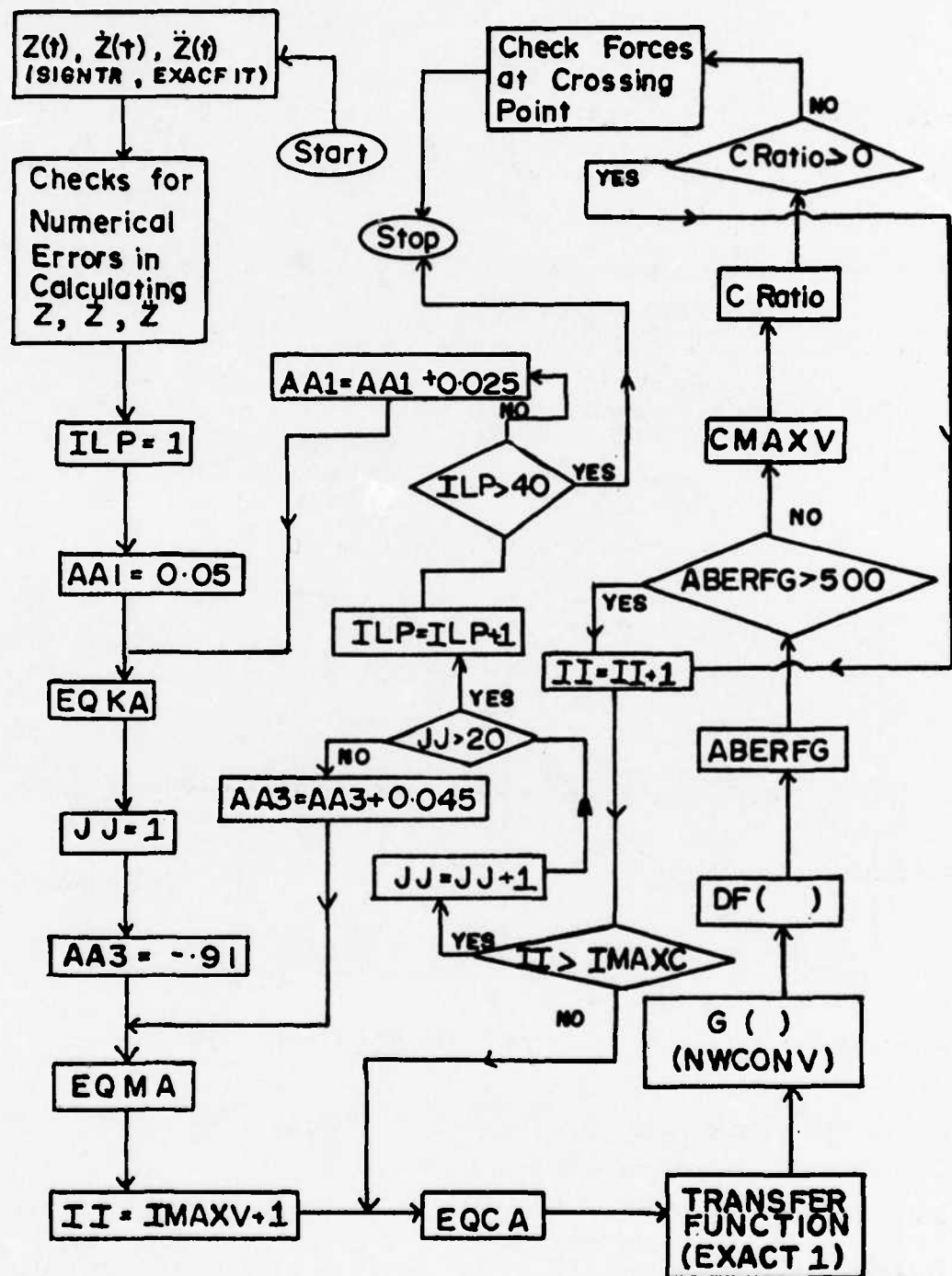


Figure C-4. Summary Flow Chart of Program FNDPRM

Then a value of  $m$  is calculated using the equation

$$m = EQMA = AA3 \times PMAX / DRV2 (IMAXD) \quad (30)$$

where  $DRV2 (IMAXD)$  is the acceleration at maximum deflection and  $AA3 =$

.91. Equation 30 is derived as follows: Let

$$k = AA1 \times PMAX / DMAX \quad (29)$$

at maximum deflection, i.e., section (3), Figure 7. Using a constant  $AA2$ , the equation

$$\begin{aligned} AA2 \times PMAX &= EQMAXDRV2(IMAXD) + EQKA \times DMAX \\ &= EQMAXDRV2(IMAXD) + AA1 \times PMAX \end{aligned}$$

is obtained. Therefore

$$\begin{aligned} AA2 \times PMAX - AA1 \times PMAX &= EQMAXDRV2(IMAXD) \\ (AA2 - AA1)PMAX &= EQMA \times DRV2(IMAXD) \end{aligned} \quad (31)$$

Letting,  $AA3 = AA2 - AA1$  yields

$$m = \frac{AA3 \times PMAX}{DRV (IMAXD)} = EQMA$$

Next a value of  $c$  is calculated using equation (32) where

$$c = EQCA = EQMA \times DRV2(II) / DRV1(II) \quad (32)$$

where  $DRV1(II)$  is the velocity at time increment  $II$  (Figure C-3). The initial value of  $II$  corresponds to the point of zero acceleration + 1 (Figure C-3). Using the initial value of  $k$ ,  $m$  and  $c$  calculated using equation (29), (30) and (32) respectively, the transfer function is

calculated using equation (11a) or (11b) whichever is applicable.

Subroutine EXACT1 performs this computation.

Next the value of  $\frac{F(t)}{m}$  (equation 33) is calculated using the discrete implicit form of the convolution integral equation (34)

$$O(t) = \int_0^t I(t-\tau) \cdot G(\tau) d\tau \quad (33)$$

where

$$I(t) = \frac{F(t)}{m}$$

Its implicit form is

$$I(i) = O(i)/\Delta T - \sum_{m=1}^{k=i-1} G(\tilde{m}) \cdot I(k+2-\tilde{m}) \quad (34)$$

where the initial value of  $i$  is 2, and  $I(1) = \frac{O(1)}{I(i) \cdot \Delta T}$  (34a)

$G(\tau)$  is the transfer function and  $\Delta T$  is the time increment. Subroutine NWCONV performs these calculations.

Next  $F(t)$ , the equivalent input function, is calculated using the equation

$$F(t) = m \times I(t) = DF(I) \quad (34a)$$

The maximum value CPMAX of  $F(t)$ , is then found and compared with 25,000 lbs. If

$$ABERFG = |CPMAX - 25000| > 500 \quad (35)$$

then  $II$  is incremented by 1, and the procedure subsequent to that step is repeated using the  $DRV2(II)$  and  $DRV1(II)$  values corresponding to

the new II. ILP, JJ and II are counters which have maximum values of 40, 20 and IMAXC (Figure C-3) respectively. These counters ensure that the tested range of values for AAI is from .05 to 1.05, for AA3 it is from -.91 to -.01, and for II it is from the first point after the point of inflection to the maximum deflection (Figure C-3). If

$$ABERFG = |CPMAX-25000| < 500 \quad (35b)$$

then c is calculated using the equation for section (1), Figure 9, equation 36

$$CMAXV = (ZVALUF - EQKA * ZVALVO) / ZVALU1 \quad (36)$$

where CMAXV = c

ZVALUF = force at section (1) (Figure 7)

EQKA = k

ZVALVO = the deflection at section (1) (Figure 7)

ZVALU1 = the velocity at section (1) (Figure 7)

The ratio given by equation (37) is next calculated

$$CDIFFR = (CMAXV - EQCA) / CMAXV \quad (37)$$

where EQCA is the c value computed in equation (32). For the first value of CDIFFR, the procedure increments II by 1 and repeats all the steps from that point. For the second and subsequent values of CDIFFR, the ratio of the current and the preceding value is calculated using the equation

$$CRATIO = QC(ICC) / QC(ICC-1) \quad (38)$$



where QC(ICC) refers to the current ratio of CDIFFR, AND QC(ICC - 1) refers to the preceding ratio of CDIFFR. If

$$\text{CRATIO} > 0$$

then the difference between the c values computed from two independent equations, equation (32) at the crossing point, and equation (36) at the point of inflection, has not passed through zero, so II is incremented and the subsequent steps are repeated. If

$$\text{CRATIO} < 0$$

then the difference between the c values calculated by equations (32) and (36) has passed through zero and the c values calculated using these two equations are approximately the same.

It has been found that the two controls, namely,

$$\text{ABERFG} < 500, \text{ and,}$$

$$\text{CRATIO} < 0$$

ensures that the conditions stated in paragraph 3.2.2, are satisfied.

Finally, the exact solution for the force is calculated by substitution EQCA, EQKA, EQMA, DRVO, DRV1, and DRV2 in the equation,

$$\text{CMPXX(I)} = \text{EQKA} \times \text{DRVO(I)} \times \text{EQMC} \times \text{DRV1(I)} + \text{EQMA} \times \text{DRV2(I)} \quad (39)$$

where CPMXX(I) is the force at each time increment I in the record. The force at the crossing point calculated by the convolution and substitution technique are computed. A listing of the program FNDPRM and a typical output is given at the end of this Appendix.

c. Prediction

The subroutines EXACFT, SIGNTR, NWCONV, EXACT 1, ERECT2, and MODPRM are used by the main program PREDCT to predict the signature of a vehicle (Vehicle A) at a site (site I) over which the vehicle has not traversed. It is required to know the signatures of vehicle A at another site (standard site), and a standard vehicle (vehicle B) at both the standard site and site I. Since details of the methodology for determining the parameters of the transfer function, the loading function, and the equivalency function has been detailed previously only a summary flow chart of program PREDCT is given here. Figure C-5 shows the summary flow chart of program PREDCT. A listing of the program and a typical output is given in the following pages of this Appendix.

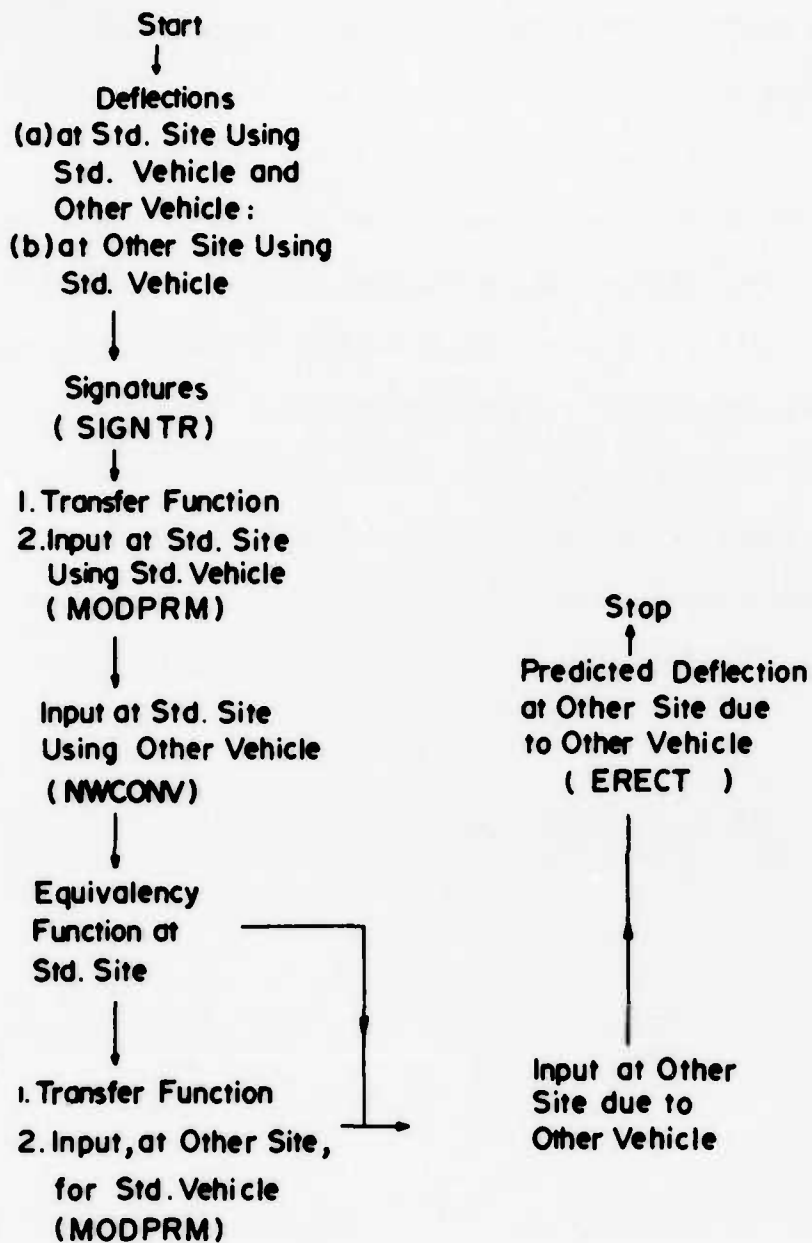


Figure C-5. Summary Flow Chart of Program PREDCT

```

1.  C-----
    C  PROGRAM FNDPRM(INPUT,OUTPUT,TAPE5=INPUT,TAPE6=OUTPUT,PLOT)
    C
    C      THIS PROGRAM COMPUTES PARAMETERS OF THE
    C      REDUCED TRANSFER FUNCTION
    C      FROM DEFLECTIONS MEASURED AT 5 POSITIONS
    C      PERPENDICULAR TO THE DIRECTION OF TRAVEL
    C      OF THE LOAD VEHICLE
    C-----
    C
    C      SUBROUTINES REQUIRED
    C          (1) EXACT1
    C          (2) NWCONV
    C          (3) EXACFIT
    C          (4) SIGNTR
    C
    C      INPUT-  NR--NUMBER OF RECORDS
    C              JM--NUMBER OF GAGES
    C              AIN--DISTANCE OF GAGE FROM OUTER EDGE OF TIRE PR
    C              NP--NUMBER OF DATA POINTS
    C              PT--TIME INCREMENT IN SECONDS
    C              WMAX--MAXIMUM WHEEL LOAD USED
    C              INITX--DIGITIZED DATA
    C              CALG--CALIBRATION DATA
    C
2.  C      DIMENSION FRESP(11,100,5),INITX(11,100,5),CALG(11,5),NP(11),PT(11)
    C      1,WMAX(11),DRV0(100),GMAX(11,5)
3.  C      DIMENSION VIPY(200),VISIG(200)
4.  C      DIMENSION AI(5),FI(5)
5.  C      DIMENSION AIN(5,11)
6.  C      DIMENSION QC(2000)
7.  C      DIMENSION APK(100),BT(100),TXPON(100)
8.  C      DIMENSION FR(10),DFY(10),FRR(10,6)
9.  C      DIMENSION DF(200)
10. C      DIMENSION T(200)
11. C      DIMENSION D(200),GG(200)
12. C      DIMENSION V(200),G(200)
13. C      DIMENSION IVEL(11,5)
14. C      DIMENSION DRV1(200),DRV2(200),CPMXX(50)
    C
15. C      READ(5,804)NR,JM
16. C      DO 810 K=1,NR
17. C      READ(5,29)(AIN(J,K),J=1,JM)
18. C      READ(5,801)NP(K),PT(K),WMAX(K)
19. C      JP=NP(K)
20. C      DO 800 I=1,JP
21. C      READ(5,802)(INITX(K,I,J),J=1,5)
22. C      800 CONTINUE
23. C      READ(5,803)(CALG(K,J),J=1,5)
24. C      810 CONTINUE
25. C      801 FORMAT(15,2F10.4)
26. C      802 FORMAT(5(14,2X))
27. C      803 FORMAT(5F12.10)
28. C      804 FORMAT(2I10)
29. C      29 FORMAT(6F10.5)
    C
    C*****RECORDS RUN
    C*****
    C      EGLIN      SITE 1      LOC B-4      LD. CT.      3.10.76      3.0 .2      46
    C*****
    C*****
    C
    C      TOP OF MAIN LOOP THAT OPERATES ON ONE RECORD AT A TIME
    C
30. C      DO 811 K=1,NR
    C
    C      CALCULATES DEFLECTION RESPONSE FUNCTION FOR JM GAGES AND
    C      THE PEAK FOR EACH GAGE FOR THE K TH RECORD
    C
31. C      DO 806 I=1..JM

```

```

32.      P1(J)=AIN(J,K)
33.      RMAX=0.0
34.      JP=NP(K)
35.      DO 807 I=2,JP
36.      FRESP(K,I-1,J)=FLOAT(INITX(K,I,J)-INITX(K,1,J))*CALG(K,J)/12.
37.      VIPY(I-1)=FRESP(K,I-1,2)
38.      IF(FRESP(K,I-1,J).LT.RMAX)GO TO 807
39.      RMAX=FRESP(K,I-1,J)
40. 807 CONTINUE
41.      GMAX(K,J)=RMAX
42.      FI(J)=GMAX(K,J)
43. 806 CONTINUE
C
C      LISTS REDUCED DATA
C
44.      WRITE(6,833)
45. 833 FORMAT(1H1,40X,*NEW RECORD*//)
46.      WRITE(6,814)
47. 814 FORMAT(//1X,*NUMBER OF DATA POINTS      RECORD NUMBER
      1EEL LOAD      TIME INCREMENT      NUMBER OF GAGES*/)
48.      WRITE(6,815)NP(K),K,WMAX(K),PT(K),JM
49. 815 FORMAT(10X,I4,19X,I4,18X,F6.0,19X,F4.2,18X,I2/)
50.      WRITE(6,816)
51. 816 FORMAT(//40X,*DEFLECTIONS IN FT*//)
52.      WRITE(6,817)
53. 817 FORMAT(13X,*GAGE 1      GAGE 2      GAGE 3      GAGE 4
      1      GAGE 5*//)
54.      DO 818 I=1,JP
55.      WRITE(6,819)(FRESP(K,I,J),J=1,JM)
56. 818 CONTINUE
57. 819 FORMAT(10X,5(F7.5,10X))
58.      WRITE(6,820)
59. 820 FORMAT(//40X,*PEAK DEFLECTIONS*//)
60.      WRITE(6,819)(GMAX(K,J),J=1,JM)
C-----
C      FIT MEASURED PEAK LATERAL DEFLECTION PROFILE TO
C      EQUATION USING SUBROUTINE EXACFIT
C-----
C
61.      CALL EXACFIT(FI,TFXP,TBETAF,FAF,AI)
C
62.      APK(K)=FAF
63.      BT(K)=TBETAF
64.      TXPUN(K)=TFXP
C
65.      VBETA=TBETAF
66.      VRVAL=TFXP
67.      VIPX=AIN(2,K)
68.      NV=JP
C-----
C      CALCULATE SIGNATURE OF PROTOTYPE USING
C      SUBROUTINE SIGNTR
C-----
C
69.      CALL SIGNTR(VBETA,VRVAL,VIPX,VIPY,VISIG,NV)
C-----
C      CALCULATE FIRST AND SECOND DERIVATIVES
C-----
70.      DO 74 I=1,JP
71.      DRV0(I)=VISIG(I)
72.      TRM1=(VISIG(I)+VISIG(I+1))/2.
73.      IF(I.EQ.1)TRM2=VISIG(I)/2.
74.      TRM2=(VISIG(I)+VISIG(I-1))/2.
75.      DRV1(I)=(TRM1-TRM2)/PT(K)
76. 74 CONTINUE
77.      DO 75 I=1,JP
78.      TRN1=(DRV1(I+1)+DRV1(I))/2.
79.      IF(I.EQ.1)TRN2=DRV1(I)/2.
80.      TRN2=(DRV1(I)+DRV1(I-1))/2.
81.      DRV2(I)=(TRN1-TRN2)/PT(K)
82. 75 CONTINUE
C-----
C      IDENTIFY FIRST PEAK BY FINDING POINT WHERE FIRST
C      DERIVATIVE CHANGES SIGN

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C-----
83.      BOTM=0.0000000001
84.      DO 726 I=1,JPP
85.      HUMP1=DRV0(I+1)-DRV0(I)
86.      IF(HUMP1.GE.0.0)GO TO 726
87.      JPP=I+6
88.      GO TO 727
89.      726 CONTINUE
90.      727 CONTINUE

C-----
C      REPLACE ZEROES BY AVERAGING BEFORE AND AFTER POINTS
C-----
91.      IMAXV=0
92.      DV1MX=0.0
93.      DO 315 I=1,JPP
94.      IF(DRV1(I).EQ.0.0)DRV1(I)=(DRV1(I+1)+DRV1(I-1))/2.
CAUTION - IS FLOATING POINT EQUALITY TO BE EXPECTED
95.      IF(DRV1(I).EQ.0.0)DRV1(I)=(DRV1(I+2)+DRV1(I-2))/2.
CAUTION - IS FLOATING POINT EQUALITY TO BE EXPECTED
96.      IF(ABS(DRV1(I)).LT.BOTM)DRV1(I)=(DRV1(I+1)+DRV1(I-1))/2.
97.      IF(ABS(DRV2(I)).LT.BOTM)DRV2(I)=(DRV2(I+1)+DRV2(I-1))/2.
98.      IF(DRV1(I).LT.DV1MX)GO TO 315
99.      DV1MX=DRV1(I)
100.     IMAXV=I
101.     315 CONTINUE

C-----
C      FIND MAXIMUM VALUE OF SIGNATURE
C-----
102.     DMAX=DRV0(I)
103.     DO 53 I=2,JPP
104.     IF(DRV0(I).LT.DMAX)GO TO 53
105.     DMAX=DRV0(I)
106.     IMAXD=I
107.     53 CONTINUE

C-----
C      REPLACE ERRONEOUS ACCELERATIONS BY AVERAGING
C      BEFORE AND AFTER POINTS
C-----
108.     IMAXV1=IMAXV-1
109.     DO 57 I=2,IMAXV1
110.     IF(DRV2(I).LE.0.0)DRV2(I)=(DRV2(I-1)+DRV2(I+1))/2.
111.     IF(DRV2(I).LE.0.0)DRV2(I)=(DRV2(I-2)+DRV2(I+2))/2.
112.     57 CONTINUE
113.     IMAXVA=IMAXV+1
114.     DO 109 I=IMAXVA,JPP
115.     IF(DRV2(I).GE.0.0)DRV2(I)=(DRV2(I-1)+DRV2(I+1))/2.
116.     IF(DRV2(I).GE.0.0)DRV2(I)=(DRV2(I-2)+DRV2(I+2))/2.
117.     109 CONTINUE
118.     DO 107 I=1,JPP
119.     IF(DRV1(I+1).EQ.DRV1(I))DRV1(I+1)=(DRV1(I+2)+DRV1(I))/2.
CAUTION - IS FLOATING POINT EQUALITY TO BE EXPECTED
120.     IF(DRV2(I+1).EQ.DRV2(I))DRV2(I+1)=(DRV2(I+2)+DRV2(I))/2.
CAUTION - IS FLOATING POINT EQUALITY TO BE EXPECTED
121.     107 CONTINUE

C-----
C      FIND TIME INTERVAL WHERE VELOCITY CHANGES SIGN
C      AND FRACTION OF VELOCITY TO ZERO BY
C      LINEAR INTERPOLATION
C-----
122.     DO 789 IA=1,JPP
123.     DEROTS=DRV1(IA+1)/DRV1(IA)
124.     IF(DEROTS.GT.0.0)GO TO 789
125.     DZERO=DRV1(IA)-DRV1(IA+1)
126.     DDTZ=DRV1(IA)/DZERO
127.     NAFNL=IA
128.     GO TO 788
129.     789 CONTINUE
130.     788 CONTINUE

C-----
C      FIND INTERVAL AND TIME WHERE ACCELERATION IS
C      ZERO AND THE CORRESPONDING DISPLACEMENT
C      AND VELOCITY
C-----
131.     DO 889 IA=1,JPP
132.     ZEROTS=DRV2(IA+1)/DRV2(IA)

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133.      IF(ZERO'S.GT.0.0)GO TO 889
134.      TZERO=DRV2(IA)-DRV2(IA+1)
135.      FDTZ=DRV2(IA)/TZERO
136.      IAFNL=IA
137.      DRORNG=DRV0(IA+1)-DRV0(IA)
138.      ZVALU0=DRV0(IA)+FDTZ*DRORNG
139.      DR1RNG=DRV1(IA+1)-DRV1(IA)
140.      ZVALU1=DRV1(IA)+FDTZ*DR1RNG
141.      GO TO 888
142.      889 CONTINUE
143.      888 CONTINUE
C
C*****
144.      WRITE(6,99)
145.      99 FORMAT(/37X, 'FOR SIGNATURE'/)
146.      WRITE(6,76)
147.      76 FORMAT(/7X, '      INCREMENT      SIGNATURE      VELOCITY      ACCEL
148.      1ERATION'/)
149.      WRITE(6,77)(I, DRV0(I), DRV1(I), DRV2(I), I=1, JPP)
150.      77 FORMAT(7X, I4, 3E15.5)
151.      WRITE(6,1091)
152.      1091 FORMAT(//////////1X, '0'/)
153.      IMAXF=0
154.      PMAX=IMAX(K)
155.      AA1=0.05
156.      ICC=0
C-----
C      TOP OF LOOP INCREMENTING AA1
C-----
156.      DO 104 ILP=1,40
157.      EQKA=AA1*PMAX/DMAX
158.      AA3=-0.91
C-----
C      TOP OF LOOP INCREMENTING AA3
C-----
159.      DO 103 JJ=1,20
160.      IT=IMAXV
161.      EQMA=AA3*PMAX/DRV2(IMAXD)
162.      CPMAX=0.0
163.      AA2=AA1+AA3
164.      IF(AA2.LT.0.0)GO TO 1021
165.      IMAXC=IMAXD
166.      IT=IT+1
C-----
C      TOP OF LOOP VARYING TIME BETWEEN ZERO ACCELERATION
C      AND ZERO VELOCITY AND CALCULATING EQCA
C      FOR EACH INCREMENT
C-----
167.      DO 102 II=IT,IMAXC
168.      EQCA=EQMA*DRV2(II)/DRV1(II)
169.      EQCA=-EQCA
C
C
170.      EQVK=EQKA
171.      EQMASS=EQMA
172.      EQVC=EQCA
173.      MM=JPP
174.      DT=PT(K)
C-----
C      CALCULATING REDUCED TRANSFER FUNCTION USING
C      SUBROUTINE EXACT1
C-----
175.      CALL EXACT1(MM,DT,EQVK,EQMASS,T,GG,EQVC)
C
176.      DO 73 I=1,JPP
177.      D(I)=DRV0(I)
178.      V(I)=GG(I)
179.      73 CONTINUE
180.      N=JPP
C-----
C      CALCULATE I(T) USING SUBROUTINE NWCONV
C      BY IMPLICIT CONVOLUTION
C-----
C

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```

181.      CALL NUCONV(N,V,G,D,DT)
      C
      C-----
      C          CALCULATING EQUIVALENT FORCE AS PRODUCT OF
      C          I(T) AND EQMASS
      C-----
182.      DO 508 MP=1,JPP
183.      DF(MP)=G(MP)*EQMASS
184.      508 CONTINUE
185.      DO 509 MA=1,JPP
186.      DF(MA)=(DF(MA)+DF(MA+1))/2.
187.      509 CONTINUE
      C
      C-----
      C          AVERAGING AND FINDING MAXIMUM EQUIVALENT FORCE
      C-----
188.      CPMAX=0.
189.      DO 501 M=1,JPP
190.      DF(M)=(DF(M)+DF(M+1))/2.
191.      IF(DF(M).GT.CPMAX)GO TO 20
192.      GO TO 502
193.      20 CPMAX=DF(M)
194.      ICF=M
195.      502 CONTINUE
196.      501 CONTINUE
      C
      C-----
      C          EXECUTING FIRST CHECK TO ENSURE THAT THE
      C          ABSOLUTE DIFFERENCE BETWEEN THE MAXIMUM COMPUTED
      C          FORCE AND 25 KIPS IS LESS THAN 500 LBS
      C-----
197.      ERFCE=CPMAX-PMAX
198.      ABERFG=ABS(ERFCE)
199.      IF(ABERFG.GT.500.0)GO TO 102
      C
      C-----
      C          EXECUTING SECOND CHECK TO ENSURE THAT THE DIFFERENCE
      C          BETWEEN THE C VALUES COMPUTED AT THE CROSSING POINT
      C          AND THE POINT OF INFLECTION GOES THROUGH ZERO
      C-----
200.      ICC=ICC+1
201.      DFRNG=DF(IAFNL+1)-DF(IAFNL)
202.      ZVALUF=DF(IAFNL)+FDTZ*DFRNG
203.      CMAXV=(ZVALUF-EQCA*ZVALU0)/ZVALU1
204.      CDIFFR=(CMAXV-EQCA)/CMAXV
205.      ABCD=CDIFFR
206.      QC(ICC)=CDIFFR
207.      IF(ICC.EQ.1)GO TO 102
208.      CRATIO=QC(ICC)/QC(ICC-1)
209.      IF(CRATIO.GT.0.0)GO TO 102
      C
      C-----
      C          CALCULATING FORCE RATIOS COMPONENTS OF FORCE
      C          AND TOTAL FORCE AT THE CROSSING POINT
      C-----
210.      FCHK=EQCA*DRV0(II)
211.      DIFCHK=FCHK-DF(II)
212.      DFCHKR=DIFCHK/FCHK
213.      FPFAC=DF(II)/PMAX
214.      ICDPT=II
215.      TRMM=EQMA*DRV2(II)
216.      TRMC=EQCA*DRV1(II)
217.      TRMK=EQCA*DRV0(II)
218.      CPMXX(II)=TRMM+TRMC+TRMK
219.      WRITE(6,847)
220.      847 FORMAT(/10X,'GOOD RUN'//)
221.      GO TO 846
      C*****
222.      102 CONTINUE
223.      1021 CONTINUE
224.      AA3=AA3+0.045
      C*****
225.      103 CONTINUE
226.      AA1=AA1+0.025
      C*****
227.      104 CONTINUE
228.      1000 FORMAT(/1X,'000')
229.      845 FORMAT(6F15.4,10X,215,F10.3)
230.      WRITE(6,1002)

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231. 1002 FORMAT(/10X, 'OUTER LOOP COMPLETED'//)
232. GO TO 94
233. 846 CONTINUE
234. WRITE(6,1043)
235. 1043 FORMAT(//////////10X, 'INCREMENT', 2X, 'M-COMP.', 8X, 'C-COMP.', 8X, 'K-C
      1OMP.', 8X, 'EXACT', 8X, 'CONVOLUTION', 8X, 'TDT FUNC', 8X, 'SIGNATURE'//)
C-----
C          CALCULATING COMPONENTS OF FORCE DUE TO INERTIAL
C          DAMPING AND STIFFNESS
C-----
236. JPN=JPP-3
237. DO 106 I=1, JPN
238. TMT=EQMA*DRV2(I)
239. TCT=EQCA*DRV1(I)
240. TKT=EQKA*DRV0(I)
241. CPMXX(I)=TCT+TKT+TMT
242. WRITE(6,1001) I, TMT, TCT, TKT, CPMXX(I), DF(I), GG(I), DRV0(I)
243. 106 CONTINUE
C-----
C          CALCULATING FORCE RATIOS AT SECTIONS (1), (2), (3)
C-----
244. AFRNG=DF(NAFNL+1)-DF(NAFNL)
245. DVALUF=DF(NAFNL)+DDTZ*AFRNG
C*****
246. ZVALUR=ZVALUF/PMAX
C*****
247. DVALZD=DVALUF/PMAX
C*****
248. FDRTIQ=ABERFG/PMAX
C-----
C          CALCULATING TIME RATIOS AT SECTIONS(1), (2), (3)
C-----
249. DENOM=FLOAT(IMAXD)
250. DENOM1=1.0
251. TCRSPT=FLOAT(II)/DENOM
252. TZROA=FLOAT(IAFNL)/DENOM
C*****
253. WRITE(6,1041)
254. 1041 FORMAT(//////////10X, 'EQUIV. MASS', 10X, 'EQUIV. STIFFNESS', 9X, 'EQUI
      1V. DAMPING'//)
255. WRITE(6,2041)
256. 2041 FORMAT(12X, 'SLUGS', 16X, 'LBS/FT', 20X, 'LBS-SEC/FT'//)
257. WRITE(6,1042)EQMA, EQKA, EQCA
258. 1042 FORMAT(10X, F10.2, 15X, F10.2, 12X, F10.1)
259. WRITE(6,1044)
260. 1044 FORMAT(//20X, '      FORCE RATIOS(FORCE OVER 25000)'//)
261. WRITE(6,1045)
262. 1045 FORMAT(25X, 'SECTION(1) SECTION(2) SECTION(3)'//)
263. WRITE(6,1046)ZVALUR, FPFRAC, DVALZD
264. 1046 FORMAT(23X, F10.3)
265. WRITE(6,1050)
266. 1050 FORMAT(//20X, '      TIME RATIOS(TIME OVER TIME TO MAX. DEF.)'//)
267. DENOM1=1.
268. WRITE(6,1045)
269. WRITE(6,1046)TZROA, TCRSPT, DENOM1
270. WRITE(6,1060)
271. 1060 FORMAT(//20X, 'C-PARAMETER DIFFERENCE RATIO'//)
272. WRITE(6,1061)CDIFFR
273. 1061 FORMAT(30X, F7.3)
274. WRITE(6,1070)
275. 1070 FORMAT(//20X, 'FORCE DIFFERENCE RATIO AT THE CROSSING POINT'//)
276. WRITE(6,1061)DFCHKR
277. WRITE(6,1080)
278. 1080 FORMAT(//20X, 'MAXIMUM FORCE DIFFERENCE'//)
279. WRITE(6,1061)ABERFG
280. 1001 FORMAT(10X, I5, 7F15.5)
C-----
281. 811 CONTINUE
282. 94 CONTINUE
C
283. STOP
284. END
C

```

```

-----C-----
1.      SUBROUTINE EXACFIT(FI,TFXP,TBETAF,FAF,AI)
C
C          THIS SUBROUTINE CALCULATES THE PARAMETERS OF THE
C          MAXIMUM LATERAL DEFLECTION PROFILE USING
C          THE DEVELOPED INTERPOLATION-ITERATION PROCEDURE
C-----C-----
C          INPUT-   FI--MEASURED DEFLECTIONS AT LOCATIONS LATERAL
C                   TO THE TIRE PRINT
C                   AI--LATERAL DISTANCES FROM EDGE OF TIRE PRINT
C                   CORRESPONDING TO FI
C          OUTPUT   TFXP--R PARAMETER
C                   TBETAF--BETA PARAMETER
C                   FAF--A PARAMETER
C
2.      DIMENSION FI(6),TBETA(3),TVAL(999),AI(5),FA(5),FFXP(5)
C$      TRACE SUBSCRIPTS
C$      TRACE ARITHMETIC
3.      M=1
4.      IFTX=0
5.      I=2
6.      IG=I+1
7.      IM=I+2
8.      ITRID=0
C
C*****
C*****
C
9.      710 CONTINUE
10.     FXP=0.2001
11.     DFXP=0.0125
12.     J=0
13.     771 CONTINUE
14.     J=J+1
15.     FXP=FXP+DFXP
16.     IFCHK=0
17.     772 CONTINUE
18.     776 CONTINUE
19.     CONS1=ALOG(FI(I))-ALOG(FI(IG))
20.     CONS2=ALOG(FI(I))-ALOG(FI(IM))
21.     CONF=CONS1/CONS2
22.     FLHS=CONF*((AI(I)**FXP)-(AI(IM)**FXP))
23.     FRHS=(AI(I)**FXP)-(AI(IG)**FXP)
24.     TVAL(J)=FLHS-FRHS
25.     IF(J.EQ.1)GO TO 771
26.     FDIF=TVAL(J)/TVAL(J-1)
27.     ABVAL=ABS(TVAL(J))
28.     IF(J.EQ.999)GO TO 726
29.     IF(FDIF.GT.0.0)GO TO 771
30.     TFDIF=ABS(TVAL(J-1))+ABS(TVAL(J))
31.     FFXP(M)=FXP-(TVAL(J)/TFDIF)*DFXP
32.     773 CONTINUE
C
33.     FBETA1=ALOG(FI(I))-ALOG(FI(IG))
34.     FBETA2=(AI(I)**FFXP(M))-(AI(IG)**FFXP(M))
35.     TBETA(M)=FBETA1/FBETA2
36.     FA1=TBETA(M)*(AI(1)**FFXP(M))
37.     FA(M)=FI(1)/EXP(FA1)
38.     GO TO 777
39.     IF(ITRID.EQ.1)GO TO 727
CAUTION - STATEMENT CANNOT BE EXECUTED - NO STATEMENT NUMBER
40.     IF(IFTX.EQ.1)GO TO 777
41.     M=M+1
42.     IG=IG+1
43.     IM=IM+2
44.     IFTX=1
45.     GO TO 710
46.     777 FAF=FA(M)
47.     TBETAF=TBETA(M)
48.     TFXP=FFXP(M)
49.     GO TO 728
C*****
C*****
50.     726 CONTINUE

```

```

51.      TTRID=1
52.      M=M+1
53.      IG=IG+1
54.      IM=IM+2
55.      IFTX=1
56.      IF(IM.LE.5)GO TO 730
57.      WRITE(6,731)
58. 731  FORMAT(/20X,*DATA DOES NOT FIT--CHECK DATA*/)
59.      GO TO 720
60. 730  GO TO 710
61. 727  CONTINUE
C*****
62.      FAF=FA(2)
63.      TBETAF=TBETA(2)
64.      TFXP=FFXP(2)
65. 728  CONTINUE
66.      WRITE(6,775)
67. 775  FORMAT(/20X,*  A PARAMETER      BETA      EXPONENT R*/)
68.      WRITE(6,778)FAF,TBETAF,TFXP
69. 778  FORMAT(20X,3E15.5/)
70.      WRITE(6,750)
71. 750  FORMAT(/20X,*  CALCULATED Y  *  MEASURED Y      LATERAL DIST.*/)
72.      DO 701 M=1,5
73.      YY1=TBETAF*(AI(M)**TFXP)
74.      YY2=EXP(YY1)
75.      YY=FAF*YY2
76.      WRITE(6,20)YY,FI(M),AI(M)
77. 701  CONTINUE
78. 720  CONTINUE
79. 20  FORMAT(20X,3E15.5)
C
80.      RETURN
81.      END
C
C
C
C

```

```

1.      SUBROUTINE SIGNTR(VBETA,VRVAL,VIPX,VIPY,VISIG,NV)
C
C      THIS SUBROUTINE CALCULATES THE SIGNATURE BY
C      DIRECT SUBSTITUTION
C-----
C      INPUT-      VBETA--BETA PARAMETER
C                  VIPX--LATERAL DISTANCE OF GAGE FROM OUTER
C                      EDGE OF TIRE PRINT
C                  VIPY--NV VALUES OF MEASURED DEFLECTION
C                      AT VIPX FROM OUTER EDGE OF TIRE PRINT
C                  VRVAL--R PARAMETER
C
C      OUTPUT-     VISIG--NV VALUES OF THE SIGNATURE
C
2.      DIMENSION VIPY(200),VISIG(200)
3.      VTOP=VBETA*(VIPX**VRVAL)
4.      DO 40 I=1,NV
5.      VISIG(I)=VIPY(I)/EXP(VTOP)
6. 40  CONTINUE
7.      RETURN
8.      END
C
C-----

```

```

1.      SUBROUTINE NWCONV(N,V,G,D,DT)
C
C      THIS SUBROUTINE IMPLICITLY CONVOLUTES V( ) AND D( ) TO
C      YIELD G( ) AT N POINTS
C-----
C      INPUT-      V--N VALUES OF INPUT
C                  D--N VALUES OF OUTPUT
C                  DT--TIME INCREMENT
C
C      OUTPUT-     G--N VALUES OF THE IMPLICIT CONVOLUTION RESULT
C
C
C
C

```

```

2.    DIMENSION V(200),G(200),Q(200)
3.    S=0.
4.    Q=0.0
5.    G(1)=Q(1)/(V(1)*DT)
6.    DO 984 I=2,N
7.    K=I-1
8.    DO 985 M=1,K
9.    Q=Q+V(K+2-M)*G(M)
10.   985 CONTINUE
11.   S=Q
12.   G(I)=(Q(I)/DT)-S/V(I)
    C
    C
13.   Q=0.0
14.   S=0.0
15.   984 CONTINUE
16.   RETURN
17.   END
    C
    C

```

```

1.    SUBROUTINE EXACT1(MM,DT,EQVK,EQMASS,T,GG,EQVC)
    C
    C      THIS SUBROUTINE CALCULATES THE REDUCED TRANSFER FUNCTION
    C      BY DIRECT SUBSTITUTION
    C-----
    C      INPUT-    EQVK--EQUIVALENT K PARAMETER
    C                EQMASS--EQUIVALENT MASS
    C                EQVC--EQUIVALENT C PARAMETER
    C                DT--TIME INCREMENT
    C                MM--NUMBER OF DATA POINTS
    C
    C      OUTPUT-   GG--MM VALUES OF THE TIME DEPENDENT TRANSFER FUN
    C
2.    DIMENSION T(200),GG(200)
    C$  TRACE ARITHMETIC
    C
3.    DO 630 I=1,MM
4.    T(I)=FLOAT(I)*DT
5.    TIME=T(I)
    C
    C
6.    BB=SQRT(EQVK/EQMASS)
7.    AA=EQVC/(2.*EQMASS)
    C
8.    TRI=BB*BB-AA*AA
9.    IF(TRI.LT.0.0)GO TO 3
    C
10.   GE1=1./SQRT(TRI)
11.   GE2=1./EXP(AA*T(I))
12.   G3=SIN(SQRT(TRI)*T(I))
13.   GG(I)=GE1*GE2*G3
    C
    C
14.   GO TO 630
    C
15.   3 CONTINUE
16.   PP=SQRT(ABS(TRI))
17.   P1=EXP(PP*T(I))
18.   P2=1./(EXP(PP*T(I)))
19.   P3=1./EXP(AA*T(I))
20.   P5=(P1-P2)/2.
21.   GG(I)=P3*P5/PP
    C
22.   630 CONTINUE
    C
23.   RETURN
24.   END

```

NEW RECORD

NUMBER OF DATA POINTS      RECORD NUMBER      MAX. WHEEL LOAD      TIME INCREMENT      NUMBER OF GAGES

46

1

25000.

.20

5

DEFLECTIONS IN FT

GAGE 1	GAGE 2	GAGE 3	GAGE 4	GAGE 5
.00001	0	.00001	.00001	-.00000
.00003	.00002	.00001	.00001	0
.00004	.00003	.00003	.00001	.00000
.00005	.00005	.00004	.00002	.00001
.00008	.00006	.00005	.00003	.00001
.00011	.00008	.00007	.00004	.00002
.00013	.00010	.00009	.00005	.00002
.00017	.00014	.00011	.00006	.00003
.00022	.00019	.00014	.00008	.00003
.00030	.00023	.00018	.00010	.00004
.00036	.00030	.00023	.00012	.00006
.00048	.00040	.00028	.00015	.00006
.00063	.00051	.00037	.00019	.00009
.00083	.00069	.00048	.00024	.00010
.00108	.00087	.00060	.00029	.00012
.00134	.00108	.00072	.00035	.00014
.00165	.00132	.00086	.00040	.00016
.00195	.00156	.00097	.00044	.00017
.00238	.00189	.00112	.00048	.00018
.00280	.00218	.00124	.00051	.00019
.00341	.00261	.00140	.00056	.00020
.00384	.00293	.00150	.00058	.00020
.00418	.00323	.00161	.00061	.00021
.00434	.00343	.00166	.00062	.00021
.00436	.00349	.00166	.00062	.00021
.00430	.00350	.00168	.00063	.00021
.00386	.00310	.00153	.00059	.00020
.00344	.00290	.00145	.00056	.00019
.00292	.00247	.00123	.00048	.00016
.00257	.00218	.00111	.00043	.00015
.00210	.00178	.00090	.00033	.00010
.00175	.00147	.00073	.00026	.00007
.00145	.00122	.00059	.00020	.00005
.00122	.00101	.00047	.00014	.00003
.00106	.00089	.00038	.00010	.00001
.00091	.00073	.00030	.00006	-.00001
.00082	.00065	.00026	.00004	-.00001
.00073	.00057	.00021	.00002	-.00002
.00067	.00051	.00018	.00001	-.00003

.00063	.00049	.00016	-.00000	-.00003
.00062	.00045	.00014	-.00001	-.00003
.00059	.00043	.00013	-.00001	-.00003
.00059	.00043	.00013	-.00002	-.00003
.00058	.00043	.00012	-.00002	-.00003
.00056	.00041	.00011	-.00002	-.00003
0	0	0	0	0

# PEAK DEFLECTIONS

.00436	.00350	.00168	.00063	.00021
--------	--------	--------	--------	--------

A PARAMETER	BETA	EXPONENT R
4.79864E-03	-6.02783E-01	1.31790E+00

# CALCULATED Y MEASURED Y LATERAL DIST.

4.35510E-03	4.35510E-03	2.50000E-01
3.56827E-03	3.49750E-03	5.83330E-01
1.71561E-03	1.68158E-03	1.50000E+00
6.38773E-04	6.30420E-04	2.50000E+00
2.07310E-04	2.12980E-04	3.50000E+00

FOR SIGNATURE

INCREMENT	SIGNATURE	VELOCITY	ACCELERATION
1	0	7.83911E-05	2.93966E-04
2	3.13564E-05	1.17587E-04	9.79888E-05
3	4.70346E-05	7.83911E-05	9.79888E-05
4	6.27128E-05	7.83911E-05	1.46983E-04
5	7.83911E-05	1.17587E-04	1.95978E-04
6	1.09747E-04	1.56782E-04	1.95978E-04
7	1.41104E-04	1.95978E-04	2.93966E-04
8	1.88139E-04	2.74369E-04	2.93966E-04
9	2.50851E-04	3.13564E-04	2.93966E-04
10	3.13564E-04	3.91955E-04	5.87933E-04
11	4.07633E-04	5.48737E-04	7.83911E-04
12	5.33059E-04	7.05520E-04	1.07788E-03
13	6.89841E-04	9.79888E-04	1.27385E-03
14	9.25014E-04	1.21506E-03	8.81899E-04
15	1.17587E-03	1.33265E-03	6.85922E-04
16	1.45807E-03	1.48943E-03	6.85922E-04
17	1.77164E-03	1.60702E-03	1.07788E-03
18	2.10088E-03	1.92058E-03	1.17587E-03
19	2.53987E-03	2.07736E-03	1.27385E-03
20	2.93183E-03	2.43012E-03	1.07788E-03
21	3.51192E-03	2.50851E-03	-8.81899E-04
22	3.93523E-03	2.07736E-03	-2.05777E-03
23	4.34286E-03	1.68541E-03	-3.03765E-03
24	4.60939E-03	8.62302E-04	-3.62559E-03
25	4.68779E-03	2.35173E-04	-3.38939E-03
26	4.70346E-03	-1.29345E-03	-5.58536E-03
27	4.17040E-03	-1.99897E-03	-2.05777E-03
28	3.90387E-03	-2.11656E-03	-1.07788E-03
29	3.32378E-03	-2.43012E-03	-4.89944E-04
30	2.93183E-03	-2.31254E-03	5.38939E-04
31	2.39877E-03	-2.39093E-03	6.85922E-04
32	1.97545E-03	-1.88139E-03	1.00439E-03

3000 RUN

INCREMENT	M-COMP.	C-COMP.	K-COMP.	EXACT	CONVOLUTION	TOT FUNC	SIGNATURE
1	72.36842	442.25146	0	514.61988	617.71209	.04052	0
2	24.12281	663.37719	95.83333	783.33333	675.91968	.03672	.00003
3	24.12281	442.25146	143.75000	610.12427	618.69802	.03287	.00005
4	36.18421	442.25146	191.66667	670.10234	788.48276	.02941	.00006
5	48.24561	663.37719	239.58333	951.20614	1087.28563	.02632	.00008
6	48.24561	884.50292	335.41667	1268.16520	1409.61497	.02355	.00011
7	72.36842	1105.62865	431.25000	1609.24708	1875.76839	.02108	.00014
8	72.36842	1547.88012	575.00000	2195.24854	2377.82005	.01886	.00019
9	72.36842	1769.00585	766.66667	2608.04094	2916.98704	.01688	.00025
10	144.73684	2211.25731	958.33333	3314.32749	3850.51099	.01511	.00031
11	192.98246	3095.76023	1245.83333	4534.57602	5092.77541	.01352	.00041
12	265.35088	3980.26316	1629.16667	5874.78070	6788.82147	.01210	.00053
13	313.59649	5528.14327	2108.33333	7950.07310	8855.46687	.01083	.00069
14	217.10526	6854.89766	2827.08333	9899.08626	10604.18900	.00969	.00093
15	168.85965	7518.27485	3593.75000	11280.88450	12230.96440	.00867	.00118
16	168.85965	8402.77778	4456.25000	13027.88743	13946.77641	.00776	.00146
17	265.35088	9066.15497	5414.58333	14746.08918	16235.51305	.00694	.00177
18	289.47368	10835.16082	6420.83333	17545.46784	18754.55138	.00621	.00210
19	313.59649	11719.66374	7762.50000	19795.76023	21549.91447	.00556	.00234
20	265.35088	13709.79532	8960.41667	22935.56287	24266.73247	.00498	.00293
21	-217.10526	14152.04678	10733.33333	24668.27485	24740.46330	.00445	.00351
22	-506.57895	11719.66374	12027.08333	23240.16813	23698.22351	.00399	.00394
23	-747.80702	9508.40643	13272.91667	22033.51608	21219.97611	.00357	.00434
24	-892.54386	4864.76608	14087.50000	18059.72222	17655.89134	.00319	.00461
25	-1326.75439	1326.75439	14327.08333	14327.08333	11497.90363	.00286	.00469
26	-1375.00000	-7297.14912	14375.00000	5702.85088	4443.21485	.00256	.00470
27	-506.57895	-11277.41228	12745.83333	961.84211	972.66864	.00229	.00417
28	-265.35088	-11940.78947	11931.25000	-274.89035	-1610.69484	.00205	.00390
29	-120.61404	-13709.79532	10158.33333	-3672.07602	-3627.83553	.00183	.00332



EQUIV. MASS SLUGS	EQUIV. STIFFNESS LBS/FT	EQUIV. DAMPING LBS-SEC/FT
246179.17	3056258.49	3641606.1

FORCE RATIOS<FORCE OVER 25000>  
SECTION<1> SECTION<2> SECTION<3>  
.981 .460 .417

TIME RATIOS<TIME OVER TIME TO MAX. DEF.>  
SECTION<1> SECTION<2> SECTION<3>  
.769 .962 1.000

C-PARAMETER DIFFERENCE RATIO  
.044

FORCE DIFFERENCE RATIO AT THE CROSSING POINT  
.197

MAXIMUM FORCE DIFFERENCE  
259.537

```

1.  PROGRAM PREDCT (INPUT,OUTPUT,TAPE3=INPUT,TAPE6=OUTPUT,PL01)
C
C-----
C      THIS PROGRAM PREDICTS THE SIGNATURE AT AN UNTESTED SITE
C      DUE TO VEHICLE A, IF THE SIGNATURE OF A STANDARD VEHICLE
C      IS KNOWN AT THE UNTESTED SITE, AND THE SIGNATURE OF BOTH
C      THE STANDARD VEHICLE AND VEHICLE A ARE KNOWN AT A
C      STANDARD SITE
C-----
C
C      STANDARD VEHICLE AND SITE
C      C 131      SITE 1      47      SIGNATURE
C-----
C
C      C 131      SITE 3      47      BOYER      SIGNATURE
C      C-135 SITE 1      47      BOYER      SIGNATURE
C-----
C      INCLUDED ONLY FOR PURPOSES OF THIS EXAMPLE-THIS SIGNATURE
C      IS THE PREDICTED SIGNATURE
C      C 135      SITE 3      BOYER      SIGNATURE      47
C-----
C
C      INPUT-      SCR( )      SIGNATURE DUE TO STANDARD VEHICLE
C                      X( )      AT STANDARD SITE
C                      DFCE( )      SIGNATURE DUE TO STANDARD VEHICLE
C                      COMPV( )      AT OTHER SITE
C                      ALL INPUT      SIGNATURE DUE TO OTHER VEHICLE
C                      DD( )      AT STANDARD SITE
C                      SIGNATURE DUE TO OTHER VEHICLE
C                      THIS EXAMPLE ONLY)
C      OUTPUT      SIGNATURES ARE IN INCHES
C                      PREDICTED SIGNATURE IN FT.
C-----
C      SUBROUTINES REQUIRED      (1) EXACT1( )
C                      (2) NWCONV( )
C                      (3) ERECT2( )
C                      (4) MODPRM( )
C-----
2.  DIMENSION SOUT1(200),SOUT2(200),VOUT1(200)
3.  DIMENSION ETINP(200),EQFNC(200)
4.  DIMENSION ET(200)
5.  DIMENSION VISIG(200)
6.  DIMENSION XT(6,200),XF(6,200),DTRK1(200),DF4(200),SFNC(200)
7.  DIMENSION PP(800),XG(800),DD(800)
8.  DIMENSION DRV0(100),DRV1(100),DRV2(100)
9.  DIMENSION DF(200),X(100),DFCE(100),DDEF(100)
10. DIMENSION SCR(100),T(200),V(200),D(200),G(200),GG(200)
11. DIMENSION COMPV(200),VOUT2(200)
C*  TRACE ARITHMETIC
C
C
12. 50 FORMAT(//60X,20H-----//)
13. 498 FORMAT(29X,54HEQUIV INPUT IN LBS      TDT FUNCTION      RESPONSE IN
14. 398 FORMAT(31X,E15.5,5X,E15.5,2X,E15.5)
C
15. READ(5,100)(SCR(I),I=1,47)
16. READ(5,100)(X(I),I=1,47)
17. READ(5,100)(DFCE(I),I=1,47)
18. READ(5,100)(COMPV(I),I=1,47)
19. 100 FORMAT(7F10.6)
C
C
20. DO 496 I=1,47
21. SOUT1(I)=SCR(I)/12.
22. VOUT1(I)=DFCE(I)/12.
23. SOUT2(I)=X(I)/12.
24. VOUT2(I)=COMPV(I)/12.
25. 496 CONTINUE
C
C

```

```

C
26. JP=47
27. PMAX =20000.
28. DT=0.04
29. MM=47
30. LL=47
31. NT=47
C
32. DO 74 I=1,NT
33. VISIG(I)=SQOUT1(I)
34. 74 CONTINUE
C
C
C
35. WRITE(6,497)
36. 497 FORMAT(//2X,23HSITE ONE STD VEHICLE//)
C
37. CALL MODPRM(PMAX,JP,DT,VISIG,EQMASS,DF,GG)
C
C
C
C COMPUTE EQUIV. INPUT FOR VEHICLE 2 SITE 1
38. DO 721 I=1,MM
39. T(I)=FLOAT(I)*DT
40. Q(I)=VOUT1(I)
41. V(I)=GG(I)
42. 721 CONTINUE
C
43. N=47
C
44. CALL NWCONV(N,V,G,Q,DT)
C
45. DO 722 I=1,MM
46. ETINP(I)=G(I)*EQMASS
47. 722 CONTINUE
C
48. WRITE(6,50)
49. WRITE(6,495)
50. 495 FORMAT(//2X,21HSITE ONE VEHICLE 2//)
51. WRITE(6,498)
52. WRITE(6,398)(ETINP(I),GG(I),Q(I),I=1,MM)
C
C
C
C COMPUTE EQUIVALENCY FUNCTION
53. DO 723 I=1,MM
54. EQFNC(I)=ETINP(I)/DF(I)
55. 723 CONTINUE
C
C COMPUTE TDT FUNCTION ,EQUIV. INPUT FOR NEXTSITE STD. VEHICLE
56. WRITE(6,397)
57. 397 FORMAT(//2X,23HNEXT SITE STD VEHICLE//)
C
C
58. DO 724 I=1,MM
59. VISIG(I)=SQOUT2(I)
60. 724 CONTINUE
C
61. CALL MODPRM(PMAX,JP,DT,VISIG,EQMASS,DF,GG)
C
C
C COMPUTE EQUIV. INPUT NEXT SITE VEHICLE 2
62. DO 725 I=1,MM
63. ET(I)=DF(I)*EQFNC(I)
64. 725 CONTINUE
C
C COMPUTE OUTPUT FOR NEXT SITE VEHICLE 2
65. DO 206 I=1,MM
66. PP(I)=ET(I)/EQMASS
67. XG(I)=GG(I)
68. 206 CONTINUE
C
C

```

```

69.      CALL ERECT2(MM,PP,XG,DT,DD)
      C
      C
70.      WRITE(6,50)
71.      WRITE(6,494)
72.      494 FORMAT(//2X,21HNEXT SITE   VEHICLE 2//)
73.      WRITE(6,498)
74.      WRITE(6,398)(ET(I),XG(I),DD(I),I=1,MM)
      C
75.      WRITE(6,50)
76.      WRITE(6,2000)
77.      2000 FORMAT(//60X,*PREDICTED*,10X,*MEASURED*//)
78.      WRITE(6,1000)(DD(I),VOUT2(I),I=1,47)
79.      1000 FORMAT(52X,2F15.5)
      C
80.      WRITE(6,50)
      C
      C
      C
      C
      C
      C
81.      STOP
82.      END
      C
      C
      C
1.      SUBROUTINE NWCONV(N,V,G,D,DT)
2.      DIMENSION V(200),G(200),D(200)
3.      S=0.
4.      Q=0.0
      C
      C
5.      G(1)=D(1)/(V(1)*DT)
6.      DO 984 I=2,N
7.      K=I-1
8.      DO 985 M=1,K
9.      Q=Q+V(K+2-M)*G(M)
10.     985 CONTINUE
      C
11.      S=Q
12.      G(I)=(D(I)/DT)-S/V(1)
      C
      C
13.      Q=0.0
14.      S=0.0
15.     984 CONTINUE
16.      RETURN
17.      END
      C
      C
      C
1.      SUBROUTINE ERECT2(MM,PP,XG,DT,DD)
2.      DIMENSION PP(800),XG(800),DD(800)
      C
      C
3.      PS2=0.0
4.      DO 331 I=2,MM
5.      K=I-1
6.      DO 332 M=1,K
7.      PS2=PP(K+1-M)*XG(M)+PS2
8.     332 CONTINUE
9.      DD(I-1)=PS2*DT
10.     PS2=0.0
11.     331 CONTINUE
12.      RETURN
13.      END
      C
      C
      C
1.      SUBROUTINE EXACT (MM,DT,EQVK,EQMASS,T,GG,EQVC)
2.      DIMENSION T(200),GG(200)

```

```

      C
      C      COMPUTING EXACT TRANSFER FUNCTION
3.      DO 630 I=1,MM
4.      T(I)=FLOAT(I)*DT
5.      TIME=T(I)
      C
      C
6.      BB=SQRT(EQVK/EQMASS)
7.      AA=EQVC/(2.*EQMASS)
      C
8.      TRI=BB*BB-AA*AA
9.      IF<TRI.LT.0.0>GO TO 3
      C
10.     GE1=1./SQRT<TRI>
11.     GE2=1./EXP<AA*T(I)>
12.     G3=SIN<SQRT<TRI>*T(I)>
13.     GG(I)=GE1*GE2*G3
      C
      C
14.     GO TO 630
      C
15.     3 CONTINUE
16.     PP=SQRT<ABS<TRI>>
17.     P1=EXP<PP*T(I)>
18.     P2=1./<EXP<PP*T(I)>>
19.     P3=1./EXP<AA*T(I)>
20.     P5=(P1-P2)/2.
21.     GG(I)=P3*P5/PP
      C
22.     630 CONTINUE
      C
      C
23.     RETURN
24.     END
      C

1.      SUBROUTINE MODPRM<PMAX,JP,DT,VISIG,EQMASS,DF,GG>
2.      DIMENSION QC<100>
3.      DIMENSION DF<200>
4.      DIMENSION T<200>
5.      DIMENSION Q<200>,GG<200>
6.      DIMENSION V<200>,G<200>
7.      DIMENSION IVEL<11,5>
8.      DIMENSION DRV1<200>,DRV2<200>,CPMXX<50>,VISIG<200>,DRV0<200>
      C
      C
9.      DO 74 I=1,JP
10.     DRV0(I)=VISIG(I)
11.     TRM1=(VISIG(I)+VISIG(I+1))/2.
12.     IF<I.GT.1>GO TO 744
13.     TRM2=VISIG(I)/2.
14.     GO TO 474
15.     744 CONTINUE
16.     TRM2=(VISIG(I)+VISIG(I-1))/2.
17.     474 CONTINUE
18.     DRV1(I)=(TRM1-TRM2)/DT
19.     74 CONTINUE
20.     DO 75 I=1,JP
21.     TRN1=(DRV1(I+1)+DRV1(I))/2.
22.     IF<I.GT.1>GO TO 755
23.     TRN2=DRV1(I)/2.
24.     GO TO 575
25.     755 CONTINUE
26.     TRN2=(DRV1(I)+DRV1(I-1))/2.
27.     575 CONTINUE
28.     DRV2(I)=(TRN1-TRN2)/DT
29.     75 CONTINUE
      C
      C
30.     BOTM=0.00000000001
      C*****
31.     DO 726 I=1,JP
32.     HUMP1=DRV0(I+1)-DRV0(I)
33.     IF<HUMP1.GE.0.0>GO TO 726
34.     JPP=I+6

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35.      GO TO 727
36.      726 CONTINUE
37.      727 CONTINUE
C*****
C
38.      IMAXV=0
39.      DV1MX=0.0
40.      DO 315 I=1,JPP
41.      IF(DRV1(I).EQ.0.0)DRV1(I)=(DRV1(I+1)+DRV1(I-1))/2.
CAUTION - IS FLOATING POINT EQUALITY TO BE EXPECTED *****
42.      IF(DRV1(I).EQ.0.0)DRV1(I)=(DRV1(I+2)+DRV1(I-2))/2.
CAUTION - IS FLOATING POINT EQUALITY TO BE EXPECTED *****
43.      IF(ABS(DRV1(I)).LT.BOTM)DRV1(I)=(DRV1(I+1)+DRV1(I-1))/2.
44.      IF(ABS(DRV2(I)).LT.BOTM)DRV2(I)=(DRV2(I+1)+DRV2(I-1))/2.
45.      IF(DRV1(I).LT.DV1MX)GO TO 315
46.      DV1MX=DRV1(I)
47.      IMAXV=I
48.      315 CONTINUE
C
C
49.      DMAX=DRV0(1)
50.      DO 53 I=2,JPP
51.      IF(DRV0(I).LT.DMAX)GO TO 53
52.      DMAX=DRV0(I)
53.      IMAXD=I
54.      53 CONTINUE
C
C
55.      IMAXV1=IMAXV-1
56.      DO 57 I=2,IMAXV1
57.      IF(DRV2(I).LE.0.0)DRV2(I)=(DRV2(I-1)+DRV2(I+1))/2.
58.      IF(DRV2(I).LE.0.0)DRV2(I)=(DRV2(I-2)+DRV2(I+2))/2.
59.      57 CONTINUE
60.      IMAXVA=IMAXV+1
61.      DO 109 I=IMAXVA,JPP
62.      IF(DRV2(I).GE.0.0)DRV2(I)=(DRV2(I-1)+DRV2(I+1))/2.
63.      IF(DRV2(I).GE.0.0)DRV2(I)=(DRV2(I-2)+DRV2(I+2))/2.
64.      109 CONTINUE
65.      DO 107 I=1,JPP
66.      IF(DRV1(I+1).EQ.DRV1(I))DRV1(I+1)=(DRV1(I+2)+DRV1(I))/2.
CAUTION - IS FLOATING POINT EQUALITY TO BE EXPECTED *****
67.      IF(DRV2(I+1).EQ.DRV2(I))DRV2(I+1)=(DRV2(I+2)+DRV2(I))/2.
CAUTION - IS FLOATING POINT EQUALITY TO BE EXPECTED *****
68.      107 CONTINUE
C*****
69.      DO 789 IA=1,JPP
70.      DEROTS=DRV1(IA+1)/DRV1(IA)
71.      IF(DEROTS.GT.0.0)GO TO 789
72.      DZERO=DRV1(IA)-DRV1(IA+1)
73.      DDTZ=DRV1(IA)/DZERO
74.      NAFNL=IA
75.      GO TO 788
76.      789 CONTINUE
77.      788 CONTINUE
C*****
78.      DO 889 IA=1,JPP
79.      ZEROTS=DRV2(IA+1)/DRV2(IA)
80.      IF(ZEROTS.GT.0.0)GO TO 889
81.      TZERO=DRV2(IA)-DRV2(IA+1)
82.      FDTZ=DRV2(IA)/TZERO
83.      IAFNL=IA
84.      DRORNG=DRV0(IA+1)-DRV0(IA)
85.      ZVALU0=DRV0(IA)+FDTZ*DRORNG
86.      DR1RNG=DRV1(IA+1)-DRV1(IA)
87.      ZVALU1=DRV1(IA)+FDTZ*DR1RNG
88.      GO TO 888
89.      889 CONTINUE
90.      888 CONTINUE
C
C
C
C
91.      WRITE(6,99)
92.      99 FORMAT(/30X,'FOR SIGNATURE'/)
93.      WRITE(6,76)

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94.      76 FORMAT(/1X,*      INCREMENT      DEFLECTION      VELOCITY      ACCEL
          1ERATION*/)
95.      WRITE(6,77)<I,DRV0(I),DRV1(I),DRV2(I),I=1,JPP>
96.      77 FORMAT(1X,I4,3E15.5)
97.      78 FORMAT(/15X,2I15/)
C=====
C=====
98.      IDIFF=IMAXD-IMAXV
99.      IMAXF=0
100.     AA1=0.05
101.     ICC=0
C=====
102.     DO 104 ILP=1,40
C=====
103.     EQKA=AA1*PMAK/DMAK
104.     AA3=-0.91
C=====
105.     DO 103 JJ=1,20
106.     IT=IMAXV
107.     EQMA=AA3*PMAK/DRV2(IMAXD)
108.     CPMAX=0.0
109.     AA2=AA1+AA3
110.     IF(AA2.LT.0.0)GO TO 1021
C=====
111.     IMAXC=IMAXD
112.     IT=IT+1
113.     DO 102 II=IT,IMAXC
114.     EQCA=EQMA*DRV2(II)/DRV1(II)
115.     EQCA=-EQCA
C
C
116.     EQVK=EQKA
117.     EQMASS=EQMA
118.     EQVC=EQCA
119.     MM=JPP
120.     CALL EXACT1(MM,DT,EQVK,EQMASS,T,GG,EQVC)
C
C
C
121.     DO 73 I=1,JPP
122.     D(I)=DRV0(I)
123.     V(I)=GG(I)
124.     73 CONTINUE
C
125.     N=JPP
126.     CALL NUCONV(N,V,G,D,DT)
C
127.     DO 508 MP=1,JPP
128.     DF(MP)=G(MP)*EQMASS
129.     508 CONTINUE
130.     DO 509 MA=1,JPP
131.     DF(MA)=(DF(MA)+DF(MA+1))/2.
132.     509 CONTINUE
C
C
133.     CPMAX=0.
134.     DO 501 M=1,JPP
135.     DF(M)=(DF(M)+DF(M+1))/2.
136.     IF(DF(M).GT.CPMAX)GO TO 20
137.     GO TO 502
138.     20 CPMAX=DF(M)
139.     ICF=M
140.     502 CONTINUE
141.     501 CONTINUE
C
142.     ERFCE=CPMAX-PMAK
143.     ABERFG=ABS(ERFCE)
144.     IF(ABERFG.GT.500.0)GO TO 102
C
145.     ICC=ICC+1
C
146.     DFRNG=DF(IAFNL+1)-DF(IAFNL)
147.     ZVALUF=DF(IAFNL)+FDTZ*DFRNG
148.     CMAXV=(ZVALUF-EQKA*ZVALU0)/ZVALU1
149.     CDIFFR=(CMAXV-EQCA)/CMAXV

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150.      ABCD=CDIFFR
151.      QC(ICC)=CDIFFR
152.      IF(ICC.EQ.1)GO TO 102
153.      CRATIO=QC(ICC)/QC(ICC-1)
154.      IF(CRATIO.GT.0.0)GO TO 102
      C
      C
      C
155.      FCHK=EQKA*DRV0(II)
156.      DIFCHK=FCHK-DF(II)
157.      DFCHKR=DIFCHK/FCHK
158.      FPFAC=DF(II)/PMA
159.      ICDPT=II
160.      IBBB=JMAXD-ICDPT
161.      BB1=FLOAT(1BBB/IDIFF)
162.      TRMM=EQMA*DRV2(II)
163.      TRMC=EQCA*DRV1(II)
164.      TRMK=EQKA*DRV0(II)
165.      CPMXX(II)=TRMM+TRMC+TRMK
166.      WRITE(6,847)
167.      847 FORMAT(/10X,*GOOD RUN*/)
168.      GO TO 846
169.      102 CONTINUE
170.      1021 CONTINUE
171.      AA3=AA3+0.045
      C*****
172.      103 CONTINUE
173.      AA1=AA1+0.025
174.      104 CONTINUE
175.      1000 FORMAT(/1X,*000*)
176.      844 FORMAT(1X,7F10.2,3E15.5)
177.      845 FORMAT(6F15.4,10X,2I5,F10.3)
      C*****
      C
178.      WRITE(6,1002)
179.      1002 FORMAT(/10X,*OUTER LOOP COMPLETED*/)
180.      GO TO 94
      C
      C
181.      846 CONTINUE
      C
182.      WRITE(6,1000)
      C*****
183.      AFRNG=DF(NAFNL+1)-DF(NAFNL)
184.      DVALUF=DF(NAFNL)+.DTZ*AFRNG
      C*****
185.      ZVALUR=ZVALUF/PMA
      C*****
186.      DVALZD=DVALUF/PMA
      C*****
187.      FORTIO=ABERFG/PMA
      C*****
188.      DENOM=FLOAT(IMAXD)
189.      DENOM1=1.
190.      TCRSPT=FLOAT(II)/DENOM
191.      TZROA=FLOAT(IAFNL)/DENOM
      C*****
192.      1199 FORMAT(/10X,11F11.3/)
193.      1001 FORMAT(10X,I5,7F15.5)
194.      CALL EXACT1(JP,DT,EQKA,EQMA,T,GG,EQCA)
195.      DO 733 I=1,JP
196.      O(I)=DRV0(I)
197.      V(I)=GG(I)
198.      733 CONTINUE
199.      N=JP
200.      CALL NWCONV(N,V,G,O,DT)
201.      DO 518 MP=1,JP
202.      DF(MP)=G(MP)*EQMA
203.      518 CONTINUE
204.
      C
205.      94 CONTINUE
206.      RETURN
207.      END

```



SITE ONE STD VEHICLE

FOR SIGNATURE

INCREMENT	DEFLECTION	VELOCITY	ACCELERATION
1	1.27667E-04	1.92708E-03	9.93490E-03
2	1.54167E-04	7.94792E-04	8.31380E-03
3	1.91250E-04	1.03125E-03	6.69271E-03
4	2.36667E-04	1.33021E-03	1.03906E-02
5	2.97667E-04	1.86250E-03	1.57552E-02
6	3.85667E-04	2.59063E-03	2.10677E-02
7	5.04917E-04	3.54792E-03	2.91276E-02
8	6.69500E-04	4.92083E-03	3.62500E-02
9	8.98583E-04	6.44792E-03	4.09245E-02
10	1.18533E-03	8.19479E-03	4.38151E-02
11	1.55417E-03	9.95312E-03	3.51432E-02
12	1.98158E-03	1.10062E-02	9.81771E-03
13	2.43467E-03	1.07385E-02	-3.29948E-02
14	2.84067E-03	8.36667E-03	-8.32943E-02
15	3.10400E-03	4.07500E-03	-1.15703E-01
16	3.16667E-03	-8.89583E-04	-1.14401E-01
17	3.03283E-03	-5.07708E-03	-8.50130E-02
18	2.76050E-03	-7.69062E-03	-4.40234E-02
19	2.41758E-03	-8.59896E-03	-4.75260E-03
20	2.07258E-03	-8.07083E-03	-9.53125E-03
21	1.77192E-03	-6.89896E-03	7.39583E-03
22	1.52067E-03	-5.80104E-03	2.50000E-03

GOOD RUN

00

SITE ONE VEHICLE 2

EQUIV INPUT IN LBS	TDT FUNCTION	RESPONSE IN FT
7.26622E+03	2.30853E-02	2.02000E-04
9.67190E+02	2.76124E-02	2.68500E-04
3.38946E+03	2.56125E-02	3.50500E-04
6.28019E+03	2.17664E-02	5.07583E-04
1.20998E+04	1.78084E-02	8.30917E-04
2.26201E+04	1.43096E-02	1.45967E-03
3.73522E+04	1.13959E-02	2.51742E-03
5.36091E+04	9.03463E-03	4.03258E-03
6.66077E+04	7.14611E-03	5.86650E-03
5.49146E+04	5.64567E-03	7.24833E-03
-4.40640E+03	4.45756E-03	6.66300E-03
-1.88870E+04	3.51838E-03	5.11650E-03
1.76576E+04	2.77663E-03	4.47067E-03
4.69750E+04	2.19108E-03	5.00992E-03
8.37103E+04	1.72893E-03	6.88358E-03
6.44724E+04	1.36424E-03	8.41667E-03
-1.57651E+04	1.07645E-03	7.41800E-03
-2.57654E+04	8.49373E-04	5.45308E-03
-5.79904E+03	6.70194E-04	3.97867E-03
-1.63126E+03	5.28813E-04	2.96208E-03
1.61962E+03	4.17257E-04	2.31008E-03
4.38986E+03	3.29234E-04	1.93375E-03
4.45170E+03	2.59780E-04	1.69475E-03

5.24889E+03	2.04977E-04	1.55192E-03
5.77634E+03	1.61736E-04	1.47250E-03
4.82121E+03	1.27617E-04	1.39683E-03
5.39067E+03	1.00695E-04	1.34767E-03
6.05333E+03	7.94527E-05	1.33158E-03
4.47763E+03	6.26916E-05	1.28433E-03
4.63410E+03	4.94664E-05	1.23733E-03
5.15415E+03	3.90311E-05	1.21075E-03
5.09242E+03	3.07972E-05	1.19233E-03
3.93199E+03	2.43003E-05	1.14658E-03
5.04313E+03	1.91740E-05	1.12867E-03
5.26145E+03	1.51291E-05	1.12800E-03
4.01299E+03	1.19375E-05	1.09825E-03
4.74872E+03	9.41922E-06	1.08333E-03
6.32678E+03	7.43217E-06	1.11892E-03
2.59107E+03	5.86430E-06	1.06242E-03
5.12136E+03	4.62719E-06	1.05375E-03
5.51294E+03	3.65105E-06	1.07242E-03
4.25295E+03	2.88083E-06	1.06250E-03
4.31075E+03	2.27310E-06	1.04625E-03
5.95350E+03	1.79358E-06	1.07567E-03
4.67396E+03	1.41521E-06	1.08050E-03
3.94255E+03	1.11666E-06	1.05650E-03
4.68328E+03	8.81093E-07	1.04683E-03

NEXT SITE STD VEHICLE

FOR SIGNATURE

INCREMENT	DEFLECTION	VELOCITY	ACCELERATION
1	9.95833E-05	1.52187E-03	7.77344E-03
2	1.21750E-04	6.21875E-04	6.71224E-03
3	1.49333E-04	8.09375E-04	5.65104E-03
4	1.86500E-04	1.07396E-03	6.19792E-03
5	2.35250E-04	1.30521E-03	5.92448E-03
6	2.90917E-04	1.54792E-03	7.12240E-03
7	3.59083E-04	1.87500E-03	8.54167E-03
8	4.40917E-04	2.23125E-03	9.60937E-03
9	5.37583E-04	2.64375E-03	1.25000E-02
10	6.52417E-04	3.23125E-03	1.47917E-02
11	7.96083E-04	3.82708E-03	1.32161E-02
12	9.58583E-04	4.28854E-03	7.79948E-03
13	1.13917E-03	4.45104E-03	-6.17187E-03
14	1.31467E-03	3.79479E-03	-2.66797E-02
15	1.44275E-03	2.31667E-03	-4.29948E-02
16	1.50000E-03	3.55208E-04	-4.88021E-02
17	1.47117E-03	-1.58750E-03	-3.80990E-02
18	1.37300E-03	-2.69271E-03	-1.61849E-02
19	1.25575E-03	-2.88229E-03	-1.82292E-03
20	1.14242E-03	-2.83854E-03	-5.88542E-03
21	1.02867E-03	-2.75000E-03	-7.35677E-04
22	9.22417E-04	-2.56146E-03	-7.16146E-04

GOOD RUN

00

EQUIV INPUT IN LBS	TDT FUNCTION	RESPONSE IN FT
2.39378E+04	2.79870E-02	1.57565E-04
-5.99763E+04	4.02600E-02	-1.68119E-04
6.45929E+03	4.45935E-02	-2.74326E-04
1.36858E+04	4.49856E-02	-2.24518E-04
2.55768E+04	4.34868E-02	-2.40447E-05
3.73268E+04	4.11442E-02	3.17975E-04
5.95647E+04	3.84877E-02	8.60932E-04
7.51046E+04	3.57813E-02	1.58148E-03
8.03293E+04	3.31525E-02	2.39395E-03
6.33737E+04	3.06592E-02	3.10814E-03
-4.96779E+03	2.83238E-02	3.29894E-03
-1.96412E+04	2.61510E-02	3.13688E-03
1.84098E+04	2.41370E-02	3.06340E-03
4.64276E+04	2.22741E-02	3.21925E-03
6.79205E+04	2.05529E-02	3.61990E-03
3.74124E+04	1.89636E-02	3.92125E-03
-3.11110E+01	1.74966E-02	3.91757E-03
2.12723E+04	1.61429E-02	3.90907E-03
5.20213E+03	1.48937E-02	3.79282E-03
1.06867E+03	1.37411E-02	3.60242E-03
-1.67619E+03	1.26777E-02	3.36579E-03
-3.75658E+03	1.16966E-02	3.10234E-03
-4.38155E+03	1.07913E-02	2.83187E-03
-6.42824E+03	9.95617E-03	2.55472E-03
-9.40418E+03	9.18563E-03	2.26518E-03
-6.84531E+03	8.47472E-03	1.99745E-03
-6.04811E+03	7.81883E-03	1.75536E-03
-7.78484E+03	7.21371E-03	1.52313E-03
-4.78390E+03	6.65541E-03	1.32403E-03
-2.34767E+03	6.14033E-03	1.16421E-03
-3.53550E+03	5.66511E-03	1.02124E-03
-8.24185E+02	5.22666E-03	9.09508E-04
3.66539E+03	4.82215E-03	8.46376E-04
5.42162E+03	4.44895E-03	8.20303E-04
-7.56887E+03	4.10463E-03	7.27339E-04
7.55546E+03	3.78696E-03	7.05572E-04
1.67329E+03	3.49387E-03	6.79791E-04
4.12036E+03	3.22347E-03	6.69173E-04
2.13777E+03	2.97399E-03	6.53120E-04
1.94469E+03	2.74383E-03	6.33810E-04
3.01993E+03	2.53147E-03	6.20752E-04
6.73974E+03	2.33555E-03	6.35642E-04
2.83888E+03	2.15480E-03	6.37603E-04
4.24396E+03	1.98303E-03	6.42583E-04
3.23174E+03	1.83417E-03	6.42152E-04
6.86666E+03	1.69222E-03	6.63086E-04
2.46450E+03	1.56125E-03	0

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PREDICTED	MEASURED
.00016	.00018
-.00017	.00028
-.00027	.00044
-.00022	.00068
-.00002	.00107
.00032	.00165
.00086	.00252
.00158	.00357
.00239	.00404
.00311	.00367
.00330	.00318

.00314	.00289
.00306	.00284
.00322	.00314
.00362	.00382
.00392	.00433
.00392	.00399
.00391	.00320
.00379	.00244
.00360	.00178
.00337	.00128
.00310	.00091
.00283	.00067
.00255	.00051
.00227	.00041
.00200	.00035
.00176	.00032
.00152	.00029
.00132	.00027
.00116	.00025
.00102	.00014
.00091	.00012
.00085	.00012
.00082	.00012
.00073	.00012
.00071	.00012
.00068	.00011
.00067	.00012
.00065	.00011
.00063	.00011
.00062	.00011
.00064	.00011
.00064	.00011
.00064	.00011
.00064	.00011
.00066	.00011
0	.00011

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APPENDIX D  
DATA DIGITIZED  
FROM LIGHT  
SENSITIVE PAPER

The data listing has the following format

- Card 1 - A comment card giving the base name, site number, grid location of measurement point, Load Cart data of test, distance from closest measurement gage to edge of tire track in inches, time increment at which data was digitized and estimated number of cards.
- Card 2 - Distance (ft) of measurement point from edge of tire print where Gage 1 is the closest.
- Card 3 - Number of cards actually read, time increment used, and weight of load cart (25 kips).
- Card 4 to (n-1) - Data digitized and listed (from left to right) as, Gage 1, Gage 2, Gage 3, Gage 4, and Gage 5.
- Card n (last card) - Calibration data for Gages 1 to 5 also listed from from left (Gage 1) to right (Gage 5).

LOC IN	SITE 1	LOC A-1	LD. CT.	3.11.76	7.25 .2	48
48	.200 25000.0	1.6875	2.6875	3.6875		
0027	0045	0071	0102	0134		
0030	0048	0074	0106	0134		
0034	0051	0078	0110	0136		
0040	0058	0085	0117	0137		
0049	0065	0094	0126	0141		
0061	0078	0107	0138	0145		
0077	0092	0122	0154	0151		
0103	0115	0146	0175	0158		
0130	0141	0172	0198	0165		
0167	0174	0203	0223	0173		
0210	0211	0234	0247	0181		
0259	0254	0272	0277	0190		
0307	0297	0306	0301	0195		
0360	0340	0340	0324	0200		
0414	0382	0371	0344	0206		
0456	0420	0394	0358	0208		
0487	0447	0411	0366	0209		
0490	0456	0415	0367	0209		
0483	0459	0419	0371	0209		
0461	0451	0418	0375	0213		
0427	0429	0403	0367	0212		
0393	0402	0385	0354	0209		
0359	0374	0363	0338	0204		
0331	0349	0344	0324	0202		
0302	0324	0320	0305	0194		
0277	0301	0299	0288	0189		
0248	0273	0273	0267	0182		
0225	0250	0249	0247	0175		
0198	0223	0223	0222	0167		
0171	0196	0196	0196	0156		
0141	0163	0163	0167	0147		
0115	0137	0137	0143	0140		
0096	0117	0117	0126	0136		
0085	0105	0104	0117	0134		
0076	0095	0095	0109	0133		
0071	0089	0089	0103	0131		
0067	0084	0084	0099	0131		
0064	0080	0080	0096	0130		
0060	0078	0078	0094	0129		
0058	0074	0074	0092	0128		
0057	0073	0073	0091	0128		
0055	0072	0072	0090	0128		
0055	0071	0072	0090	0128		
0053	0070	0070	0089	0127		
0053	0069	0069	0088	0128		
0053	0069	0069	0087	0127		
0051	0069	0069	0087	0128		
0051	0069	0069	0087	0127		
.00008065	.00006995	.00004052	.00002212	.00002778		

C	EGLIN	SITE 1	LOC A-1	LD. CT.	3.11.76	7.00	53
	.58333	.91666	1.83333	2.83333	3.83333		
53	.200	25000.0					
0023	0052	0075	0107	0137			
0028	0057	0079	0108	0135			
0034	0067	0090	0117	0136			
0042	0077	0102	0127	0139			
0052	0088	0115	0140	0143			
0065	0104	0130	0156	0149			
0080	0121	0150	0173	0153			
0096	0138	0167	0189	0158			
0113	0158	0185	0203	0164			
0135	0180	0208	0222	0169			
0160	0206	0229	0241	0174			
0184	0231	0251	0259	0179			
0211	0256	0271	0272	0183			
0249	0292	0299	0291	0188			
0288	0325	0321	0305	0191			
0325	0357	0342	0316	0193			
0364	0388	0359	0326	0195			
0401	0414	0375	0333	0196			
0433	0436	0388	0339	0198			
0453	0447	0393	0340	0197			
0473	0456	0400	0343	0197			
0484	0460	0402	0342	0197			
0488	0461	0402	0343	0198			
0489	0461	0402	0344	0199			
0487	0458	0403	0346	0201			
0484	0453	0402	0346	0202			
0475	0446	0397	0344	0202			
0458	0430	0384	0334	0201			
0437	0411	0370	0323	0198			
0412	0389	0351	0308	0192			
0386	0367	0331	0292	0187			
0360	0344	0309	0273	0182			
0330	0316	0284	0254	0176			
0296	0288	0257	0232	0170			
0267	0260	0232	0212	0164			
0237	0233	0207	0192	0159			
0213	0211	0187	0175	0154			
0191	0191	0167	0159	0149			
0168	0173	0149	0143	0144			
0148	0154	0131	0127	0141			
0129	0138	0115	0114	0136			
0113	0123	0100	0101	0134			
0100	0112	0089	0094	0131			
0089	0102	0080	0086	0131			
0081	0093	0073	0079	0127			
0070	0085	0064	0072	0126			
0062	0078	0059	0067	0125			
0056	0073	0054	0064	0125			
0051	0069	0051	0063	0124			
0049	0066	0048	0059	0124			
0048	0064	0047	0058	0123			
0044	0063	0044	0057	0122			
0042	0061	0043	0056	0121			
	.00008065	.00006995	.00004052	.00002212	.00002778		

C	EGLIN	SITE 1	LOC A-2	LD. CT.	3.11.76	5.50 .2	38
	.45833	.79167	1.70833	2.70833	3.70833		
38	.200	25000.0					
0042	0070	0100	0131	0148			
0043	0070	0100	0132	0148			
0044	0071	0101	0135	0149			
0045	0072	0103	0138	0151			
0046	0074	0106	0144	0153			
0050	0077	0111	0155	0156			
0054	0082	0116	0168	0162			
0065	0092	0129	0193	0171			
0083	0110	0149	0230	0183			
0107	0131	0172	0273	0198			
0138	0158	0199	0318	0211			
0182	0197	0231	0366	0226			
0245	0249	0269	0418	0238			
0301	0293	0298	0451	0245			
0318	0316	0311	0476	0255			
0286	0301	0307	0480	0262			
0238	0263	0281	0446	0254			
0195	0225	0250	0395	0239			
0160	0190	0218	0342	0222			
0132	0161	0189	0290	0205			
0111	0140	0167	0249	0192			
0095	0124	0149	0216	0180			
0086	0113	0137	0193	0173			
0079	0105	0129	0178	0167			
0074	0100	0123	0166	0163			
0071	0097	0119	0158	0161			
0069	0094	0116	0155	0159			
0067	0092	0116	0151	0158			
0066	0091	0114	0150	0157			
0065	0090	0113	0148	0157			
0065	0090	0113	0149	0158			
0064	0089	0112	0148	0157			
0063	0089	0113	0148	0158			
0063	0088	0112	0148	0158			
0061	0088	0112	0148	0158			
0061	0088	0112	0148	0158			
0061	0087	0111	0148	0158			
0061	0087	0112	0149				
	.0001613	.0001399		.00002212	.00002778		



C	EGLIN	SITE 1	LOC A-2	LD. CT.	3.11.76	7.00 .2	45
	.58333	.91666	1.83333	2.83333	3.83333		
45	.200	25000.0					
0026	0054	0083	0120	0145			
0026	0055	0085	0124	0147			
0027	0057	0088	0131	0150			
0030	0059	0091	0139	0153			
0032	0062	0096	0148	0156			
0035	0067	0101	0159	0160			
0041	0074	0109	0175	0166			
0050	0084	0121	0198	0175			
0062	0099	0137	0227	0185			
0079	0116	0155	0261	0197			
0099	0138	0175	0294	0207			
0123	0160	0194	0323	0216			
0153	0187	0214	0349	0222			
0187	0217	0233	0374	0226			
0223	0244	0249	0390	0228			
0255	0266	0261	0403	0230			
0277	0279	0270	0412	0230			
0286	0280	0273	0415	0231			
0281	0275	0273	0418	0232			
0265	0261	0262	0403	0227			
0237	0237	0245	0377	0218			
0211	0215	0228	0351	0211			
0181	0189	0205	0317	0200			
0156	0167	0187	0287	0190			
0134	0147	0169	0256	0180			
0114	0129	0151	0225	0171			
0097	0114	0137	0199	0163			
0082	0101	0123	0176	0157			
0073	0093	0114	0163	0153			
0067	0086	0108	0152	0150			
0060	0081	0102	0140	0146			
0056	0076	0098	0133	0143			
0050	0072	0094	0127	0142			
0048	0070	0091	0122	0141			
0045	0068	0089	0120	0141			
0045	0067	0088	0118	0140			
0043	0066	0087	0117	0139			
0042	0064	0087	0116	0139			
0041	0064	0086	0115	0139			
0040	0062	0085	0115	0139			
0038	0062	0084	0112	0138			
0037	0060	0083	0110	0138			
0036	0059	0082	0108	0138			
0034	0058	0081	0107	0138			
0034	0058	0081	0107	0138			
	.0001613	.0001399	.00008104	.00002212	.00002778		

C	EGLIN	SITE 1	LDC A-3	LD. CT.	3.11.76	4.00 .2	37
	.33333	.66666	1.58333	2.583333	3.583333		
37	.200	25000.0					
0048	0071	0094	0131	0148			
0049	0071	0094	0131	0148			
0050	0071	0095	0135	0149			
0050	0073	0097	0137	0151			
0052	0074	0099	0141	0152			
0054	0075	0101	0149	0155			
0058	0079	0105	0158	0161			
0064	0082	0110	0172	0167			
0072	0088	0118	0188	0173			
0080	0098	0127	0202	0178			
0092	0111	0139	0220	0182			
0109	0125	0152	0242	0188			
0146	0159	0182	0287	0202			
0193	0197	0214	0330	0212			
0261	0250	0252	0382	0223			
0326	0298	0281	0414	0230			
0366	0329	0297	0435	0235			
0357	0333	0300	0446	0240			
0312	0305	0282	0424	0234			
0263	0268	0256	0386	0225			
0220	0230	0226	0340	0211			
0187	0198	0198	0298	0198			
0157	0170	0170	0250	0183			
0131	0143	0143	0204	0168			
0116	0127	0126	0174	0158			
0105	0116	0115	0152	0150			
0098	0108	0108	0137	0145			
0093	0102	0102	0128	0142			
0091	0099	0099	0120	0139			
0087	0096	0096	0116	0137			
0085	0094	0094	0114	0136			
0084	0093	0093	0110	0135			
0083	0093	0093	0109	0135			
0083	0092	0092	0109	0135			
0082	0091	0091	0107	0134			
0081	0091	0091	0107	0133			
0081	0089	0089	0105	0133			
	.0001613	.0001399	.00008104	.00002212	.00002778		

C	EGLIN	SITE 1	LDC A-3	LD. CT.	3.11.76	4.50 .2	45
	.375	.708	1.625	2.625	3.625		
45	.200	25000.0					
0030	0049	0081	0100	0140			
0029	0049	0081	0102	0140			
0030	0049	0081	0103	0140			
0030	0051	0083	0106	0142			
0031	0052	0085	0111	0143			
0034	0055	0088	0117	0145			
0037	0058	0092	0126	0149			
0040	0064	0098	0137	0152			
0047	0070	0105	0151	0157			
0054	0078	0114	0168	0163			
0064	0089	0125	0188	0169			
0079	0105	0140	0212	0176			
0097	0123	0157	0242	0186			
0120	0144	0176	0270	0193			
0149	0170	0194	0293	0198			
0186	0203	0215	0320	0204			
0232	0239	0238	0349	0211			
0278	0271	0255	0367	0214			
0322	0298	0268	0378	0215			
0345	0308	0272	0378	0214			
0349	0308	0272	0378	0215			
0334	0295	0265	0368	0211			
0303	0269	0248	0339	0203			
0270	0242	0227	0312	0196			
0234	0211	0200	0271	0185			
0203	0184	0176	0234	0174			
0173	0159	0154	0199	0165			
0153	0141	0138	0175	0159			
0136	0126	0126	0153	0150			
0124	0116	0115	0138	0147			
0113	0108	0108	0126	0143			
0105	0099	0101	0113	0139			
0098	0094	0093	0102	0134			
0092	0089	0088	0093	0131			
0088	0086	0085	0086	0129			
0083	0083	0082	0079	0126			
0080	0080	0080	0074	0124			
0079	0079	0079	0073	0124			
0077	0077	0077	0070	0124			
0075	0075	0075	0066	0121			
0073	0073	0073	0063	0121			
0072	0072	0072	0060	0119			
0072	0072	0072	0060	0119			
0070	0070	0070	0058	0118			
0068	0069	0069	0056	0117			
.0001613	.0001399	.00008104	.00002212	.00002778			

C	EGLIN	SITE 1	LOC A-4	LD. CT.	3.11.76	5.00 .2	53
	.41667	.75	1.66667	2.66667	3.66667		
53		.200 25000.0					
0042	0069	0099	0134	0155			
0045	0071	0101	0139	0157			
0046	0074	0104	0147	0160			
0048	0075	0107	0153	0163			
0050	0078	0110	0160	0166			
0053	0082	0114	0168	0169			
0056	0086	0119	0178	0174			
0061	0091	0125	0190	0178			
0068	0098	0133	0205	0183			
0076	0106	0143	0224	0190			
0083	0116	0153	0240	0197			
0093	0125	0164	0258	0203			
0102	0135	0174	0275	0209			
0115	0149	0188	0298	0215			
0128	0163	0201	0315	0221			
0148	0182	0217	0338	0227			
0169	0203	0234	0361	0232			
0195	0226	0252	0385	0238			
0224	0252	0271	0409	0243			
0255	0275	0287	0427	0247			
0287	0299	0304	0444	0250			
0317	0318	0316	0457	0252			
0335	0329	0322	0463	0252			
0341	0330	0322	0462	0251			
0338	0326	0321	0462	0252			
0323	0313	0310	0445	0249			
0304	0295	0295	0426	0244			
0281	0274	0277	0400	0236			
0251	0248	0255	0368	0228			
0225	0227	0238	0341	0221			
0207	0212	0222	0317	0212			
0189	0196	0207	0293	0205			
0173	0181	0192	0269	0198			
0158	0169	0180	0247	0191			
0146	0157	0168	0227	0184			
0137	0148	0158	0211	0178			
0128	0141	0150	0196	0172			
0121	0135	0144	0184	0169			
0116	0130	0138	0174	0165			
0111	0126	0134	0167	0164			
0108	0124	0131	0162	0161			
0107	0120	0128	0157	0158			
0104	0119	0126	0152	0158			
0102	0117	0124	0149	0156			
0100	0116	0122	0146	0155			
0099	0115	0121	0144	0155			
0098	0114	0120	0142	0153			
0097	0113	0119	0140	0153			
0096	0112	0119	0139	0152			
0095	0111	0119	0138	0151			
0095	0111	0118	0137	0151			
0095	0111	0118	0137	0151			
0094	0110	0117	0136	0152			
.0001613	.0001399	.00008104	.00002212	.00002778			

C	EGLIN	SITE 1	LDC A-5	LD. CT.	3:11.76	5.00 .2	43
	.41667	.75	1.66667	2.66667	3.66667		
43	.200	25000.0					
0036	0059	0083	0123	0141			
0037	0061	0086	0128	0143			
0040	0065	0090	0138	0147			
0042	0068	0094	0148	0150			
0045	0072	0100	0159	0157			
0052	0079	0107	0174	0162			
0057	0085	0114	0185	0166			
0065	0093	0124	0202	0173			
0074	0105	0136	0221	0180			
0087	0118	0150	0244	0187			
0104	0139	0168	0269	0196			
0129	0161	0188	0294	0202			
0161	0190	0210	0321	0209			
0196	0220	0233	0344	0215			
0233	0247	0251	0363	0219			
0262	0266	0261	0370	0221			
0279	0275	0264	0372	0219			
0290	0279	0269	0376	0220			
0286	0275	0268	0381	0223			
0275	0265	0264	0381	0227			
0252	0246	0248	0358	0219			
0225	0225	0223	0328	0209			
0198	0198	0204	0296	0198			
0172	0174	0181	0261	0187			
0149	0155	0162	0230	0179			
0132	0138	0146	0202	0169			
0116	0124	0131	0180	0162			
0106	0115	0123	0166	0157			
0098	0107	0114	0152	0152			
0091	0101	0108	0143	0149			
0084	0095	0103	0133	0145			
0078	0090	0098	0123	0143			
0073	0086	0093	0117	0139			
0071	0082	0090	0110	0137			
0066	0079	0087	0104	0135			
0063	0077	0084	0099	0132			
0062	0076	0083	0096	0132			
0060	0074	0081	0093	0131			
0059	0074	0081	0093	0132			
0059	0073	0080	0092	0131			
0059	0073	0080	0091	0131			
0058	0073	0080	0091	0130			
0058	0072	0080	0090	0130			
.0001613	.0001399	.00008104	.00002212	.00002778			

C	EGLIN	SITE 1	LOC A-5	LD. CT.	3.11.76	6.00 .2	35
.5	.83333	1.75	2.75	3.75			
35	.200	25000.0					
0070	0082	0094	0122	0140			
0071	0084	0096	0126	0142			
0073	0086	0099	0132	0144			
0075	0088	0101	0138	0147			
0078	0092	0106	0148	0152			
0084	0097	0112	0159	0156			
0091	0104	0120	0176	0163			
0104	0115	0132	0197	0171			
0122	0132	0150	0227	0181			
0142	0149	0167	0251	0188			
0175	0179	0195	0293	0200			
0209	0208	0217	0320	0208			
0257	0250	0250	0359	0219			
0294	0277	0266	0372	0218			
0313	0296	0276	0380	0222			
0305	0298	0279	0387	0226			
0273	0275	0261	0365	0221			
0238	0247	0240	0337	0213			
0201	0214	0212	0298	0203			
0176	0188	0188	0265	0191			
0152	0165	0165	0226	0180			
0135	0147	0147	0197	0169			
0122	0132	0132	0171	0161			
0113	0122	0122	0154	0154			
0106	0114	0116	0142	0150			
0103	0110	0110	0132	0147			
0099	0109	0105	0125	0144			
0096	0105	0102	0120	0142			
0096	0103	0100	0116	0139			
0094	0103	0100	0115	0140			
0093	0102	0099	0113	0139			
0092	0101	0098	0111	0138			
0092	0100	0097	0111	0138			
0091	0100	0096	0109	0137			
0090	0099	0097	0110	0137			
.0001613	.0001399	.00008104	.00002212	.00002778			

C	EGLIN	SITE 1	LDC C-1	LD.CT.	3.10.76	7.0	.2	40
	.58333	.91667	1.83333	2.83333	3.83333			
40		.200 25000.0						
0018	0037	0054	0067	0102				
0019	0037	0055	0069	0103				
0020	0038	0056	0071	0103				
0021	0040	0059	0075	0103				
0024	0043	0060	0080	0103				
0026	0045	0063	0085	0104				
0029	0048	0068	0095	0103				
0033	0053	0073	0104	0104				
0039	0058	0079	0117	0105				
0047	0065	0087	0132	0107				
0059	0074	0096	0150	0111				
0075	0085	0109	0170	0117				
0097	0098	0123	0194	0124				
0121	0113	0137	0216	0129				
0149	0128	0153	0240	0153				
0184	0145	0167	0258	0142				
0222	0165	0183	0279	0145				
0249	0183	0194	0289	0146				
0263	0194	0201	0294	0146				
0260	0196	0202	0295	0147				
0250	0194	0202	0296	0148				
0227	0183	0195	0287	0150				
0202	0169	0183	0271	0147				
0171	0149	0164	0242	0139				
0144	0132	0148	0215	0131				
0117	0113	0128	0182	0122				
0096	0099	0113	0157	0116				
0079	0083	0097	0128	0110				
0064	0070	0083	0104	0105				
0054	0060	0073	0085	0104				
0046	0054	0065	0071	0104				
0042	0048	0060	0061	0104				
0038	0044	0055	0053	0104				
0035	0042	0052	0047	0103				
0035	0040	0050	0043	0103				
0034	0039	0050	0042	0103				
0034	0039	0050	0040	0103				
0034	0039	0049	0040	0103				
0034	0039	0049	0039	0103				
0034	0038	0048	0038	0103				
.0001613		.0001399	.00008104	.00002212	.00002778			

C	EGLIN	SITE 1	LDC C-1	LD.CT.	3.10.76	7.0	.2	54
	.58333	.91667	1.83333	2.83333	3.83333			
54		.200 25000.0						
0036	0055	0076	0095	0120				
0037	0056	0077	0098	0120				
0038	0057	0080	0101	0120				
0039	0059	0081	0104	0121				
0042	0061	0084	0108	0123				
0044	0064	0087	0116	0124				
0046	0067	0091	0121	0126				
0049	0070	0095	0127	0127				
0052	0075	0099	0134	0129				
0057	0080	0105	0143	0132				
0062	0084	0109	0150	0133				
0070	0091	0115	0160	0136				
0076	0098	0123	0170	0138				
0087	0106	0131	0183	0142				
0098	0114	0140	0195	0145				
0112	0126	0150	0210	0149				
0129	0137	0161	0226	0153				
0148	0150	0170	0239	0155				
0171	0164	0183	0255	0161				
0196	0178	0193	0267	0162				
0225	0191	0204	0284	0167				
0251	0200	0211	0293	0170				
0277	0211	0219	0304	0174				
0291	0216	0222	0310	0177				
0299	0217	0224	0314	0179				
0299	0215	0226	0323	0184				
0291	0207	0222	0319	0186				
0276	0195	0213	0308	0185				
0256	0181	0201	0293	0183				
0235	0171	0191	0277	0181				
0213	0159	0179	0258	0176				
0191	0147	0168	0238	0171				
0170	0134	0154	0215	0164				
0152	0123	0141	0195	0157				
0138	0113	0132	0179	0151				
0127	0106	0122	0163	0146				
0119	0098	0115	0148	0140				
0112	0094	0108	0138	0137				
0108	0090	0104	0128	0132				
0104	0086	0099	0120	0130				
0100	0083	0097	0114	0127				
0097	0080	0093	0107	0125				
0095	0079	0091	0102	0123				
0093	0077	0088	0094	0121				
0092	0075	0086	0092	0119				
0090	0074	0085	0087	0118				
0089	0073	0084	0084	0117				
0089	0071	0083	0083	0116				
0087	0071	0082	0081	0115				
0087	0070	0081	0079	0114				
0086	0070	0080	0077	0114				
0085	0070	0080	0077	0113				
0085	0069	0079	0074	0114				
0084	0069	0078	0074	0113				
	.0001613	.0001399	.00008104	.00002212	.00002778			



C	EGLIN	SITE 1	LDC C-2	LD.CT.	3.10.76	4.5	.2	56
56	.375	.708	1.625	2.625	3.625			
		.200 25000.0						
0035	0054	0074	0101	0117				
0037	0055	0075	0103	0118				
0038	0057	0078	0108	0119				
0039	0059	0079	0113	0120				
0041	0062	0083	0119	0121				
0044	0065	0087	0127	0124				
0047	0070	0093	0140	0127				
0052	0076	0099	0151	0130				
0056	0082	0107	0164	0133				
0062	0087	0113	0179	0138				
0068	0095	0122	0192	0142				
0074	0102	0130	0208	0146				
0082	0110	0139	0222	0150				
0088	0119	0148	0240	0154				
0096	0127	0157	0256	0157				
0106	0137	0168	0275	0162				
0114	0147	0178	0290	0167				
0123	0155	0187	0305	0169				
0133	0166	0197	0321	0173				
0145	0178	0208	0337	0176				
0160	0191	0220	0352	0178				
0176	0206	0232	0368	0180				
0191	0218	0241	0380	0180				
0208	0230	0251	0390	0190				
0225	0242	0261	0402	0180				
0239	0251	0267	0409	0179				
0247	0256	0271	0412	0178				
0250	0256	0272	0412	0174				
0250	0255	0273	0415	0174				
0246	0251	0272	0415	0174				
0236	0243	0264	0403	0171				
0226	0233	0256	0390	0166				
0212	0220	0244	0367	0158				
0196	0206	0229	0343	0150				
0179	0190	0211	0312	0141				
0164	0176	0196	0281	0132				
0150	0162	0180	0251	0124				
0138	0149	0166	0225	0117				
0129	0140	0156	0206	0114				
0121	0133	0147	0188	0110				
0115	0127	0140	0176	0110				
0110	0122	0133	0165	0108				
0105	0117	0129	0156	0108				
0100	0113	0124	0147	0107				
0098	0110	0121	0140	0106				
0094	0108	0116	0133	0106				
0091	0104	0113	0128	0105				
0089	0102	0110	0122	0106				
0086	0100	0109	0118	0106				
0085	0098	0107	0115	0106				
0082	0096	0104	0111	0107				
0081	0095	0103	0108	0105				
0081	0094	0102	0106	0105				
0079	0093	0101	0105	0102				
0079	0092	0100	0103	0102				
0079	0092	0099	0102	0104				
.0001613	.0001399	.00008104	.00002212	.00002778				

C	EGLIN	SITE 1	LDC C-2	LD.CT.	3.10.76	4.5	.2	53
.375	.708	1.625	2.625	3.625				
53	.200	25000.0						
0017	0030	0043	0068	0106				
0019	0031	0044	0070	0106				
0019	0032	0045	0072	0105				
0020	0033	0046	0075	0105				
0022	0034	0048	0079	0105				
0024	0036	0050	0082	0105				
0025	0038	0052	0088	0106				
0028	0041	0056	0094	0106				
0032	0045	0060	0102	0106				
0035	0050	0065	0113	0106				
0041	0054	0070	0125	0106				
0047	0061	0077	0138	0106				
0054	0068	0086	0155	0106				
0062	0076	0095	0172	0105				
0071	0085	0105	0189	0106				
0079	0093	0114	0205	0106				
0091	0104	0127	0225	0106				
0102	0114	0136	0240	0107				
0114	0125	0147	0259	0109				
0126	0136	0157	0271	0110				
0143	0150	0170	0292	0113				
0158	0164	0182	0308	0114				
0174	0178	0192	0323	0116				
0190	0191	0202	0333	0116				
0203	0203	0211	0346	0119				
0210	0210	0216	0352	0120				
0212	0214	0219	0356	0120				
0210	0216	0220	0362	0124				
0205	0215	0221	0365	0126				
0197	0210	0220	0365	0128				
0185	0201	0213	0357	0127				
0170	0189	0203	0343	0125				
0158	0178	0193	0327	0121				
0145	0166	0181	0307	0116				
0134	0152	0168	0285	0111				
0118	0139	0152	0258	0107				
0105	0125	0137	0229	0106				
0094	0113	0124	0202	0106				
0083	0102	0110	0175	0105				
0072	0090	0096	0148	0106				
0066	0082	0087	0130	0106				
0059	0075	0079	0114	0106				
0054	0068	0072	0100	0106				
0050	0063	0066	0088	0105				
0046	0058	0061	0078	0105				
0043	0054	0057	0069	0105				
0041	0051	0054	0063	0106				
0038	0049	0051	0056	0106				
0036	0047	0047	0052	0105				
0034	0047	0047	0048	0105				
0033	0045	0045	0046	0105				
0034	0044	0044	0045	0106				
0032	0044	0044	0044	0105				
.0001613	.0001399	.00008104	.00002212	.00002778				

C	EGLIN	SITE 1	LDC C-3	LD.CT.	3.10.76	4.5	.2	60
60	.375	.708	1.625	2.625	3.625			
	.200	25000.0						
0037	0060	0084	0118	0131				
0038	0061	0086	0121	0133				
0039	0062	0089	0127	0136				
0041	0065	0091	0134	0139				
0043	0067	0094	0140	0140				
0044	0068	0097	0145	0144				
0046	0071	0100	0153	0148				
0049	0074	0104	0163	0151				
0052	0078	0109	0177	0158				
0055	0082	0113	0186	0162				
0058	0086	0120	0198	0167				
0063	0091	0126	0212	0172				
0069	0099	0135	0230	0180				
0075	0106	0143	0245	0186				
0084	0115	0154	0268	0194				
0094	0126	0167	0295	0204				
0103	0136	0178	0317	0213				
0113	0147	0190	0340	0222				
0124	0158	0203	0362	0230				
0136	0170	0217	0386	0238				
0148	0182	0229	0407	0245				
0161	0197	0242	0428	0252				
0174	0210	0255	0450	0258				
0189	0224	0268	0472	0265				
0203	0235	0277	0485	0268				
0218	0248	0288	0501	0274				
0234	0259	0295	0513	0276				
0245	0265	0299	0520	0279				
0247	0264	0300	0521	0280				
0242	0259	0298	0521	0279				
0232	0248	0289	0503	0273				
0217	0237	0278	0482	0264				
0203	0222	0264	0454	0254				
0189	0209	0251	0426	0242				
0176	0196	0237	0399	0231				
0164	0183	0222	0370	0218				
0154	0173	0209	0343	0206				
0142	0163	0197	0315	0195				
0134	0153	0186	0295	0185				
0125	0145	0175	0271	0176				
0118	0138	0167	0252	0167				
0111	0130	0158	0233	0159				
0106	0126	0153	0221	0153				
0101	0121	0147	0208	0148				
0098	0118	0142	0198	0145				
0094	0114	0138	0190	0142				
0091	0111	0134	0181	0138				
0088	0108	0131	0175	0136				
0086	0107	0128	0171	0134				
0085	0105	0126	0166	0133				
0083	0103	0124	0163	0131				
0082	0102	0124	0159	0131				
0081	0100	0121	0157	0130				
0079	0099	0121	0154	0129				
0078	0099	0120	0153	0129				
0078	0098	0119	0152	0129				
0078	0098	0118	0151	0129				
0077	0097	0119	0150	0129				
0077	0097	0118	0150	0128				
0077	0097	0118	0149	0128				
.0001613	.0001300	.00008104	.00002212	.00002778				

C	EGLIN	SITE 1	LDC C-3	LD.CY.	3.10.76	4.0	.2	30
	.33333	.66667	1.58333	2.58333	3.58333			
50	.200	25000.0						
0036	0059	0080	0108	0126				
0038	0061	0083	0115	0129				
0041	0064	0086	0123	0132				
0044	0066	0091	0133	0136				
0048	0071	0096	0145	0142				
0052	0076	0102	0159	0148				
0056	0080	0108	0172	0153				
0063	0086	0116	0188	0160				
0068	0092	0122	0202	0166				
0073	0098	0131	0220	0174				
0083	0106	0140	0237	0181				
0091	0115	0151	0258	0189				
0101	0126	0162	0280	0198				
0114	0137	0175	0304	0208				
0127	0151	0188	0328	0217				
0144	0166	0203	0354	0228				
0160	0181	0218	0380	0237				
0177	0197	0232	0402	0245				
0195	0211	0244	0425	0252				
0210	0225	0256	0441	0259				
0224	0238	0268	0464	0265				
0233	0247	0275	0476	0268				
0238	0255	0283	0490	0273				
0232	0255	0287	0498	0275				
0220	0248	0284	0497	0275				
0204	0235	0273	0475	0269				
0186	0218	0257	0448	0259				
0169	0201	0241	0415	0246				
0152	0183	0221	0375	0229				
0135	0165	0199	0328	0210				
0120	0149	0178	0289	0192				
0107	0136	0163	0255	0179				
0098	0125	0150	0226	0167				
0089	0115	0137	0198	0153				
0081	0106	0125	0169	0141				
0075	0098	0116	0150	0132				
0068	0091	0106	0129	0125				
0064	0087	0102	0118	0120				
0061	0083	0098	0109	0117				
0057	0080	0095	0102	0115				
0055	0078	0092	0098	0113				
0054	0076	0090	0093	0111				
0053	0075	0088	0091	0111				
0052	0074	0088	0089	0111				
0052	0074	0088	0089	0111				
0051	0073	0087	0087	0111				
0050	0072	0087	0087	0111				
0050	0072	0088	0087	0111				
0050	0072	0087	0087	0110				
0050	0072	0087	0087	0111				
.0001613	.0001399	.00008104	.00002212	.00002778				

C	EGLIN	SITE 1	LOC C-4	LD.CT.	3.10.76	4.0	.2	61
	.33333	.66667	1.58333	2.58333	3.58333			
61	.200	25000.0						
0034	0054	0075	0107	0117				
0036	0055	0076	0111	0119				
0037	0057	0077	0115	0120				
0037	0058	0079	0120	0122				
0039	0060	0080	0125	0124				
0041	0062	0084	0131	0126				
0044	0066	0088	0139	0129				
0046	0069	0091	0147	0132				
0049	0072	0096	0156	0135				
0051	0075	0100	0165	0138				
0055	0079	0103	0172	0140				
0058	0083	0107	0181	0144				
0061	0087	0112	0191	0147				
0066	0092	0118	0203	0150				
0071	0098	0123	0214	0155				
0076	0103	0130	0226	0159				
0081	0109	0136	0237	0161				
0088	0116	0143	0250	0166				
0094	0124	0149	0263	0170				
0101	0132	0157	0277	0175				
0110	0140	0166	0292	0178				
0120	0151	0176	0309	0184				
0130	0161	0185	0326	0188				
0141	0172	0195	0343	0192				
0153	0184	0206	0359	0197				
0169	0199	0218	0378	0203				
0185	0212	0228	0389	0205				
0204	0227	0238	0400	0207				
0224	0242	0248	0411	0209				
0243	0255	0255	0419	0211				
0258	0263	0263	0427	0213				
0266	0266	0266	0428	0213				
0266	0266	0266	0430	0213				
0262	0265	0268	0436	0218				
0256	0261	0266	0436	0218				
0247	0254	0265	0432	0218				
0234	0242	0255	0416	0213				
0221	0230	0243	0393	0206				
0204	0214	0228	0361	0192				
0187	0199	0211	0325	0177				
0170	0181	0194	0292	0163				
0156	0168	0178	0259	0150				
0142	0155	0163	0226	0136				
0132	0144	0151	0202	0128				
0122	0136	0142	0183	0122				
0116	0130	0137	0171	0119				
0112	0125	0132	0162	0117				
0108	0121	0127	0155	0115				
0105	0118	0124	0149	0115				
0102	0116	0122	0144	0112				
0099	0113	0119	0140	0112				
0098	0112	0117	0136	0111				
0097	0111	0116	0134	0110				
0095	0110	0115	0132	0110				
0094	0110	0115	0130	0111				
0093	0108	0113	0129	0111				
0091	0107	0112	0128	0110				
0091	0105	0111	0127	0112				
0090	0105	0110	0127	0112				
0090	0104	0111	0126	0111				
0089	0104	0111	0126	0111				
	.0001613	.0001399	.00008104	.00002212	.00002778			

C	EGLIN	SITE 1	LDC C-4	LD.CT.	3.10.76	4.5	.2	38
.375	.708	1.625	2.625	3.625				
38	.200	25000.0						
0025	0041	0061	0080	0104				
0026	0042	0062	0081	0104				
0027	0043	0063	0082	0103				
0030	0045	0064	0086	0104				
0034	0050	0071	0100	0104				
0042	0058	0079	0121	0108				
0051	0066	0090	0144	0115				
0060	0076	0100	0166	0124				
0070	0086	0110	0188	0131				
0084	0100	0126	0217	0142				
0099	0114	0139	0243	0152				
0117	0133	0156	0274	0164				
0137	0151	0173	0303	0173				
0161	0173	0191	0332	0183				
0186	0194	0207	0358	0191				
0210	0213	0220	0376	0197				
0227	0229	0230	0390	0200				
0232	0234	0236	0394	0200				
0229	0236	0237	0401	0203				
0218	0232	0239	0408	0208				
0202	0222	0236	0409	0210				
0184	0204	0222	0386	0204				
0166	0188	0207	0356	0194				
0148	0172	0189	0321	0181				
0131	0154	0172	0285	0167				
0115	0138	0155	0249	0152				
0102	0124	0139	0216	0140				
0092	0111	0126	0186	0129				
0081	0100	0113	0157	0119				
0073	0091	0103	0136	0111				
0068	0085	0095	0118	0107				
0063	0078	0089	0104	0104				
0057	0073	0082	0091	0103				
0055	0070	0080	0084	0103				
0053	0068	0077	0080	0103				
0052	0066	0076	0078	0103				
0050	0064	0075	0075	0103				
0049	0064	0074	0075	0103				
.0001613	.0001399	.00008104	.00002212	.00002778				

C	EGLIN	SITE 1	LDC C-5	LD.CT.	3.10.76	4.5	.2	52
52	.375	.708	1.625	2.625	3.625			
		.200 25000.0						
0036	0058	0087	0124	0141				
0037	0059	0089	0130	0143				
0040	0062	0092	0139	0148				
0041	0063	0096	0148	0152				
0044	0068	0101	0161	0159				
0047	0072	0107	0175	0167				
0052	0077	0113	0189	0175				
0057	0083	0121	0209	0183				
0068	0097	0136	0238	0196				
0081	0112	0154	0273	0209				
0092	0126	0169	0303	0221				
0106	0141	0186	0335	0235				
0121	0158	0204	0369	0245				
0142	0181	0227	0408	0260				
0164	0202	0246	0438	0269				
0190	0228	0269	0472	0278				
0214	0250	0288	0497	0285				
0244	0277	0310	0531	0295				
0270	0295	0323	0545	0297				
0295	0312	0336	0561	0303				
0313	0321	0340	0567	0306				
0318	0322	0343	0566	0309				
0313	0318	0345	0568	0314				
0296	0304	0335	0568	0312				
0279	0288	0322	0549	0307				
0257	0267	0303	0514	0295				
0238	0250	0286	0483	0282				
0220	0233	0268	0447	0268				
0204	0218	0253	0418	0258				
0190	0204	0237	0390	0246				
0178	0192	0223	0361	0234				
0166	0181	0210	0333	0223				
0156	0171	0197	0309	0210				
0146	0161	0188	0289	0201				
0138	0153	0178	0269	0193				
0132	0148	0172	0253	0184				
0127	0142	0164	0240	0178				
0123	0139	0160	0231	0174				
0118	0134	0156	0221	0170				
0115	0132	0152	0212	0165				
0112	0129	0148	0204	0161				
0109	0127	0146	0199	0159				
0108	0124	0144	0194	0156				
0105	0123	0142	0189	0155				
0104	0121	0141	0186	0153				
0103	0121	0139	0184	0152				
0102	0120	0139	0182	0152				
0101	0119	0138	0181	0151				
0101	0119	0138	0181	0151				
0100	0119	0137	0180	0151				
0101	0118	0137	0180	0152				
0100	0117	0137	0180	0152				
.0001613	.0001399	.00008104	.00002212	.00002778				

C	EGLIN	SITE 1	LOC C-5	LD.CT.	3.10.76	5.0	.2	38
	.41667	.75	1.66667	2.66667	3.66667			
38	.200	25000.0						
0033	0041	0056	0072	0160				
0034	0044	0057	0075	0163				
0036	0044	0059	0080	0165				
0037	0046	0062	0088	0168				
0040	0049	0065	0095	0172				
0045	0054	0071	0108	0178				
0049	0059	0077	0121	0183				
0055	0065	0085	0138	0192				
0065	0074	0095	0158	0201				
0074	0084	0107	0181	0211				
0088	0096	0122	0210	0223				
0102	0110	0137	0241	0233				
0122	0130	0156	0276	0246				
0148	0153	0178	0313	0261				
0175	0179	0202	0352	0275				
0206	0206	0225	0386	0285				
0238	0233	0245	0415	0294				
0266	0256	0262	0436	0299				
0282	0271	0273	0449	0302				
0283	0279	0279	0461	0306				
0272	0276	0282	0466	0309				
0250	0263	0274	0458	0309				
0226	0240	0254	0425	0300				
0201	0217	0232	0388	0285				
0175	0190	0207	0336	0265				
0153	0168	0180	0284	0243				
0128	0141	0151	0224	0220				
0110	0120	0127	0181	0200				
0098	0107	0112	0151	0185				
0089	0098	0101	0125	0173				
0081	0090	0092	0106	0164				
0077	0085	0087	0094	0159				
0075	0082	0084	0087	0156				
0072	0080	0081	0083	0154				
0071	0078	0079	0079	0152				
0070	0077	0077	0077	0151				
0069	0076	0076	0075	0149				
0068	0075	0076	0073	0149				
	.0001613	.0001399	.00008104	.00002212	.00002778			



C	EGLIN	SITE 1	LDC A-4	LD. CT.	3.11.76	5.00 .2	41
	.41667	.75	1.66667	2.66667	3.66667		
41		.200 25000.0					
0108	0126	0139	0159	0175			
0110	0127	0139	0159	0175			
0110	0128	0140	0162	0177			
0111	0128	0142	0165	0178			
0112	0129	0143	0169	0180			
0113	0130	0146	0173	0182			
0116	0133	0148	0179	0185			
0117	0134	0150	0185	0187			
0121	0137	0154	0194	0191			
0124	0141	0159	0202	0195			
0128	0144	0163	0212	0198			
0132	0148	0168	0222	0202			
0139	0154	0175	0234	0207			
0146	0161	0182	0247	0211			
0155	0169	0191	0263	0216			
0166	0180	0202	0279	0221			
0181	0193	0216	0302	0227			
0200	0210	0232	0328	0235			
0230	0235	0253	0355	0242			
0267	0267	0278	0387	0249			
0302	0295	0302	0414	0254			
0338	0322	0323	0439	0260			
0374	0354	0343	0463	0265			
0391	0371	0354	0474	0267			
0387	0375	0358	0480	0271			
0363	0361	0349	0471	0268			
0327	0333	0327	0439	0260			
0290	0300	0300	0400	0249			
0254	0267	0267	0349	0234			
0222	0236	0236	0298	0215			
0196	0210	0208	0244	0196			
0178	0185	0190	0206	0182			
0164	0171	0176	0176	0171			
0157	0165	0168	0159	0166			
0147	0157	0150	0141	0158			
0145	0155	0147	0137	0158			
0143	0154	0147	0136	0158			
0142	0153	0146	0134	0157			
0142	0152	0146	0134	0158			
0142	0152	0145	0134	0158			
0141	0150	0145	0135	0158			
.0001613	.0001399	.00008104	.00002212	.00002778			

C	EGLIN	SITE 2	LDC A-1	LD.CT.	3.11.76	3.0	.2	70
70	.25	.58333	1.5	2.5	3.5			
		.200	25000.0					
0023	0055	0079	0104	0125				
0027	0060	0082	0108	0129				
0032	0067	0087	0115	0135				
0038	0073	0092	0120	0140				
0044	0079	0096	0125	0144				
0051	0086	0100	0131	0150				
0057	0094	0106	0136	0154				
0065	0101	0111	0144	0160				
0072	0111	0117	0150	0166				
0082	0120	0123	0157	0173				
0092	0130	0129	0165	0178				
0102	0141	0136	0172	0185				
0113	0152	0143	0179	0191				
0125	0163	0150	0186	0196				
0138	0175	0157	0194	0204				
0151	0187	0164	0201	0209				
0163	0198	0170	0208	0215				
0176	0209	0176	0214	0220				
0191	0221	0183	0221	0227				
0202	0230	0188	0226	0230				
0212	0239	0193	0230	0234				
0220	0245	0198	0235	0238				
0225	0251	0201	0237	0241				
0227	0253	0202	0239	0244				
0228	0254	0204	0241	0246				
0229	0256	0205	0244	0248				
0228	0255	0206	0246	0252				
0227	0254	0208	0250	0260				
0226	0253	0208	0252	0264				
0225	0252	0202	0239	0244				
0224	0251	0208	0253	0267				
0220	0246	0205	0251	0268				
0213	0240	0202	0248	0266				
0206	0233	0198	0244	0264				
0200	0228	0195	0241	0263				
0193	0220	0190	0236	0259				
0187	0214	0187	0232	0256				
0181	0208	0183	0228	0253				
0175	0203	0179	0224	0250				
0170	0197	0175	0220	0246				
0165	0192	0172	0217	0246				
0160	0187	0169	0213	0243				
0154	0181	0165	0208	0237				
0146	0173	0160	0202	0231				
0140	0167	0155	0196	0227				
0133	0159	0150	0189	0220				
0126	0153	0145	0184	0215				
0119	0146	0140	0177	0209				
0114	0140	0136	0173	0204				
0108	0135	0131	0166	0197				
0102	0129	0127	0161	0191				
0098	0123	0123	0157	0184				
0093	0119	0119	0152	0180				
0090	0116	0116	0149	0177				
0086	0114	0112	0144	0173				
0083	0112	0111	0142	0171				
0080	0109	0107	0140	0167				
0079	0102	0108	0136	0162				
0076	0102	0106	0134	0160				
0075	0098	0104	0131	0156				
0073	0097	0103	0131	0155				
0071	0096	0102	0130	0154				
0070	0095	0101	0127	0153				
0069	0094	0100	0127	0152				
0068	0092	0098	0125	0149				
0066	0090	0097	0123	0147				
0066	0089	0096	0122	0145				
0065	0088	0095	0120	0142				
0065	0086	0095	0119	0141				
0064	0085	0094	0118	0141				
.000040325	.000034965	.00004052	.00002212	.00001111				

	N	SITE 2	LDC A-2	LD.CT.	3.11.76	4.5	.2	72
68	.075	.708	1.625	2.625	3.625			
		.200	25000.0					
0140	0154	0165	0190	0207				
0141	0155	0166	0192	0208				
0142	0155	0166	0193	0209				
0144	0157	0167	0194	0211				
0146	0158	0168	0195	0213				
0146	0159	0169	0196	0215				
0147	0160	0170	0197	0216				
0150	0163	0172	0201	0219				
0153	0165	0174	0203	0224				
0155	0168	0176	0206	0227				
0159	0172	0179	0210	0232				
0163	0175	0182	0215	0237				
0167	0180	0186	0219	0243				
0174	0187	0190	0227	0252				
0180	0193	0195	0233	0260				
0189	0201	0201	0241	0271				
0198	0211	0209	0250	0280				
0209	0221	0217	0260	0292				
0221	0232	0224	0269	0303				
0235	0246	0234	0282	0315				
0252	0261	0245	0294	0327				
0269	0276	0255	0307	0340				
0290	0295	0268	0321	0354				
0310	0314	0280	0334	0367				
0335	0336	0293	0348	0382				
0357	0356	0305	0361	0392				
0382	0377	0319	0373	0405				
0399	0393	0328	0382	0412				
0409	0406	0337	0391	0419				
0416	0415	0342	0397	0425				
0421	0416	0345	0401	0430				
0425	0415	0350	0408	0438				
0424	0412	0351	0412	0444				
0412	0397	0348	0409	0444				
0396	0376	0335	0398	0435				
0376	0355	0323	0385	0424				
0355	0331	0308	0367	0407				
0334	0312	0295	0351	0390				
0313	0291	0281	0333	0371				
0295	0274	0268	0316	0351				
0277	0259	0255	0299	0331				
0261	0244	0244	0284	0313				
0248	0232	0232	0269	0295				
0236	0224	0222	0258	0279				
0226	0217	0213	0247	0266				
0218	0211	0206	0239	0256				
0211	0205	0202	0232	0247				
0205	0195	0201	0227	0241				
0201	0191	0198	0222	0234				
0197	0189	0196	0217	0229				
0192	0186	0192	0214	0226				
0189	0182	0190	0213	0223				
0188	0180	0188	0210	0220				
0187	0179	0187	0209	0219				
0185	0177	0186	0208	0218				
0183	0175	0185	0207	0217				
0184	0181	0173	0206	0216				

0184	0181	0173	0204	0214
0184	0180	0173	0204	0214
0183	0180	0171	0204	0214
0182	0179	0170	0204	0214
0182	0178	0170	0202	0213
0181	0178	0170	0203	0212
0182	0178	0169	0202	0212
0181	0177	0168	0202	0211
0180	0176	0167	0202	0212
0180	0176	0165	0202	0211
0180	0175	0164	0201	0211

.000040325 .000034965 .00004052 .00002212 .00001111

C	EGLIN	SITE-2	LOC C-1	LD.CT.	3.11.76	4.5	.2	70
	.375	.708	1.625	2.625	3.625			
70	.200	25000.0						
0041	0057	0117	0141	0192				
0041	0058	0117	0142	0194				
0042	0059	0118	0142	0194				
0043	0060	0118	0142	0194				
0044	0060	0119	0144	0195				
0045	0062	0119	0145	0197				
0047	0062	0120	0146	0197				
0049	0065	0121	0149	0200				
0052	0067	0123	0150	0202				
0054	0069	0125	0152	0204				
0056	0072	0127	0156	0207				
0060	0074	0130	0159	0210				
0063	0079	0132	0162	0213				
0067	0082	0134	0166	0217				
0072	0087	0138	0169	0220				
0078	0093	0142	0175	0225				
0085	0099	0146	0179	0229				
0092	0106	0151	0186	0235				
0101	0113	0155	0190	0239				
0111	0121	0162	0197	0244				
0122	0131	0169	0203	0249				
0136	0145	0177	0212	0257				
0152	0159	0186	0220	0263				
0171	0176	0196	0230	0271				
0193	0195	0208	0239	0278				
0220	0218	0220	0251	0286				
0250	0243	0236	0261	0293				
0284	0271	0251	0271	0299				
0315	0295	0263	0278	0305				
0348	0320	0277	0284	0306				
0376	0341	0285	0288	0308				
0402	0362	0294	0293	0308				
0419	0378	0301	0296	0308				
0427	0390	0307	0299	0311				
0426	0398	0312	0304	0315				
0418	0400	0313	0309	0320				
0401	0391	0311	0309	0325				
0368	0365	0297	0298	0320				
0327	0330	0280	0284	0313				
0297	0305	0267	0273	0306				
0268	0279	0252	0260	0298				
0242	0255	0238	0247	0289				
0215	0229	0223	0234	0277				
0193	0207	0210	0222	0268				
0173	0189	0199	0210	0259				
0159	0173	0188	0201	0249				
0145	0159	0179	0191	0242				
0134	0147	0171	0183	0234				
0125	0137	0164	0175	0227				
0115	0127	0157	0168	0220				
0110	0120	0152	0163	0215				
0103	0114	0147	0157	0210				
0099	0108	0143	0153	0206				
0095	0104	0139	0150	0204				
0092	0101	0138	0148	0202				
0088	0098	0135	0146	0200				
0087	0096	0134	0145	0199				
0085	0095	0134	0144	0199				
0083	0093	0132	0143	0198				
0083	0092	0132	0143	0198				
0082	0091	0132	0142	0198				
0080	0089	0132	0142	0198				
0080	0089	0131	0142	0198				
0079	0089	0130	0142	0198				
0079	0087	0130	0141	0197				
0079	0087	0130	0141	0197				
0079	0087	0130	0141	0198				
0077	0087	0130	0141	0197				
0077	0087	0130	0142	0197				
0076	0087	0130	0142	0198				
.000040325	.000034965	.00004052	.00002212	.00001111				

C	EGLIN	SITE-2	LOC C-2	LD.CT.	3.11.76	4.0	.2	60
	.33333	.66667	1.58333	2.58333	3.58333			
60	.200	25000.0						
0071	0087	0105	0130	0157				
0073	0088	0106	0132	0160				
0076	0090	0107	0132	0162				
0077	0092	0109	0134	0163				
0079	0094	0110	0136	0165				
0081	0097	0112	0139	0168				
0085	0100	0114	0141	0171				
0089	0103	0117	0143	0173				
0094	0109	0121	0148	0178				
0100	0114	0124	0152	0181				
0109	0122	0130	0158	0187				
0117	0130	0136	0163	0192				
0129	0142	0142	0170	0198				
0140	0154	0152	0177	0205				
0158	0169	0163	0187	0214				
0174	0183	0172	0192	0218				
0195	0203	0184	0202	0226				
0216	0222	0197	0208	0232				
0242	0247	0211	0218	0239				
0269	0269	0225	0224	0244				
0301	0297	0241	0232	0250				
0330	0320	0253	0235	0251				
0364	0345	0266	0240	0254				
0390	0364	0276	0242	0256				
0415	0384	0287	0246	0259				
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0435	0407	0297	0251	0263				
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0382	0382	0283	0255	0270				
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0133	0142	0130	0157	0181				
0131	0139	0129	0154	0178				
0128	0136	0128	0152	0176				
0126	0133	0126	0150	0174				
0126	0133	0125	0150	0172				
0125	0132	0125	0150	0172				
0124	0130	0124	0148	0170				
0124	0129	0123	0148	0169				
0122	0129	0122	0146	0169				
0121	0127	0121	0146	0168				
0121	0127	0121	0145	0168				
0121	0126	0120	0145	0167				
0119	0126	0121	0145	0167				
0118	0125	0121	0145	0167				
0118	0125	0121	0145	0166				
0117	0124	0121	0145	0166				
0117	0125	0121	0144	0167				
0117	0124	0121	0144	0166				
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NONCONTACT NONDESTRUCTIVE DETERMINATION OF PAVEMENT  
DEFLECTION UNDER MOVING LOADS(U) PURDUE RESEARCH  
FOUNDATION LAFAYETTE IN M E HARR ET AL AUG 77

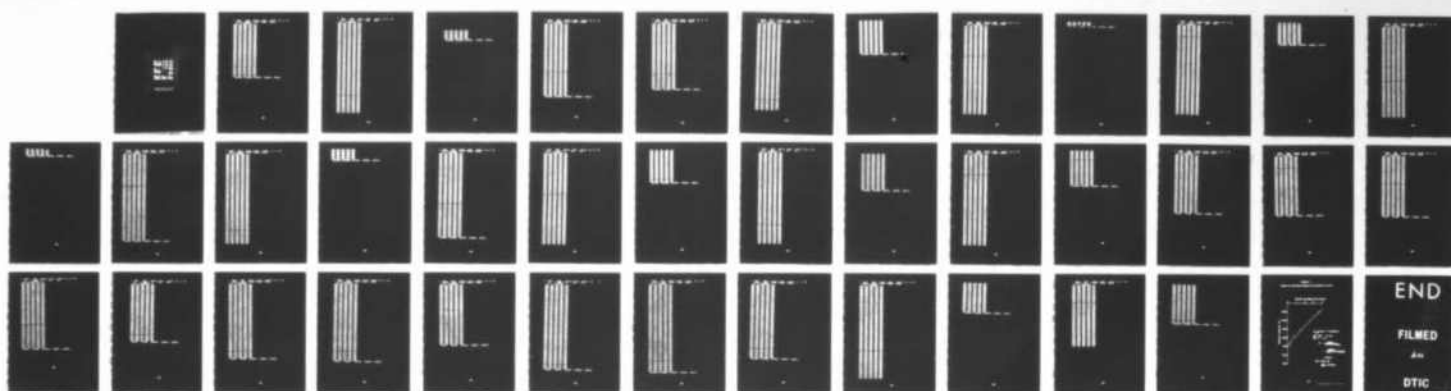
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RESOLUTION TEST CHART  
NATIONAL BUREAU OF STANDARDS-1963-A





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200-20 210-2 100-4 100-7 200-70 4.0 .2 70



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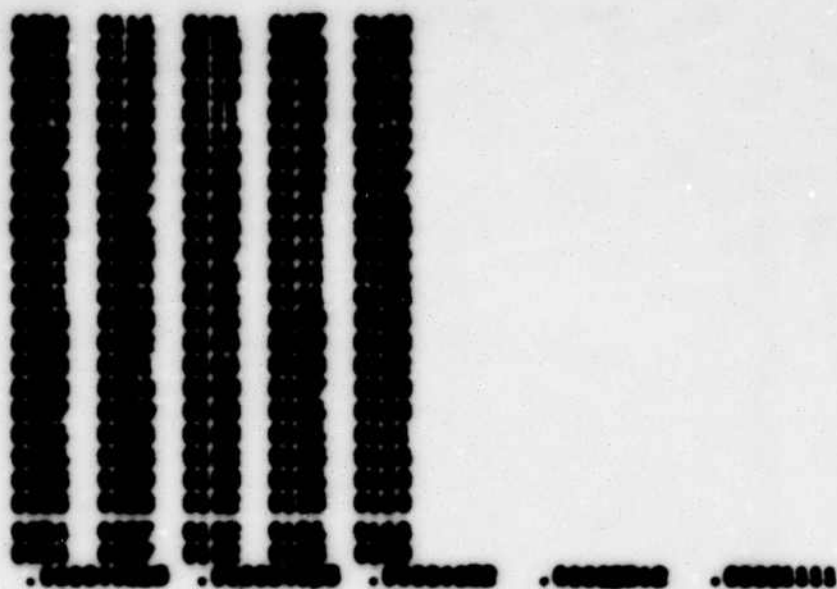




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| 0110 | 0108 | 0106 | 0104 | 0102 |
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| 0115 | 0105 | 0103 | 0101 | 0099 |
| 0114 | 0104 | 0102 | 0100 | 0098 |
| 0113 | 0103 | 0101 | 0099 | 0097 |
| 0112 | 0102 | 0100 | 0098 | 0096 |
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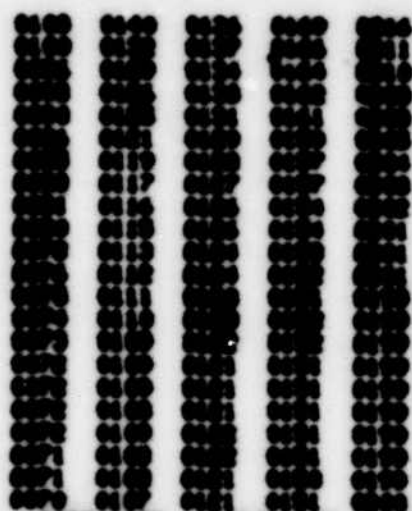




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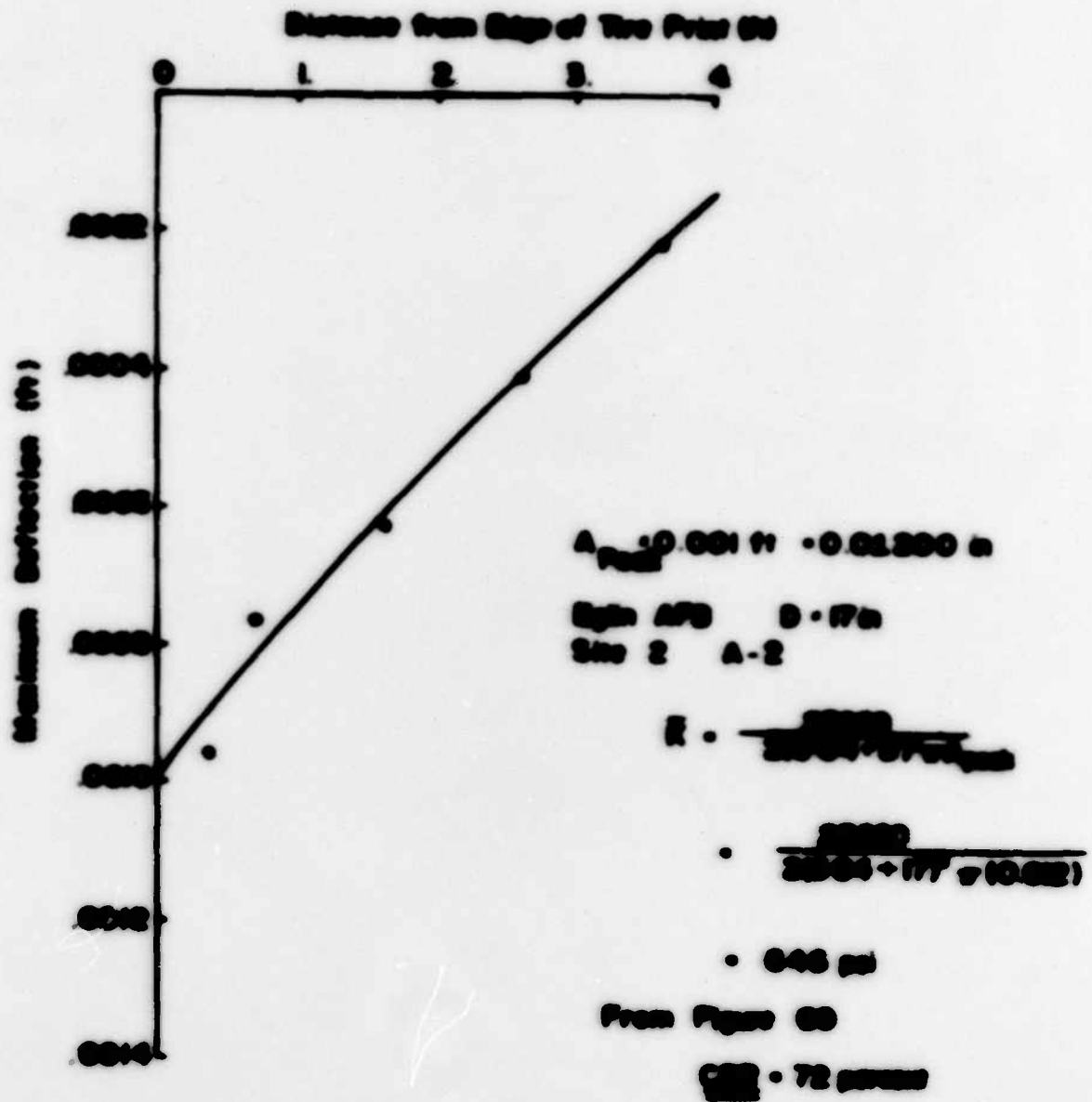
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# APPENDIX E

## EXAMPLE OF SUBLIFTED FLOORING FOR ESTIMATING $\epsilon$ AND $C_{SE}$



**END**

**FILMED**

**2-86**

**DTIC**